



# 17th International Symposium on Capture Gamma-Ray Spectroscopy and Related Topics - CGS17



## Towards a microscopic understanding of shape isomerism in medium-mass nuclei

Silvia Leoni – University of Milano and INFN

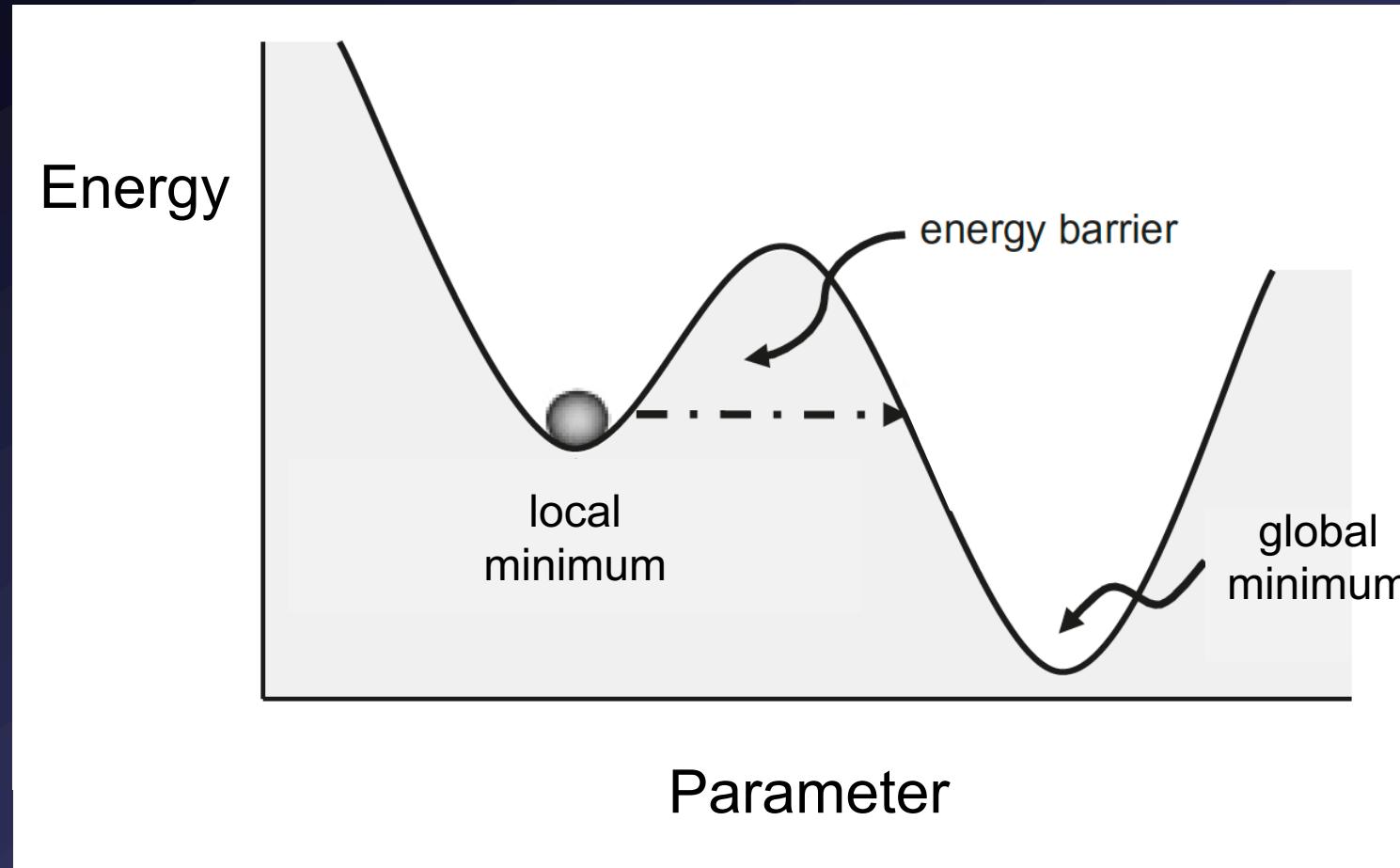
In collaboration with:

