

# Neutron Elastic Scattering Differential Cross Sections on $^{13}\text{C}$

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FIBERTEK, INC.



## FiberTek, Inc

Jarrold Marsh

- Preface: What are “nuclear data”?
- Motivations for  $^{13}\text{C}$  measurements
- Measurement Techniques
- $^{13}\text{C}$  Results to date



U.S. DEPARTMENT OF  
**ENERGY**

Supported by U.S. DoE FY20/21/22/23 awards  
SC0021424, SC0021243, SC0021175, SSC000056

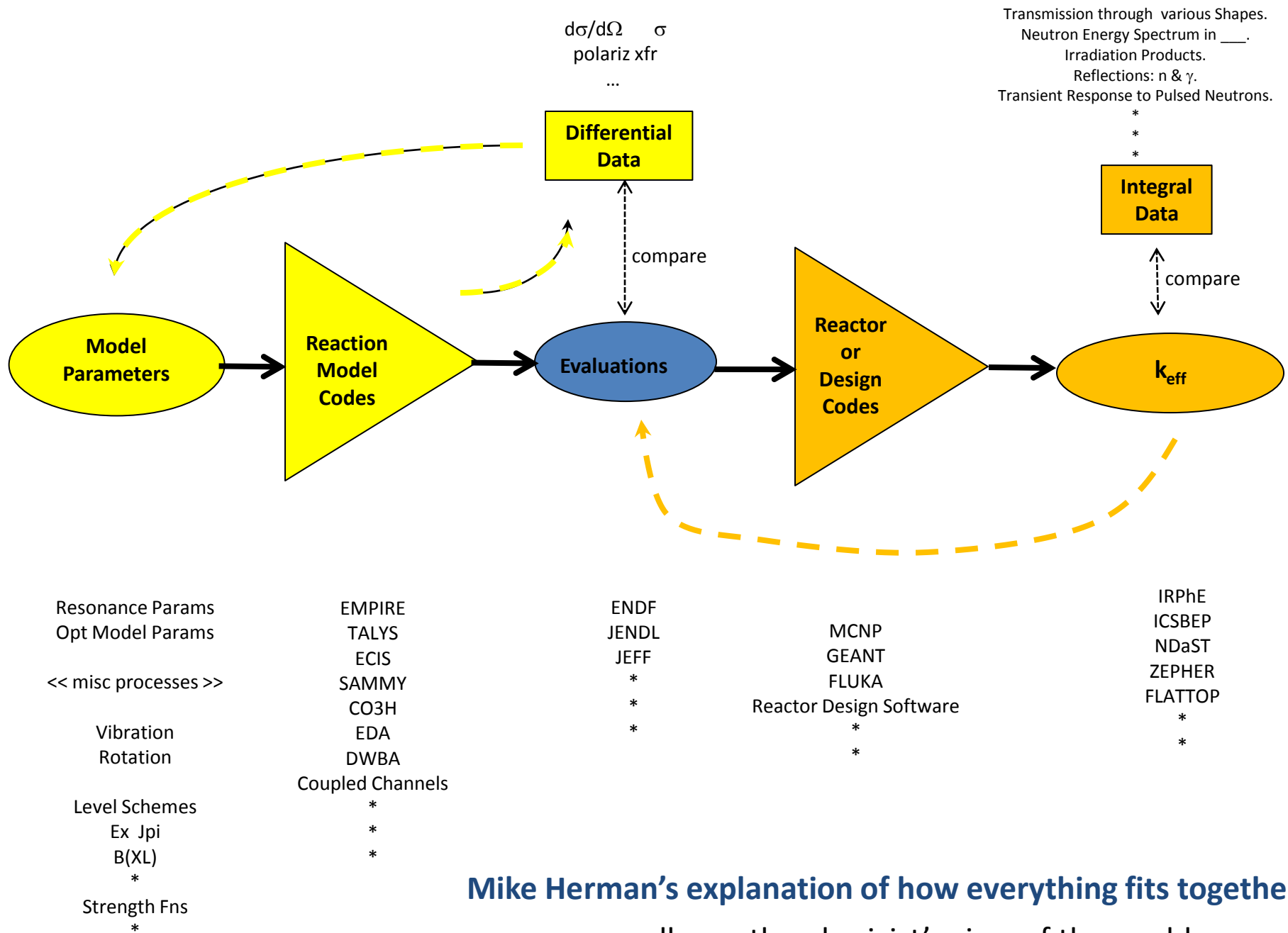


- “Nuclear Data” or “the Evaluations” or “Data Libraries” are:
  - Recommended set of cross sections intended to be used together
  - Experimental “differential” data guided by reaction model calculations.
  - Reaction Model calculations guided by “differential” & “integral” experimental data
  - Judged by a specific evaluation team
    - ENDF
    - JENDL
    - JEFF
  - for the evaluation team’s directed purpose
  - These are **not** “standards” (as in NIST stds or JRC/BRC/IRMM stds)



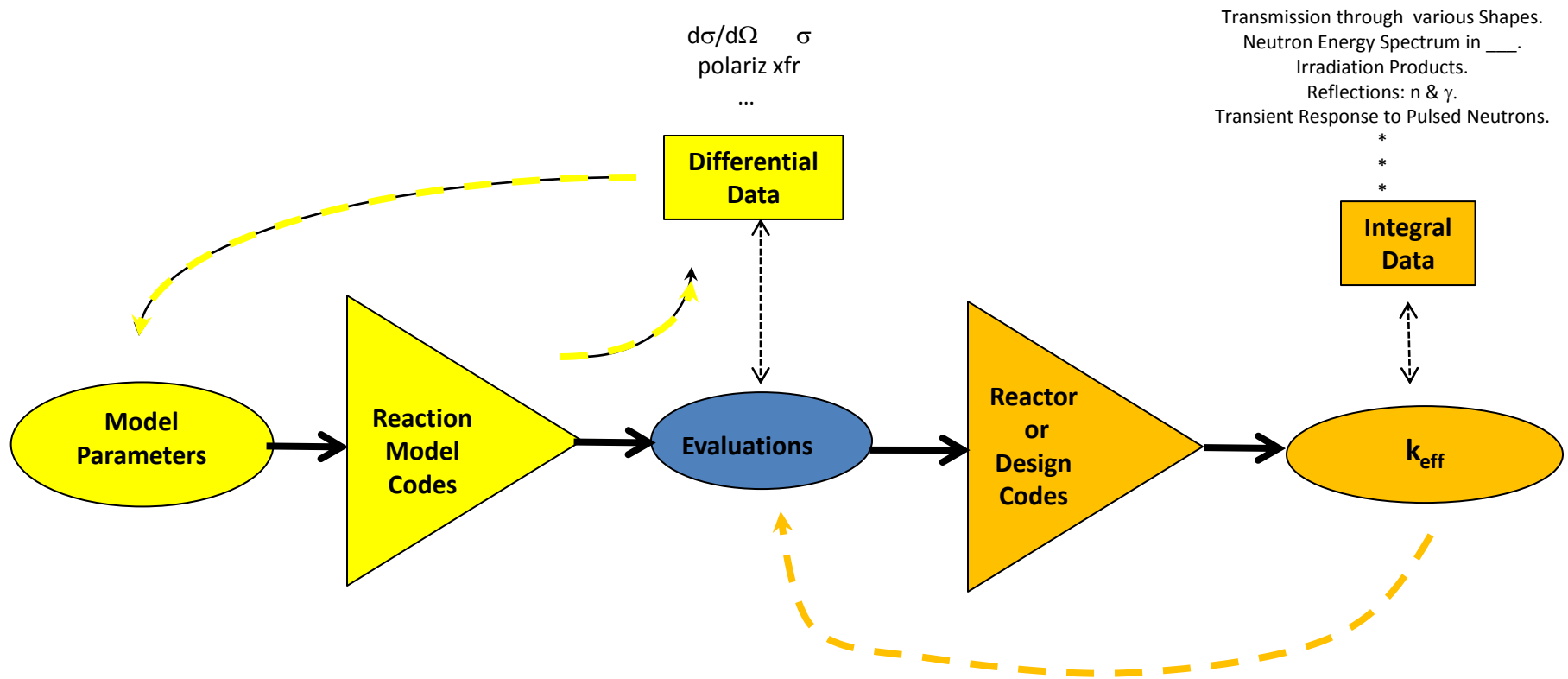
- Consumed by:
  - Nuclear Power Industry
  - Nuclear Propulsion
  - Dosimetry & Cancer Treatment Centers
  - “Stockpile Stewardship”
  - Physicists & Chemists

Shockingly, we are not the big users.