- **B. Fornal** et al., Institute of Nuclear Physics, Krakow, Poland
- **N. Mărginean** et al., IFIN HH, Bucharest, Romania
- **R.V.F. Janssens** et al., University of North Carolina, USA
- **C. Michelagnoli** et al., ILL, Grenoble, France
- **M. Sferrazza** et al., Universite libre de Bruxelles, Belgium
- **J. Wilson** et al., IJCLAB Orsay, France
- **T. Otsuka, Y. Tsunoda** et al., University of Tokyo, Japan



UNIVERSITÀ  
DEGLI STUDI  
DI MILANO

# The Potential Energy Surface (PES) of a system a fundamental concept in physics on all scales

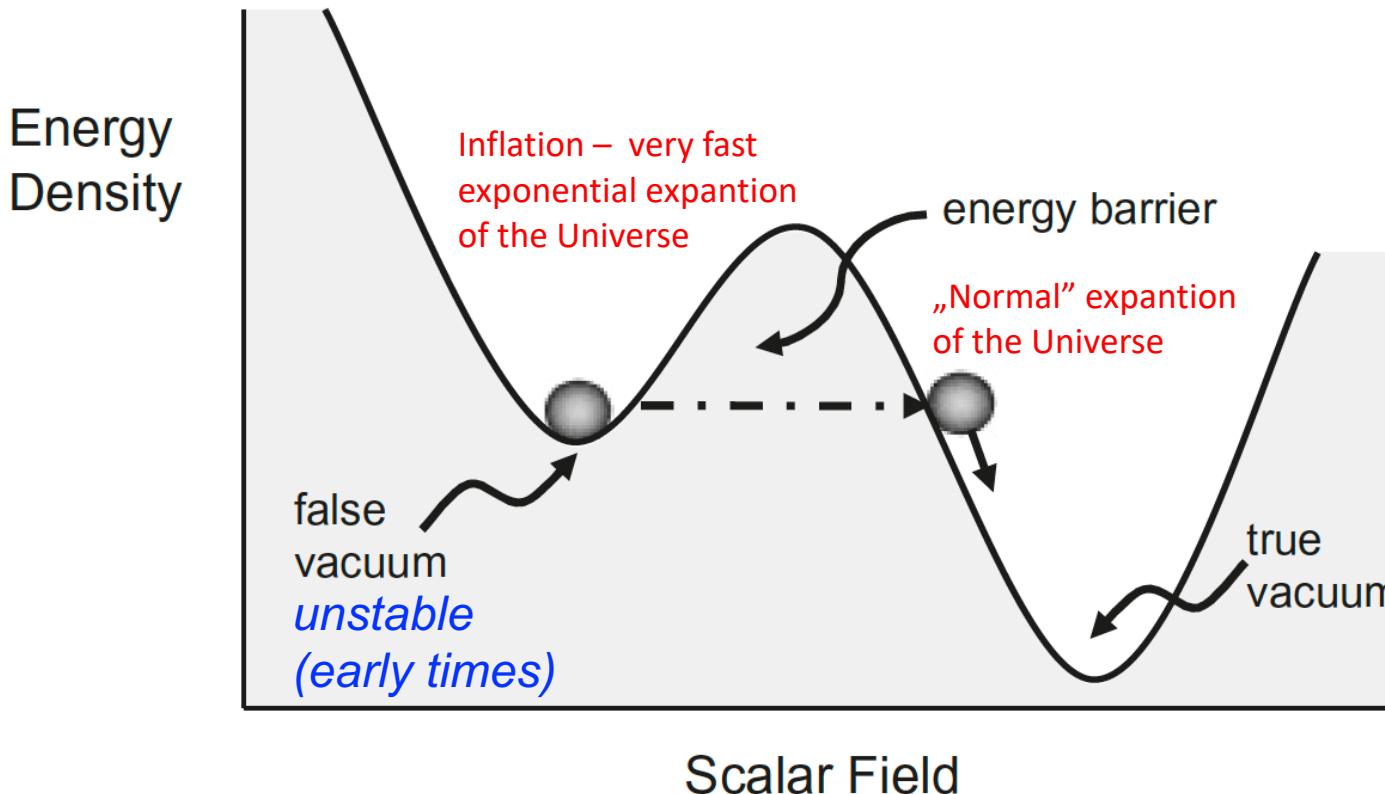


*physical systems  
tend to minimize  
their potential  
energy*

in Quantum Mechanics  
a system trapped in a **local minimum** can decay into the **global minimum**,  
specifically, into the ground state of the system

# Potential Energy Surface (PES) in COSMOLOGY

Alan Guth idea on Cosmic inflation – «Expansion of the Universe»

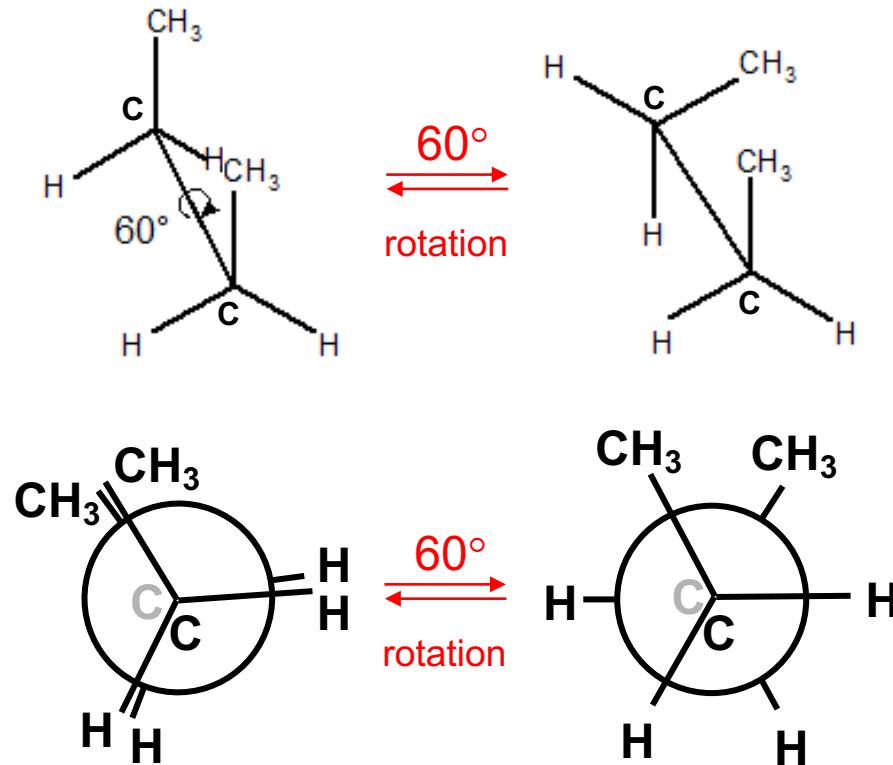


Toy model for Universe expansion

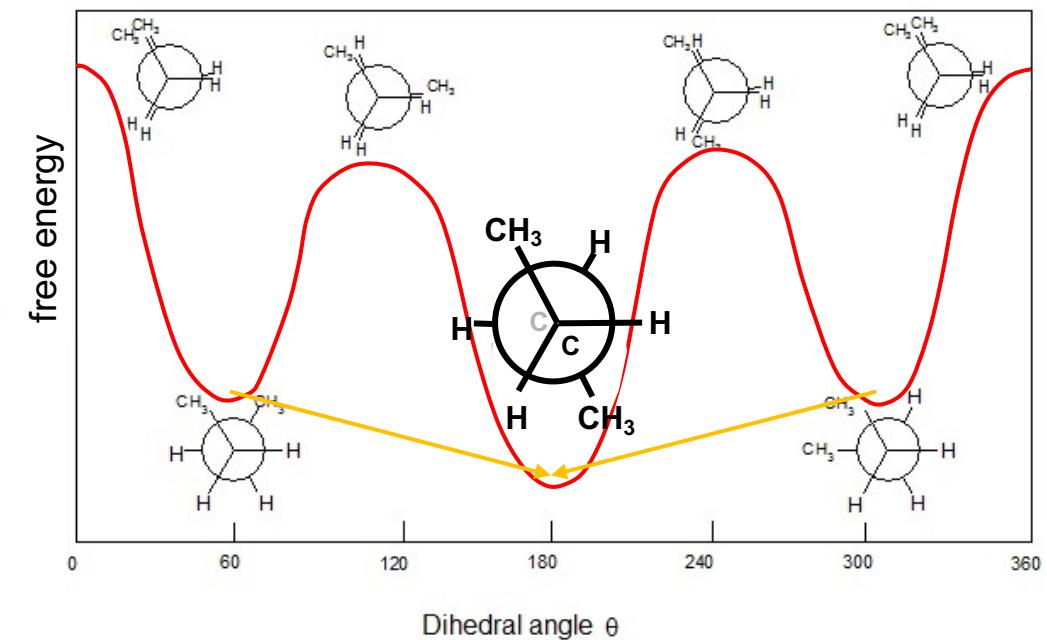
Strong repulsive gravity of the false vacuum causes a period of very fast, accelerated expansion. The inflation period ends when the system decays into the true vacuum