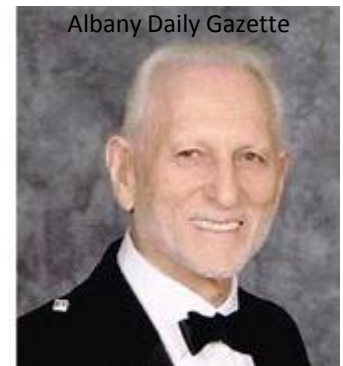
**Mike Herman's explanation of how everything fits together**

yellow – the physicist's view of the world  
orange – the engineer's view of the world.



## Cecil Lubitz' Rules about data:

- We will never be able to measure XS well enough for the reactor design codes.
- We will never be able to calculate XS well enough for the reactor design codes.
- When we measure cross section, we have no way to objectively determine the true accuracy.
- What we can check are the agreements between differential & integral data.
- Experimental measurements establish a "volume" for the answer rather than the "value".
- The Evaluator is free to change the values for the integral measurement to be best.
- If two things agree, they both may be wrong.



1925-2021  
 USNA '45  
 One of the  
 ENDF founders  
 4

# Motivations

## Undergraduate students on the Carbon paper

data taken 2011-2016 & 2016-2020

64 (n,n') ang distrib at 45 incident energies btw 0.5 - 8 MeV  
+ 12 (n,n'γ) btw 5.6-7.8 MeV

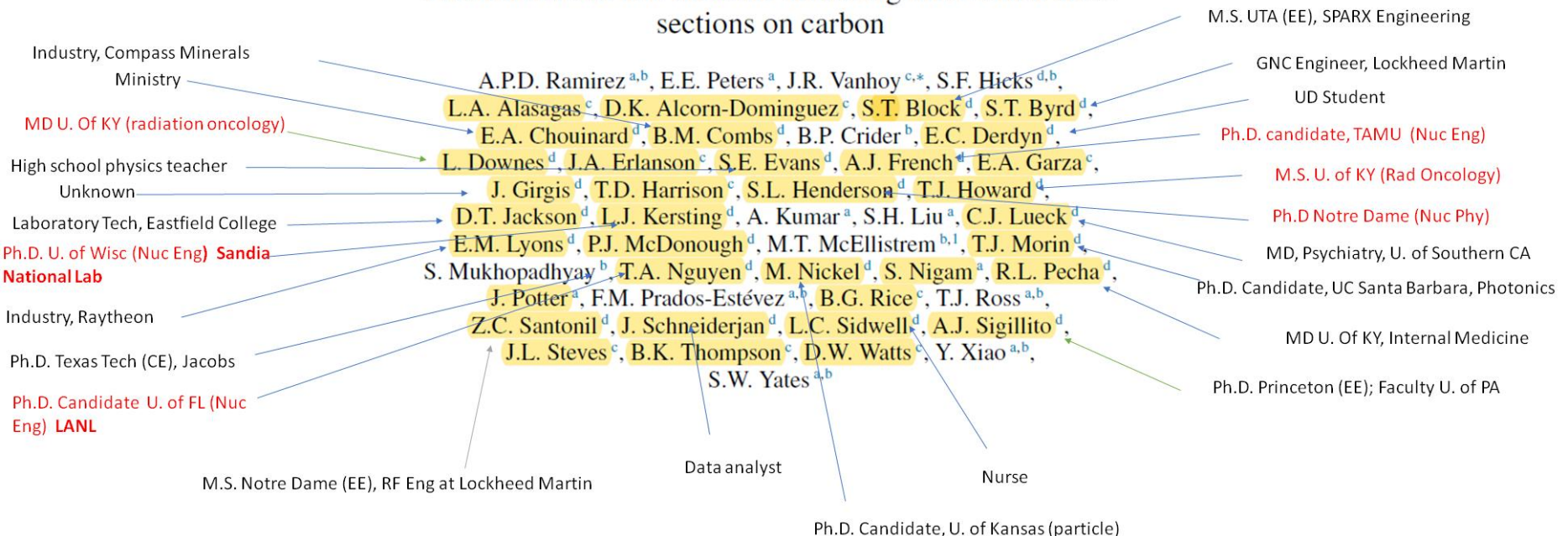
a monster project

ELSEVIER

Nuclear Physics A 1023 (2022) 122446

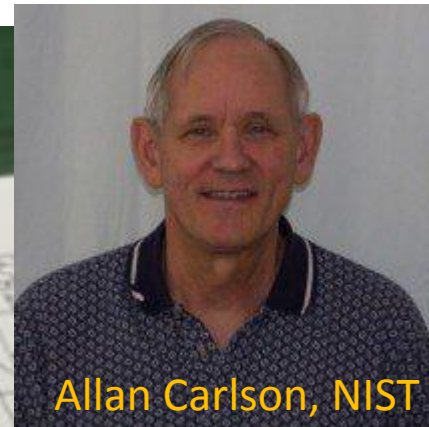
www.elsevier.com/locate/nucphysa

### Neutron elastic and inelastic scattering differential cross sections on carbon



~ "Since you did  $^{nat}\text{C}$ , perhaps you can do  $^{13}\text{C}$ ...