# Potential Energy Surface (PES) of MOLECULES

## Butane molecule $C_4H_{10}$ Conformational isomers



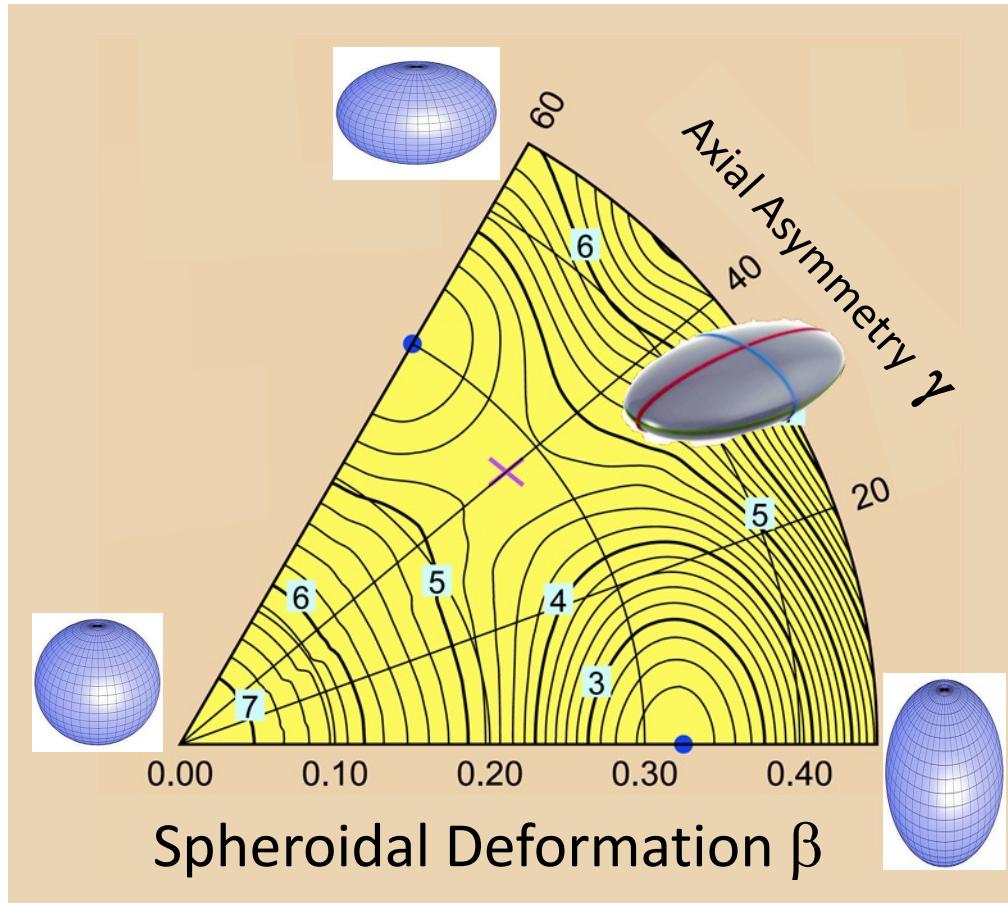