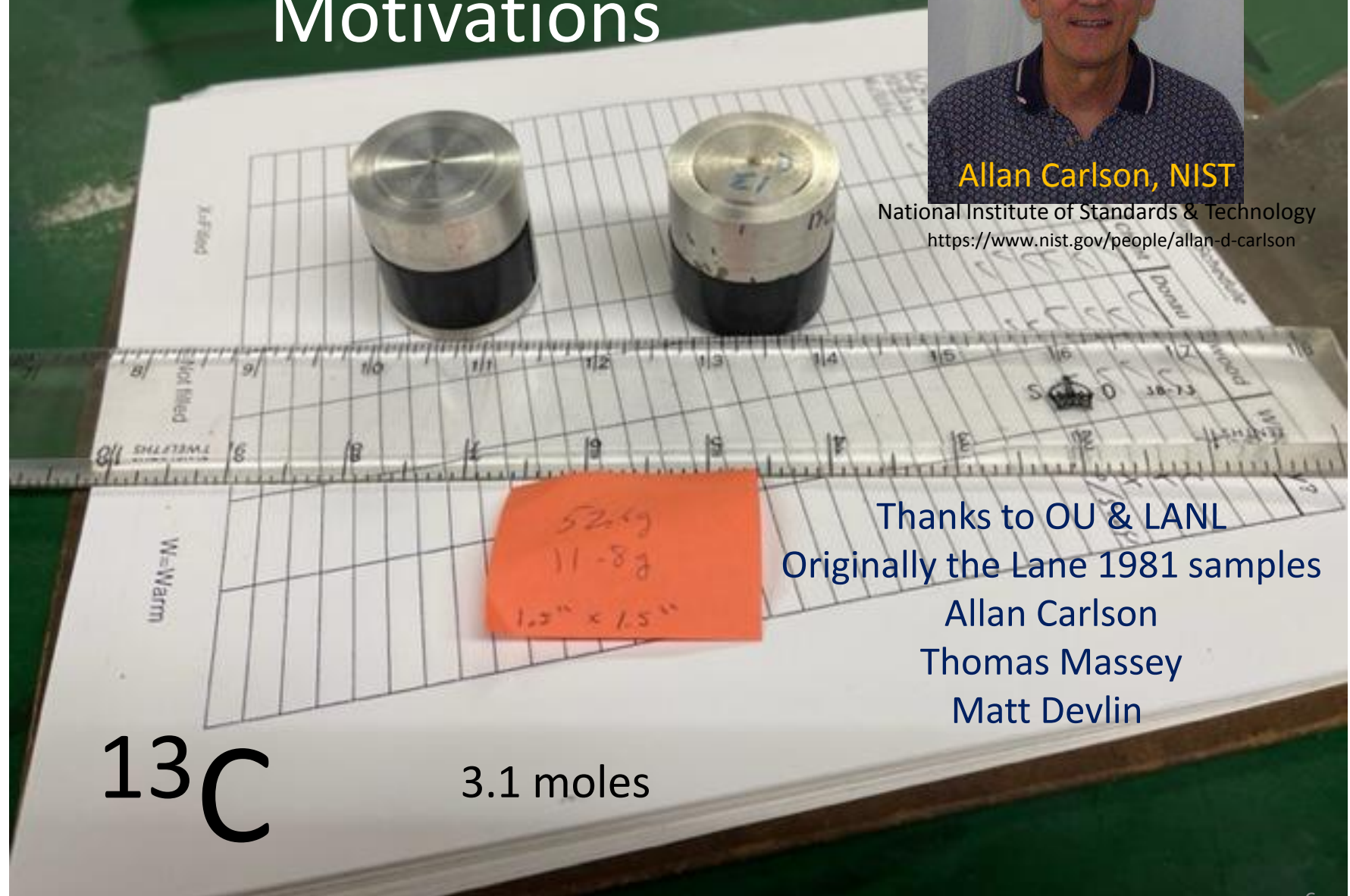
# Motivations



Allan Carlson, NIST

National Institute of Standards & Technology

<https://www.nist.gov/people/allan-d-carlson>



Thanks to OU & LANL

Originally the Lane 1981 samples

Allan Carlson

Thomas Massey

Matt Devlin

$^{13}\text{C}$

3.1 moles



# Motivations

ENDF 7.1  
2011

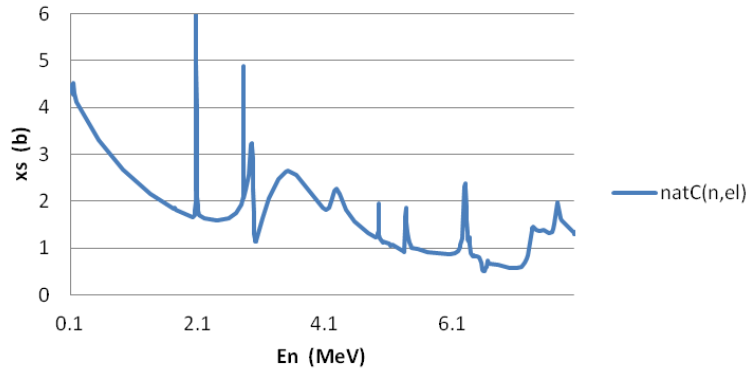
ENDF 8.0  
2018



ENDF 8.1  
soon

some were happy  
some were surprised  
some were upset  
some were mad

natC(n,el) ENDF7.1



very small  
abundance fluctuations

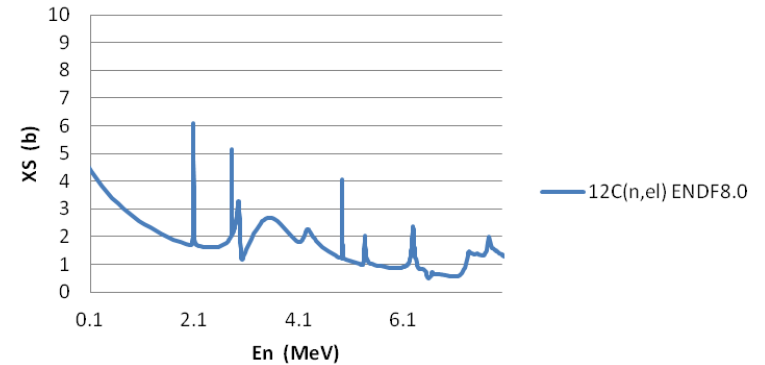
$\pm 5$

0.9890

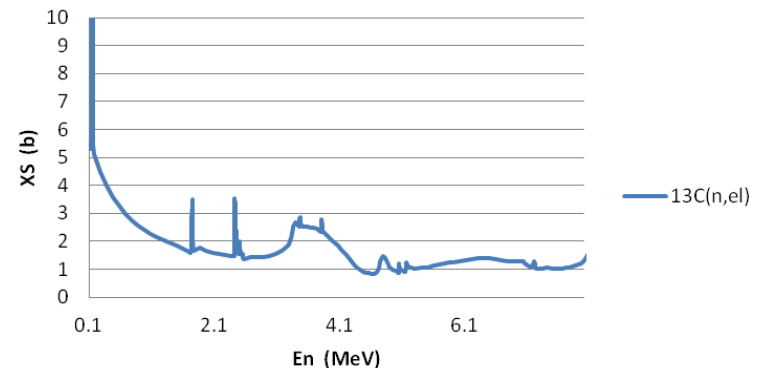
0.0110

$\pm 5$

$^{12}\text{C}(\text{n,el})$  ENDF8.0



$^{13}\text{C}(\text{n,el})$  ENDF8.0



natC is a xs *standard*

btw 1 keV and 1.8 MeV

uncert 0.68 - 0.71%

Carlson NDS 110, 3215 (2009)

Carlson NDS 148, 143 (2018)

“Evaluation of Nuclear Data Stds”

# Motivations

Carlson NDS 148, 143 (2018) “Evaluation of Nuclear Data Stds”

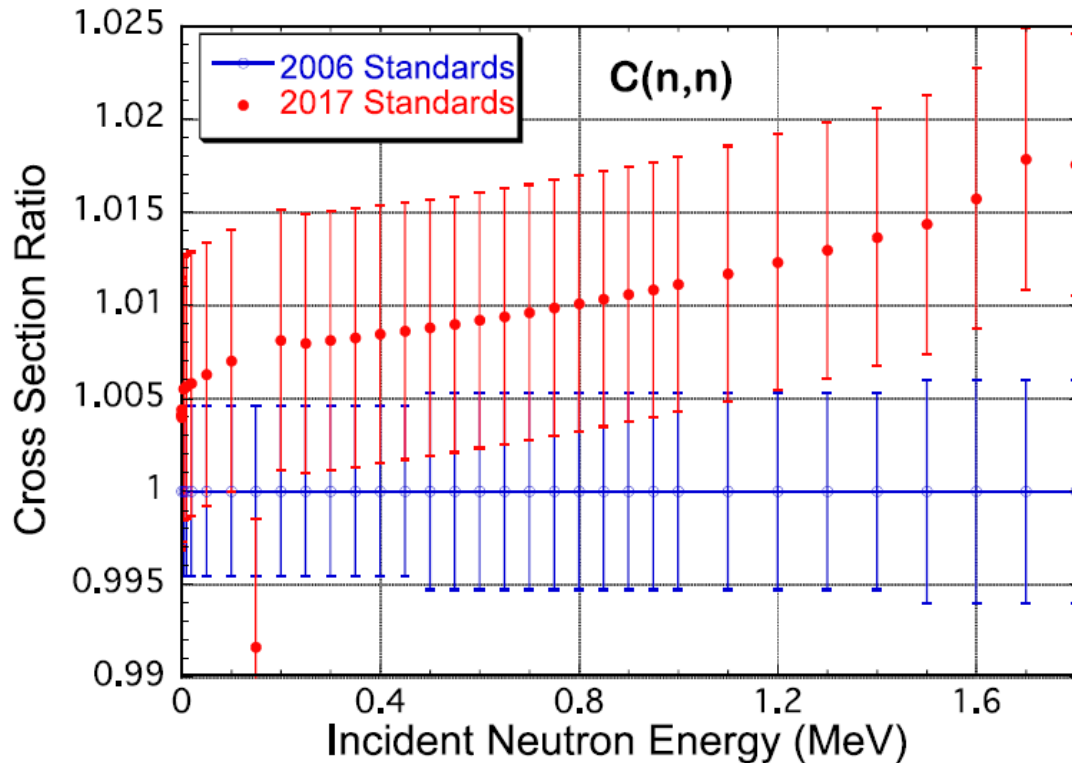


FIG. 18. (Color online) Comparison of the carbon total elastic cross section for the 2017 evaluation with the 2006 standards evaluation. The unrecognized systematic uncertainty of 0.65 % has been included in the 2017 data. The baseline at 1.00 is the 2006 standards evaluation. The structures at about 0.15 MeV and 1.76 MeV are a result of changes in the evaluated  $^{13}\text{C}$  total cross section.

## Worries

that the 2017 & 2006 values differ by more than the uncertainty

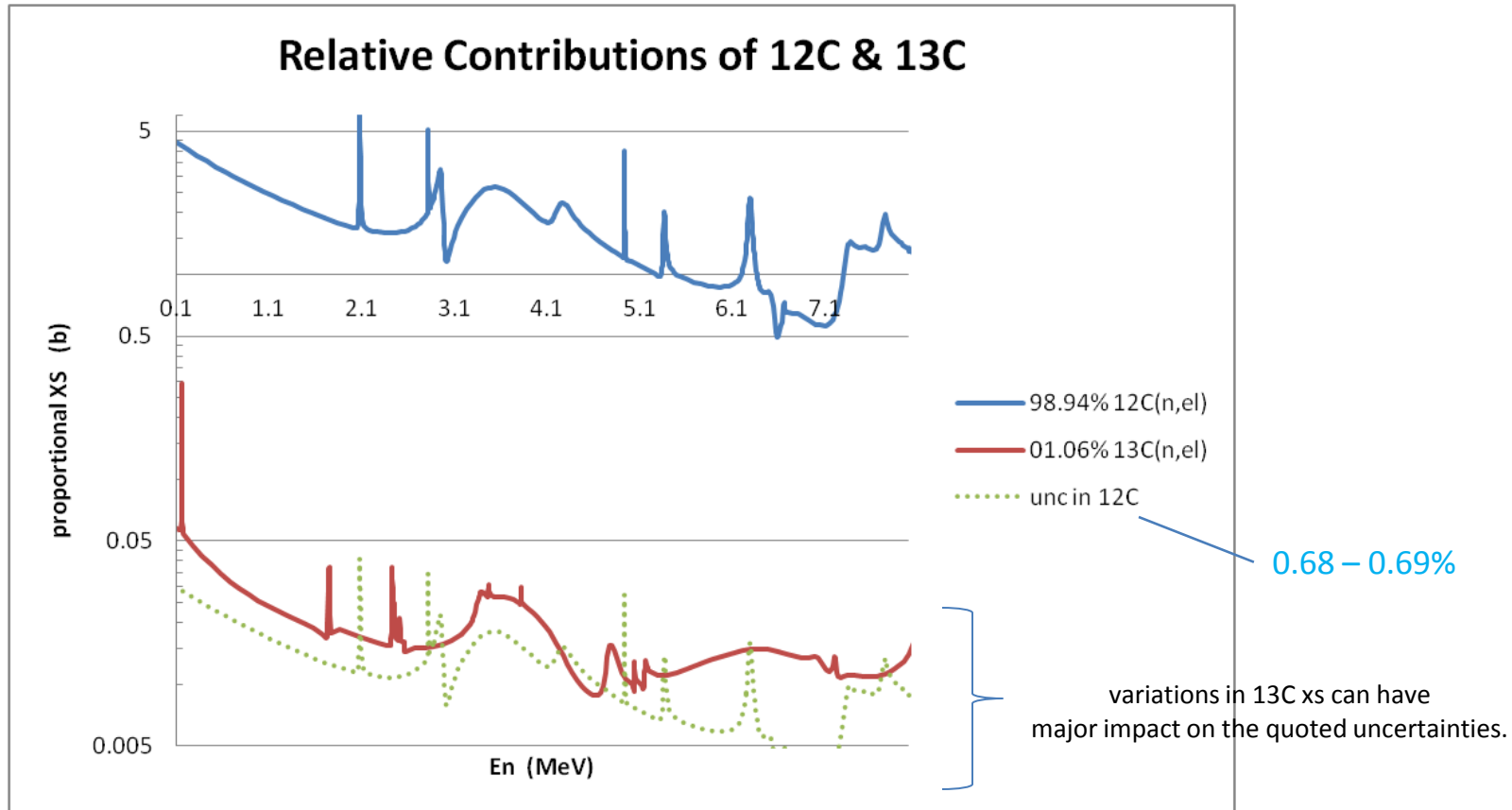
Alan Carlson “Recent Standards Work”  
CSEWG 2023 @ BNL Nov 2022

Differences are due to  
addition of  $^{13}\text{C}$  information

Recent RPI data indicate  
less discrepancy in  
0.15 - 0.40 MeV region.



# Motivations



**Modeling cross sections (even in the 'plain' regions) requires a huge amount of information.**

Potential scattering (think: OM + corrections)

Resonances (+ CN state properties, mixing, interference, subthreshold tails)

ALSO: The ENDF recommended values are deduced by examination of the CN and not an individual reaction channel.

Gerry Hale  
Mark Paris

# Motivations

## Previous work on $^{13}\text{C}$

PHYSICAL REVIEW C VOLUME 23, NUMBER 5 MAY 1981

### States in $^{14}\text{C}$ from $\sigma_T$ and $\sigma_{el}(\theta)$ for $^{13}\text{C}+n$ : Measurement, $R$ -matrix analysis, and model calculations

R. O. Lane, H. D. Knox, and P. Hoffmann-Pinther  
John E. Edwards Accelerator Laboratory, Ohio University, Athens, Ohio 45701

R. M. White  
University of California, Lawrence Livermore National Laboratory, Livermore, California 94550

G. F. Auchampaugh  
University of California, Los Alamos National Scientific Laboratory, Los Alamos, New Mexico 87545  
(Received 16 October 1980)

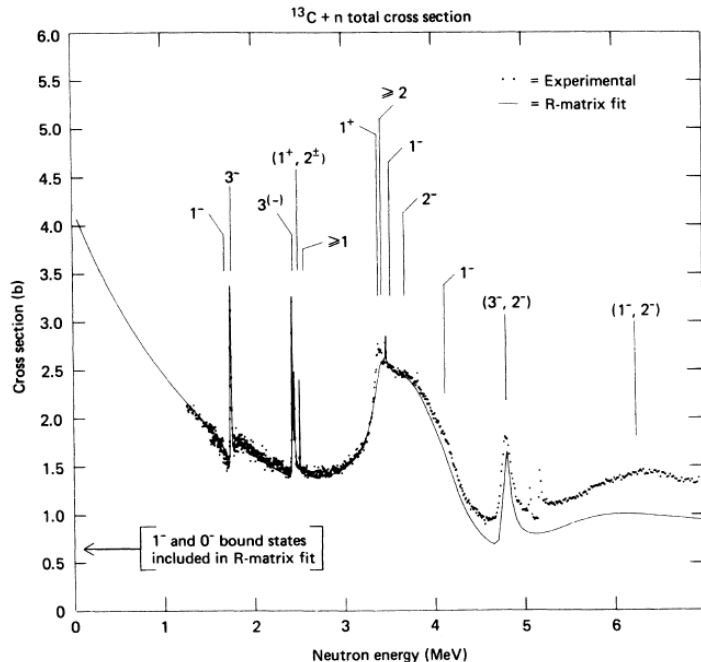


FIG. 3. Total cross section  $\sigma_T$  (points) from Ref. 7 and integrated elastic scattering cross section  $\sigma_{el}$  (curve) from  $R$ -matrix analysis for  $^{13}\text{C}+n$ . The  $J^\pi$  assignments and approximate locations for states in  $^{14}\text{C}$  resulting from the  $R$ -matrix analysis are indicated in the figure. Only a representative number from the full set of data points for  $\sigma_T$  are shown to portray adequately the features of the total cross section. The scatter in the points is taken as the measure of errors on  $\sigma_T$ . For the  $1^-$  resonance near 1.75 MeV the location of the resonance dip is indicated rather than the calculated resonance energy (see Fig. 4).

Experimental  $\sigma_{\text{tot}}$   
total Cross section  
measured at the old  
LANL Tandem.