Rotation about single bond of butane



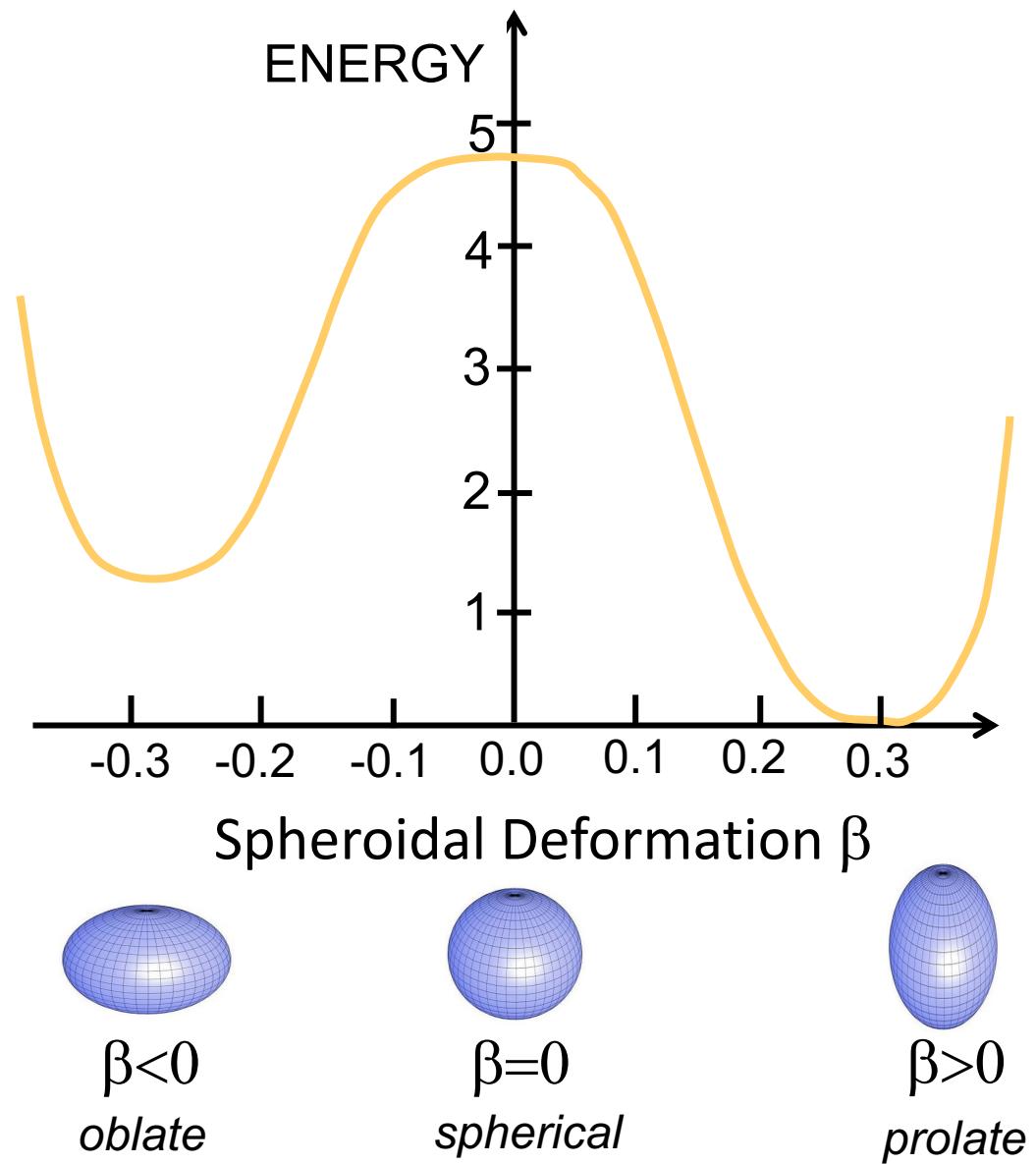
Free energy diagram of butane  
as a function of dihedral angle