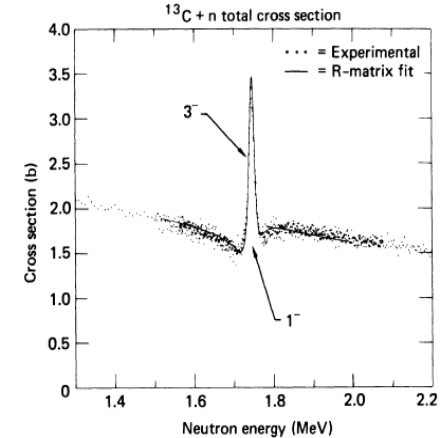
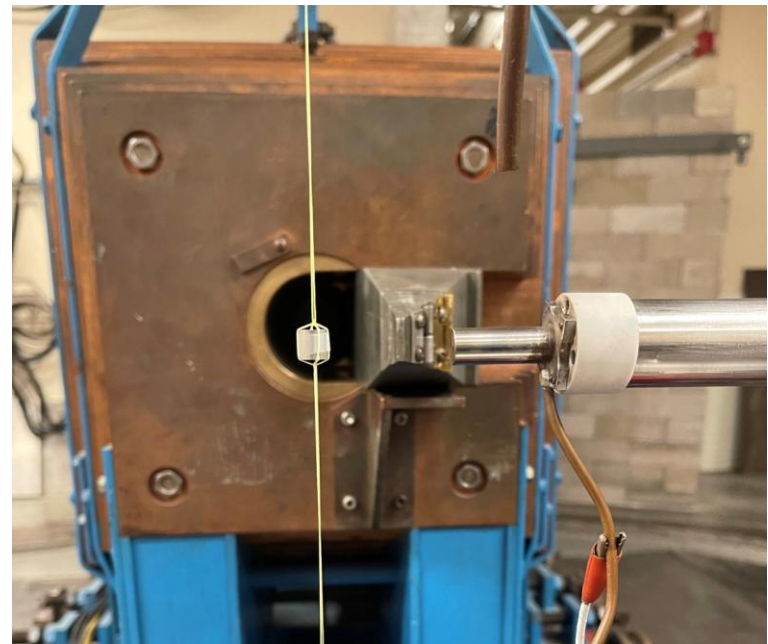


FIG. 4. Expanded plot of the total cross section (points) from Ref. 7 and integrated elastic scattering cross section (curve) from  $R$ -matrix analysis for  $^{13}\text{C}+n$  for the resonances near 1.75 MeV. The curve has been averaged over the experimental resolution of FWHM  $\approx 3.5$  keV. Note that in Table I the energy of the  $3^-$  resonance (peak) is actually slightly lower than that of the  $1^-$  resonance (dip). The apparent reversal of this order occurs in this case because of the slight asymmetry of the  $1^-$  dip and the nearly equal energies of the resonances. The full data set for  $\sigma_T$  is shown from  $E_n \approx 1.6$  to 2.0 MeV while only a partial set is displayed outside this region to aid in relating to other figures. The scatter in the points is taken as a measure of the errors.

Most previous measurements do not go below  $\sim 1$  MeV.

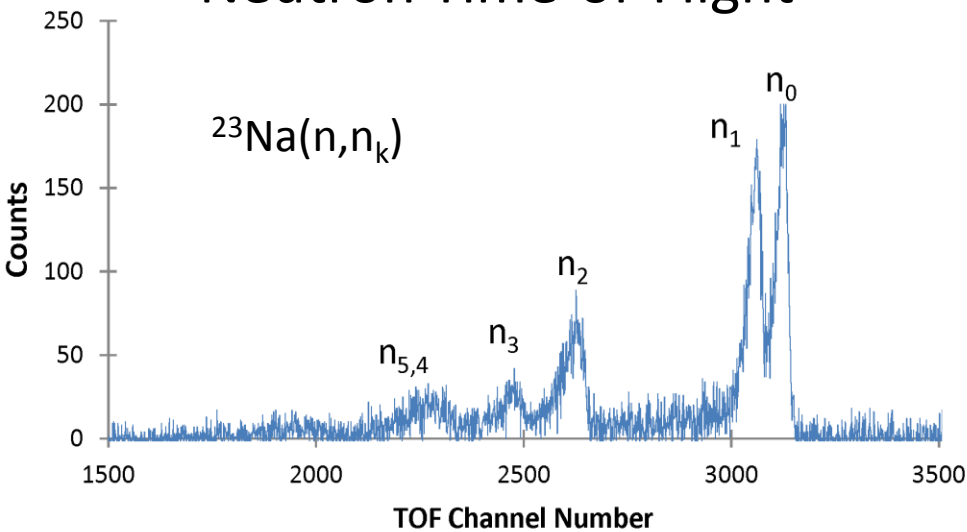
## Quick reminders about the University of Kentucky Accelerator Lab programs

- **Accelerator**
  - HVEC Model CN: 7 MV
  - rf source
  - p, d,  $^3\text{He}$ ,  $\alpha$ , ... ions
  - Authorized for  $^3\text{H}$  gas targets
  - measure exit neutron energy
  - 1 ns pulse widths every 533 ns
- **Basic Nuclear Science**
  - Nuclear Structure via (n,n' $\gamma$ )
    - Level Schemes & Transitions
    - Spectroscopic Information
    - DSAM Lifetimes
  - ( $^3\text{He}$ ,n $\gamma$ )
- **Applied Nuclear Science**
  - Differential (n,n') Cross Sections
    - $^{12,13}\text{C}$ ,  $^7\text{Li}$ ,  $^{19}\text{F}$ ,  $^{54,56}\text{Fe}$ ,  $^{23}\text{Na}$ ,  $^{28}\text{Si}$
  - Detector Development
    - Univ Guelph / TRIUMF
  - measurements for 'friends'





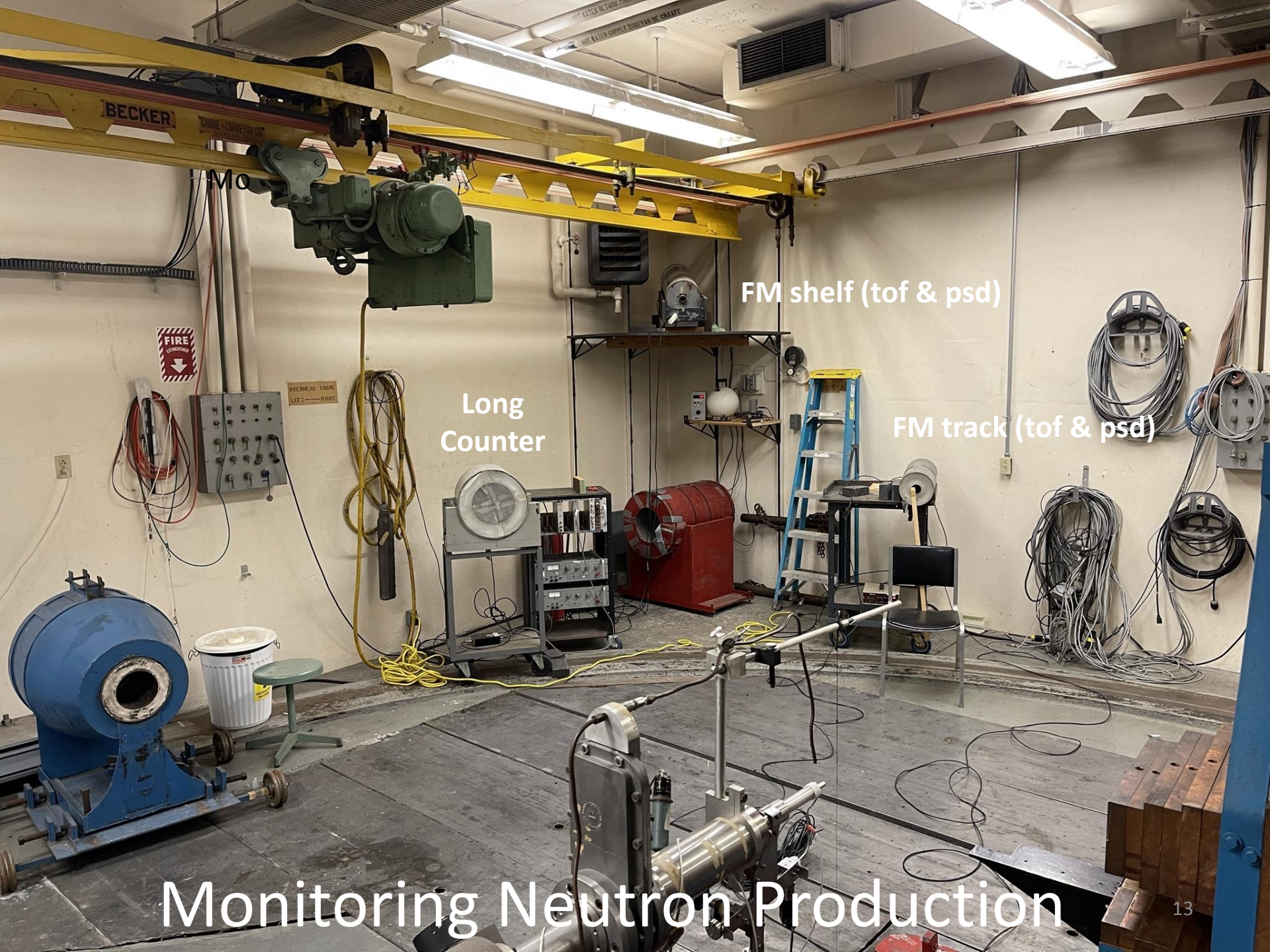
# Neutron Time-of-Flight



Pulsed beam. PSD.  
Exit channel neutrons sort by flight time.







Mo

FM shelf (tof & psd)

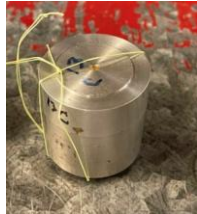
Long  
Counter

FM track (tof & psd)

Monitoring Neutron Production

# The Basic Idea for Processing Measurements

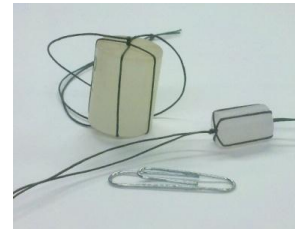
$^{13}\text{C}$  Differential Cross Sections are measured wrt to  $\text{H}(n,n)$



Sample spectrum



Container spectrum



Polyethylene spectrum

xs unc  
0.35 – 0.43%  
&  
isotropic in cm

$\text{H}(n,n)$   
elastic scattering  
differential cross  
sections are used as  
our standard

3

$^{13}\text{C} \leftarrow \text{Sample} - \text{Cont.}$

1

Correct for Detector Efficiency

4

Convert to raw Cross Section

2

\*Correct for Atten & Multiple scatt

Extract Peak Yields

Correct for Detector Efficiency

\*

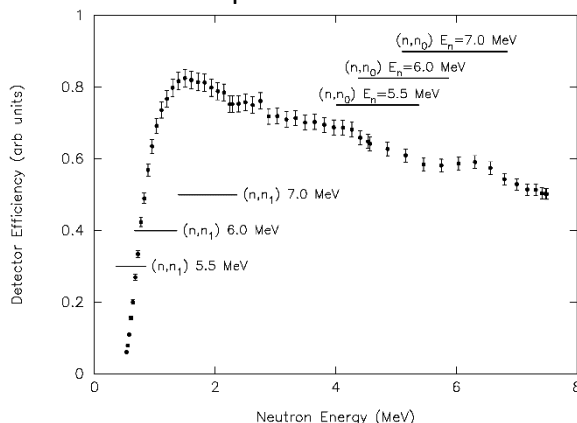
It's important to do the geometrical, attenuation, and multiple scattering corrections well.





# Measuring MAIN Detector Efficiency

example from former 12C

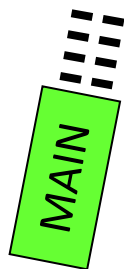


The reaction channels sample different parts of the efficiency curve at different energies.

$$eff(E_n) = \frac{Yield}{FM \bullet \frac{d\sigma}{d\Omega_{Tpn}}}$$

**MAIN detector efficiencies must be measured because of**

- discriminator threshold effects
- individ scintillator assembly behaviors
- sub-LLD pileup



Measure  
angular / energy dependence of the  
 $T(p,n)$  or  $D(d,n)$  source reactions.

# Generic UKAL Uncertainties

Issue	
Counting Statistics $n_0, n_1$	<1%
Ability to Extract Yield from Peaks in Spectra (elas)	~2% usually
Ability to Extract Yield from Peaks in Spectra (inel)	...hum
Monitoring Neutron Production	<1%
Sample Mass	<<1%
H(n,n) reference XS	<0.5%
Detector Efficiency	
$3\text{H}(p,n) \quad d\sigma/d\Omega$	~3%

Issue	
Atten & Mult Scat	
$n\sigma$	0.3 %
sample radius	0.3 %
sample-Tcell dist	0.2 %
method	<5%

making new MCNP tests with  
improved gas cell description to  
make this more definite

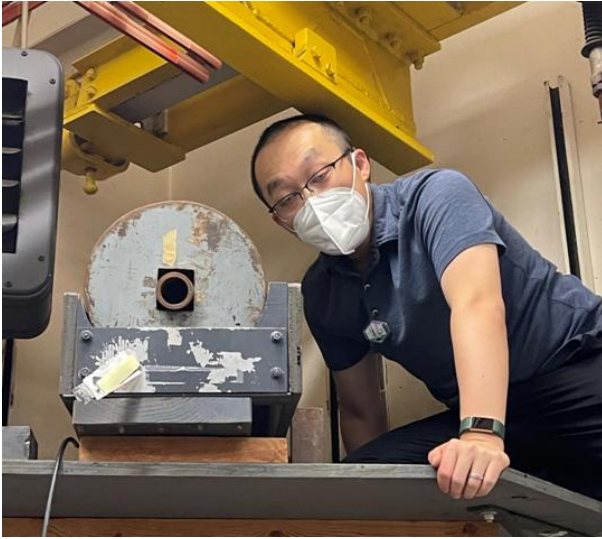
depends on the level scheme of  
the target nucleus – overlapping peaks?

- Overall during  $^{23}\text{Na}$  runs: elastics ~8-10%  
inelastics ~13-18%

Overall during C runs: elastics ~6%  
inelastics ~10%

- Overall during  $^{54-56}\text{Fe}$  runs: elastics ~7-10%  
inelastics ~10-14%

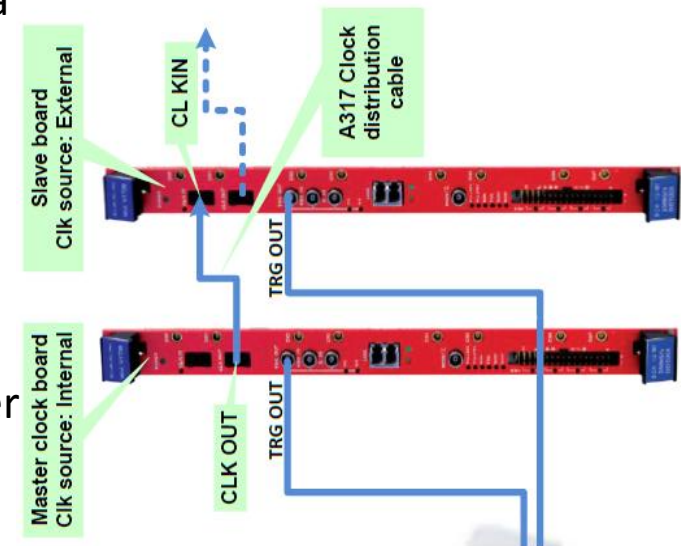
We cannot make sub% determinations of cross section values, however our angular distributions guide selections of model parameters.