# Potential Energy Surface (PES) of a NUCLEUS

two-dimensional contour

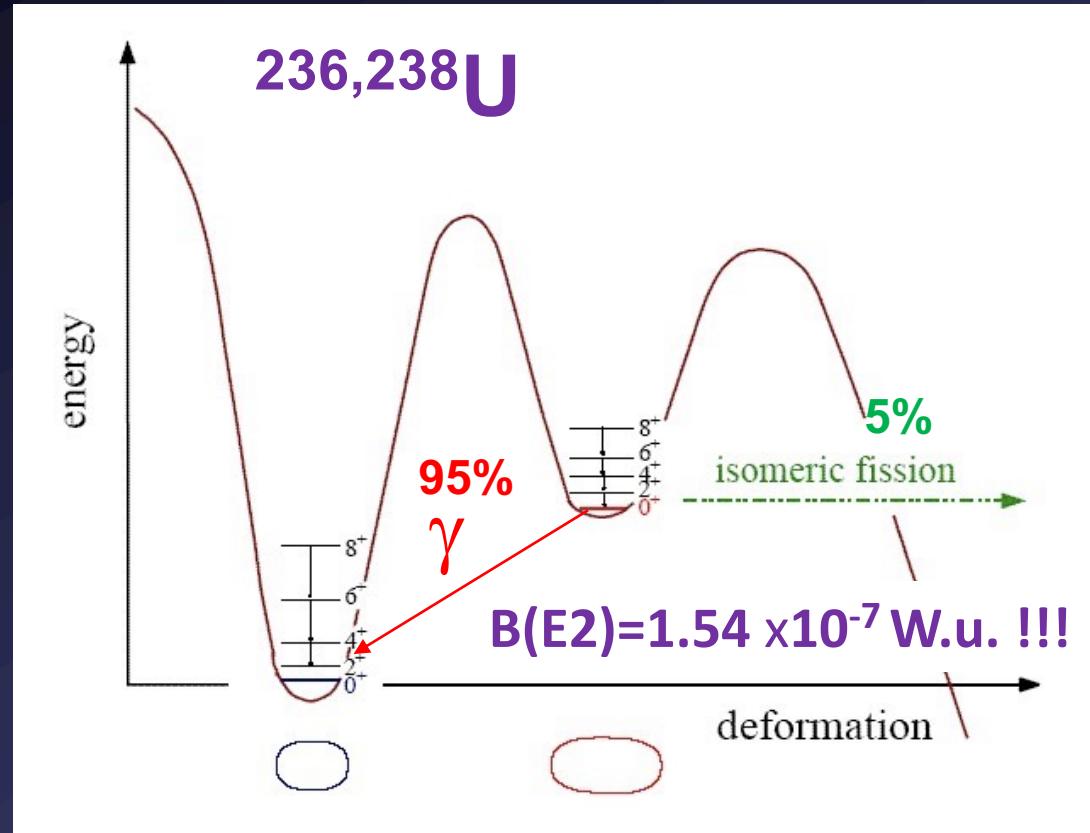


one-dimensional representation



# SHAPE ISOMERS - very peculiar metastable states

- HIGH Potential BARRIER
- Nucleus trapped In the minimum
- very retarded photon decay (***10<sup>7</sup> hindrance***)



**Structures living in  
“separate worlds”**

**MAIN FINGER PRINT:  
hindrance  
of deexciting transitions**

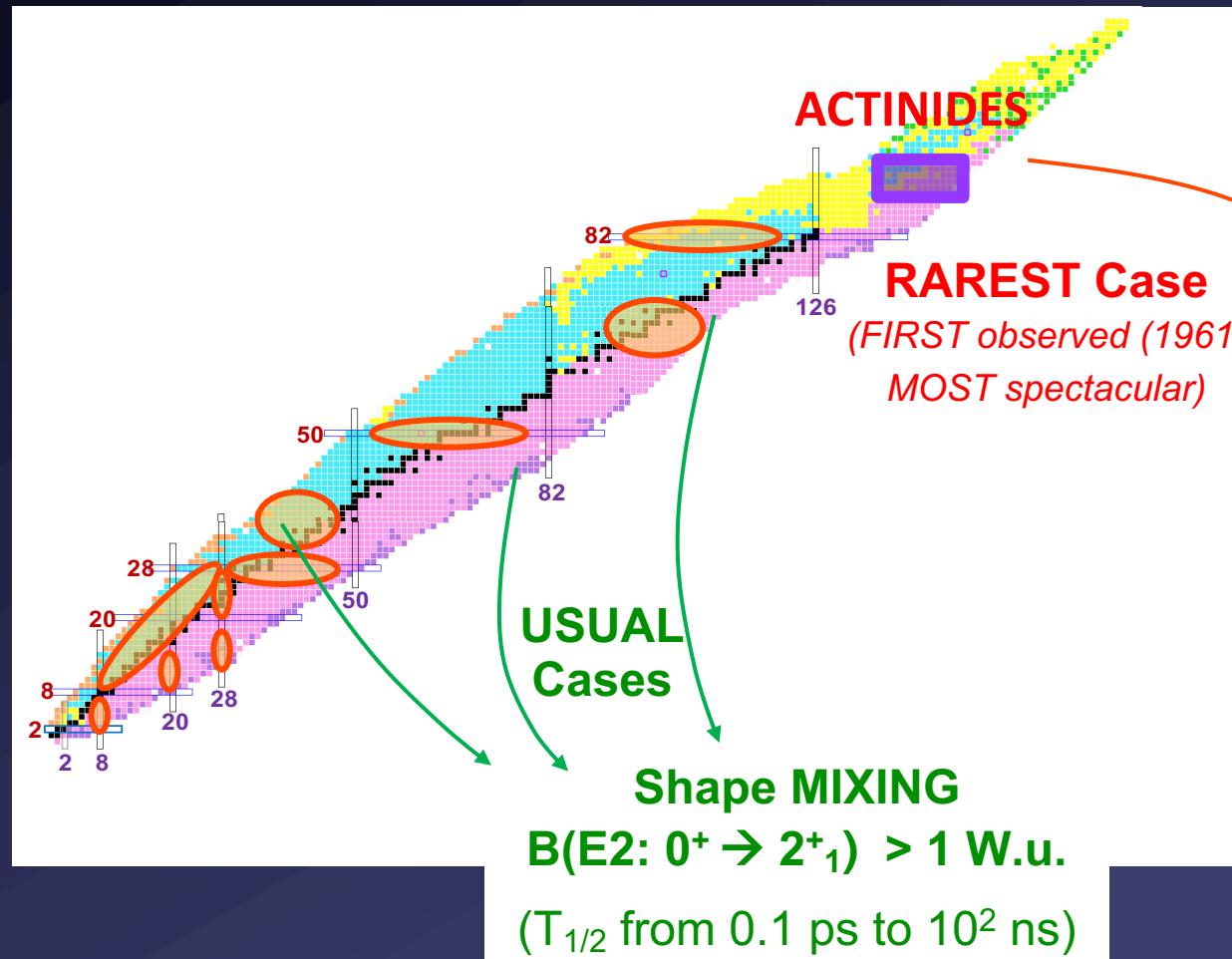
**Can OTHER (lighter) nuclei exhibit this feature ?**