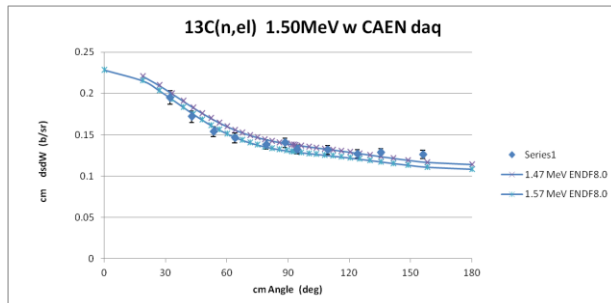
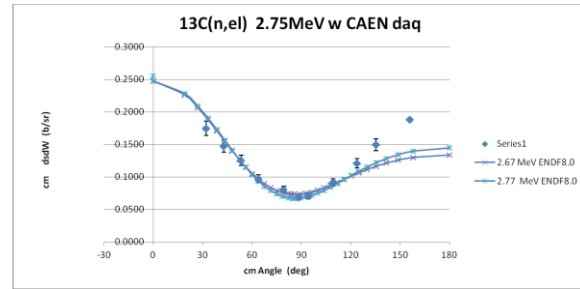
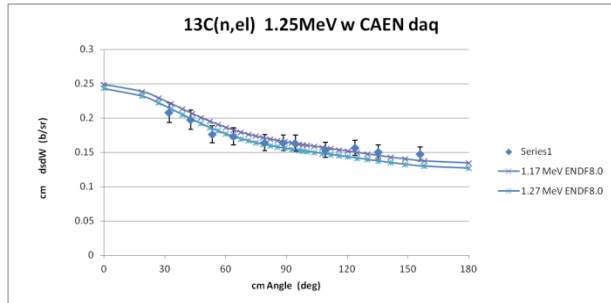
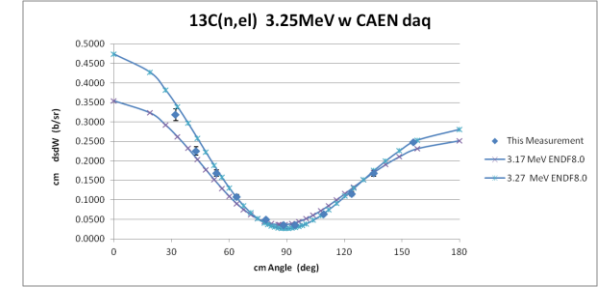
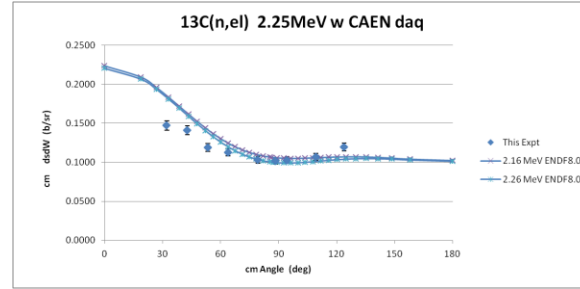
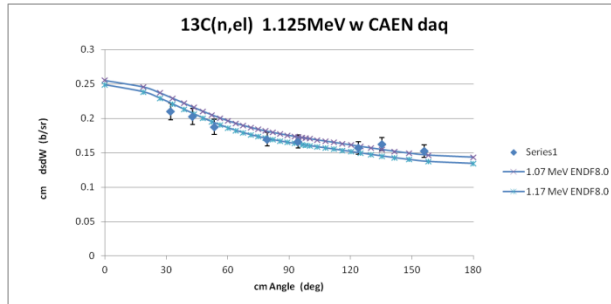
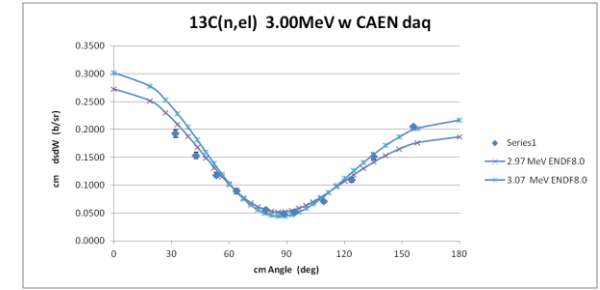
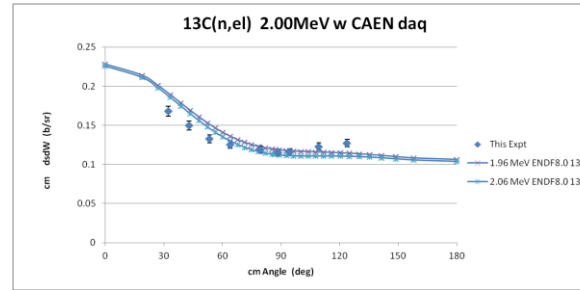
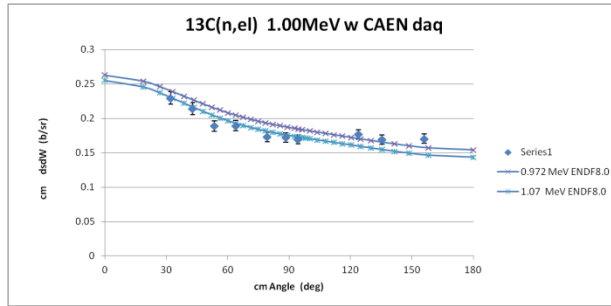
V1730 500 MS/s  
scintillators nTOF  
MAIN & FM  
beam pulse

V1782 100 MS/s  
HPGe  
Long Counter

- + can record time-dependent  $\gamma$ -ray spectra
- + observe time dependence of background
- + trapezoidal filter can be fine tuned for each detector, kinda
- + can replay data & change your mind about settings
- + n detector efficiencies less of a hassle
- + can actually digitize the 1.875 MHz beam pulse
- can't do detailed live-monitoring of data coming in
- time consuming development, testing, refining
- modules may not perform as expected or play well together
- $\gamma$  peak shapes fill hard disks & buffers fast
- new ways to do things wrong
- team members not completely satisfied with nTOF resolution yet



# $E_n > 1.0$ MeV n+13C elastic scattering angular distributions (preliminary)



Angular distributions seem bland.

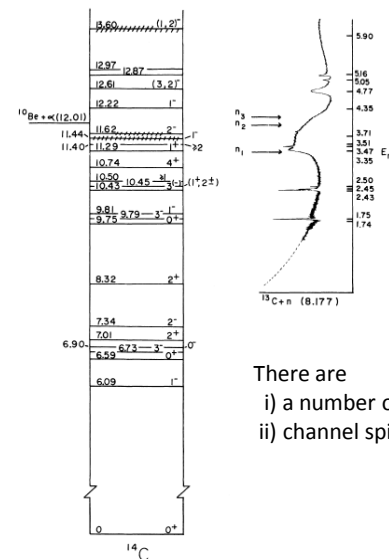
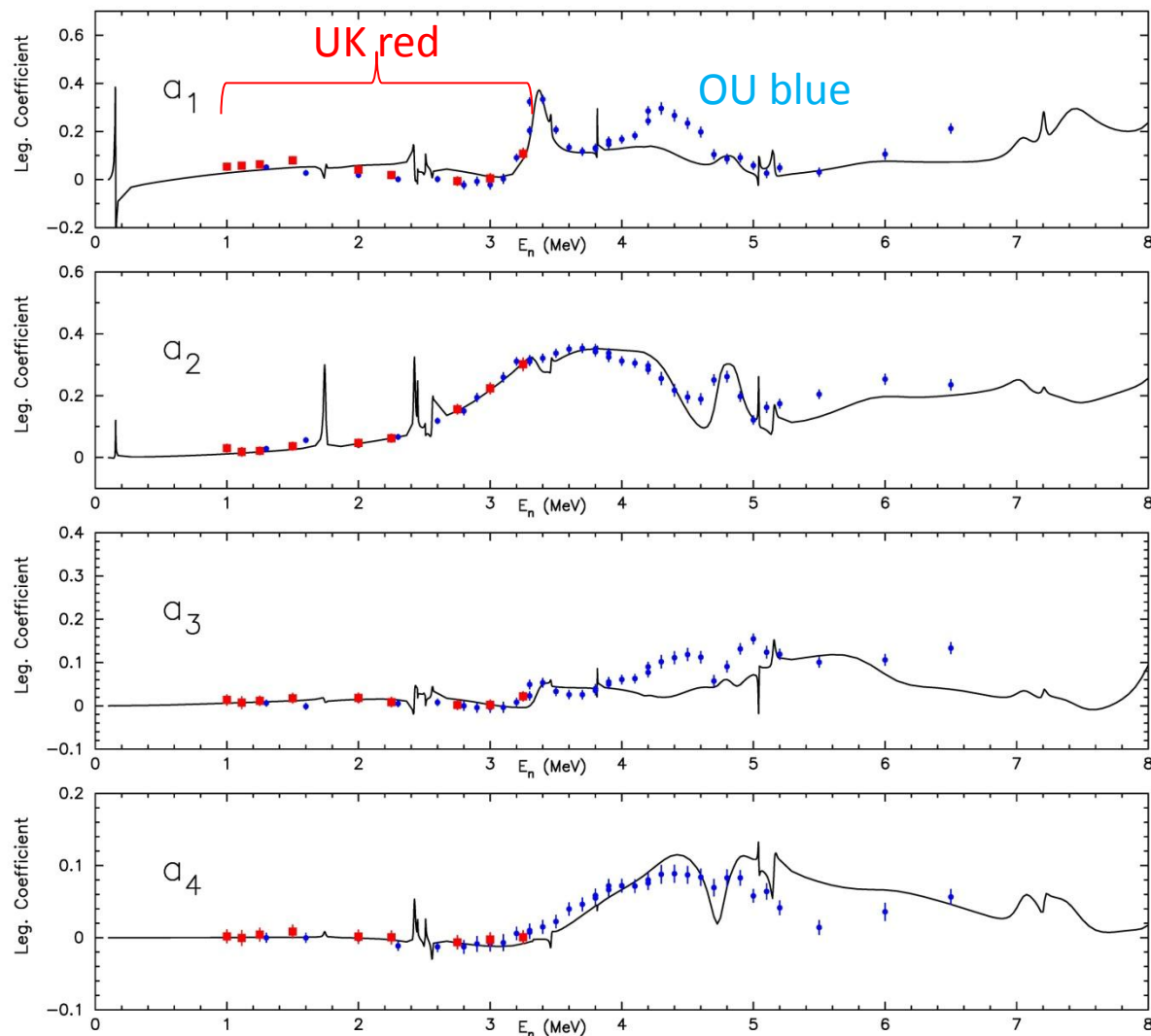
Detail is apparent if one examines Legendre expansion coefficients.

$$W(\theta) = A_0 \sum_L a_L P_L(\cos \theta) \quad ; a_0 = 1$$

$$a_L^{ENDF} = \frac{a_L^{exp}}{2L + 1}$$

# Comparison of the ENDF8.0 Legendre Coefficients compared to the coefficients from the LANE1981 experimental measurements (preliminary).

Detail is apparent if one examines Legendre expansion coefficients.  
Legendre coeffs contain info on reaction mechanism amplitudes.



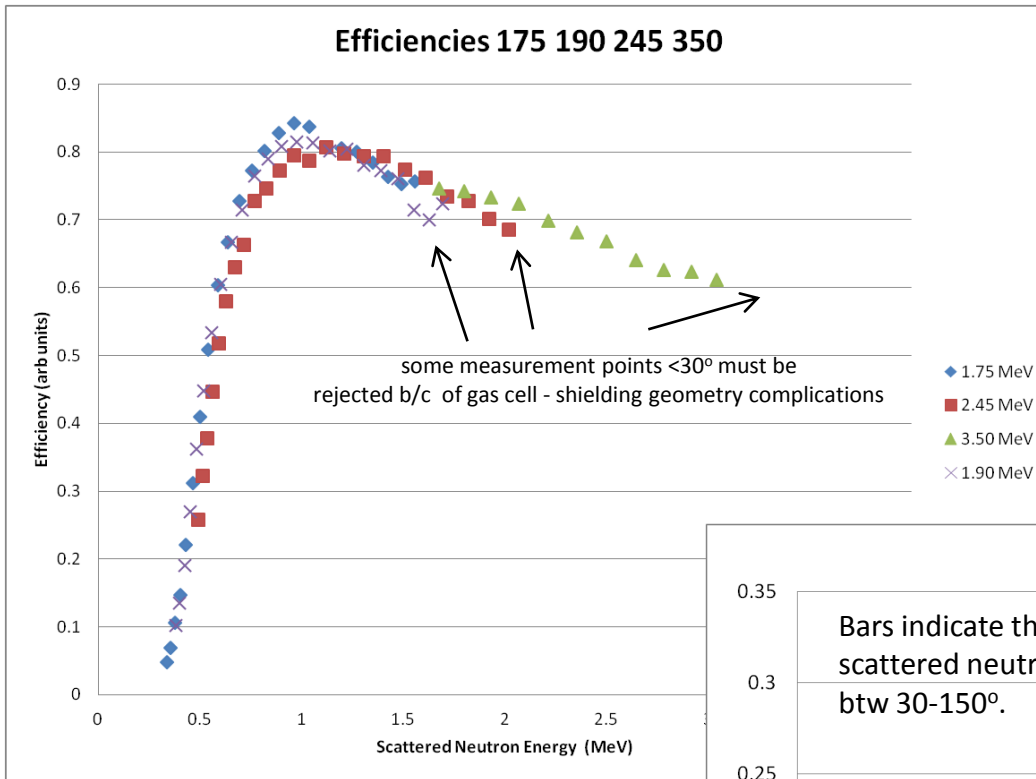
There are  
i) a number of CN levels  
ii) channel spin mixing.

Discrepancies btw current ENDF  
& 1981 experimental  
measurements.

So far, we are  
extremely consistent with  
OhioU values !

We need to  
go lower in energy  
&  
check out the 4-5 MeV region

## Above $E_n = 1$ MeV measurements go well

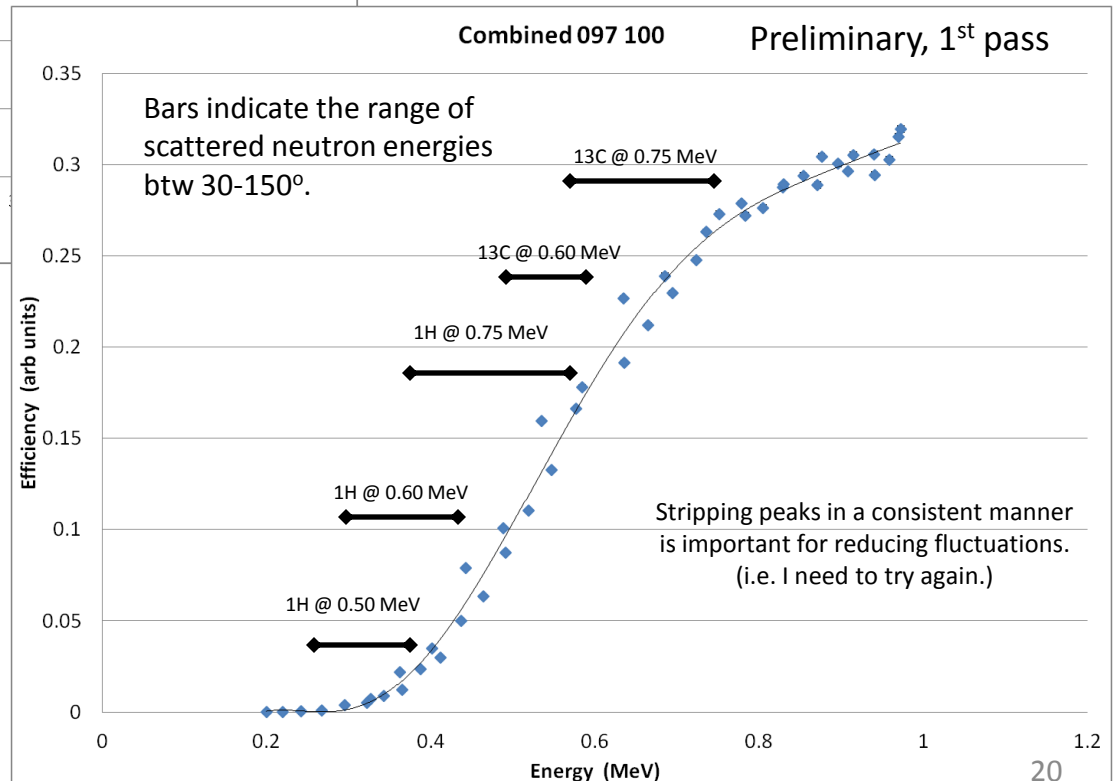


MAIN detector efficiencies must be measured b/c

- descrim threshold effects
- individ scintillator behavior
- sub-LLD pileup

Below 1 MeV, challenges develop which require more work.

Our usual  $H(n,n)$  xs normalization reaction, not usable  $E_n < 0.6$  MeV b/c scattered neutron energies become too low for our EJ301 detectors.





SUMMARY:

- Finishing the  $^{13}\text{C}$  data request.
- The team is working on many projects
- Re-canned  $^7\text{Li}$  and measure again.
- $^{19}\text{F}$  – time dependent (n,n' $\gamma$ )



NSF 1913028 / 2209178



# Dirty Hands

## Laboratory Skills

### Operation, Maintenance, Repair, Design



**Dirty Hands** brought to you by



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**ENERGY**