# Shape coexistence in atomic nuclei

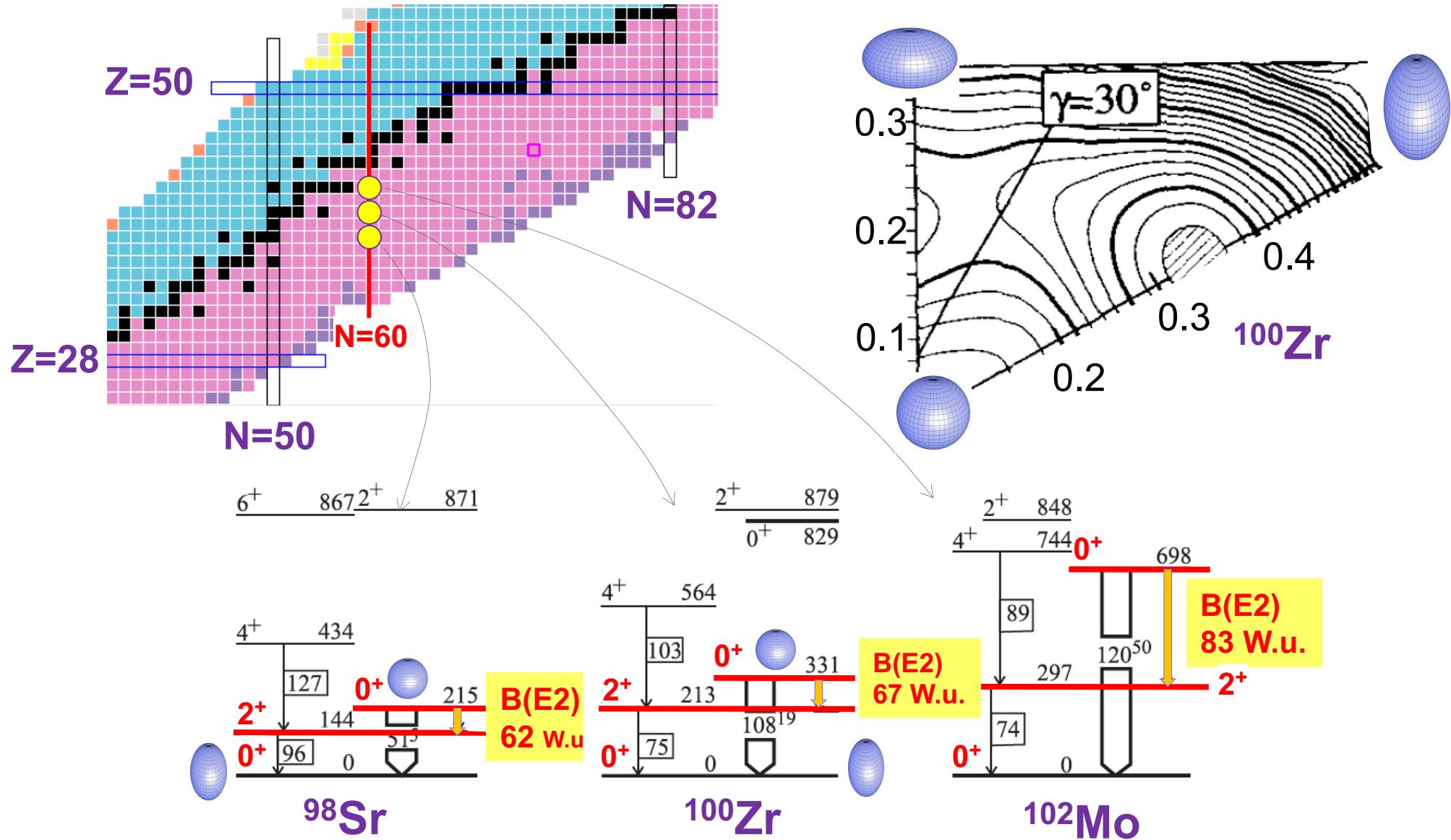
Close to  
spin 0

*After 50 years of  
investigation:*

*"An ubiquitous  
phenomenon  
across the nuclear  
chart"*



In general, NO HINDRANCE observed  
for decay between different shapes, even if isomeric  
i.e.,  $B(E2) \gtrsim 1 \text{ W.u.}$

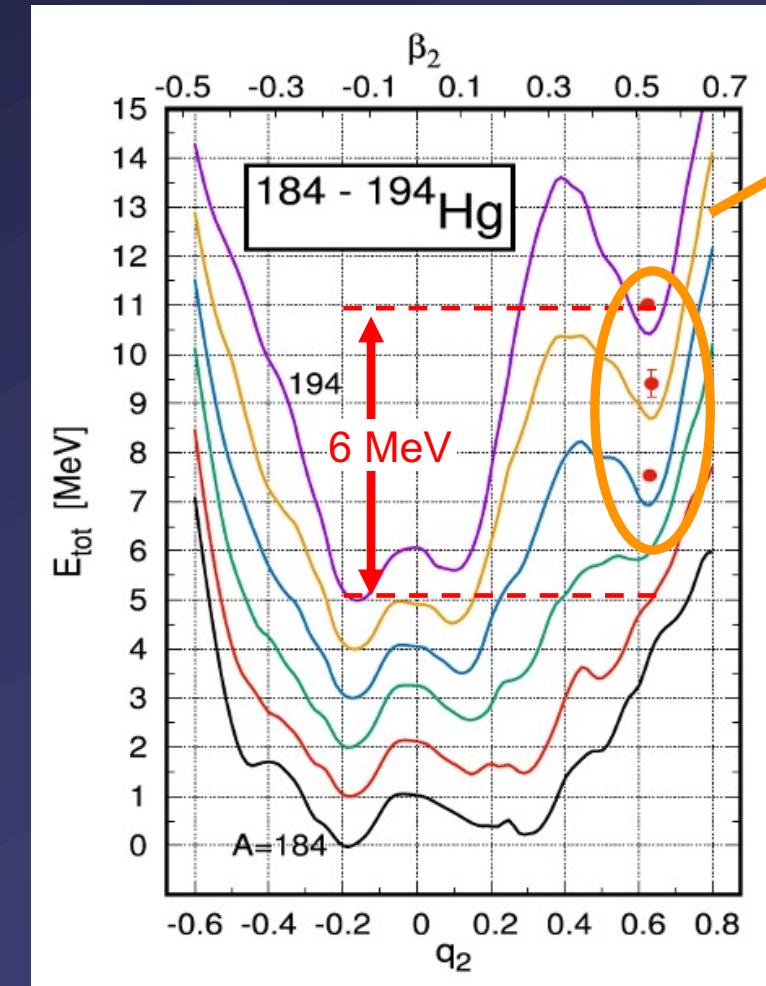
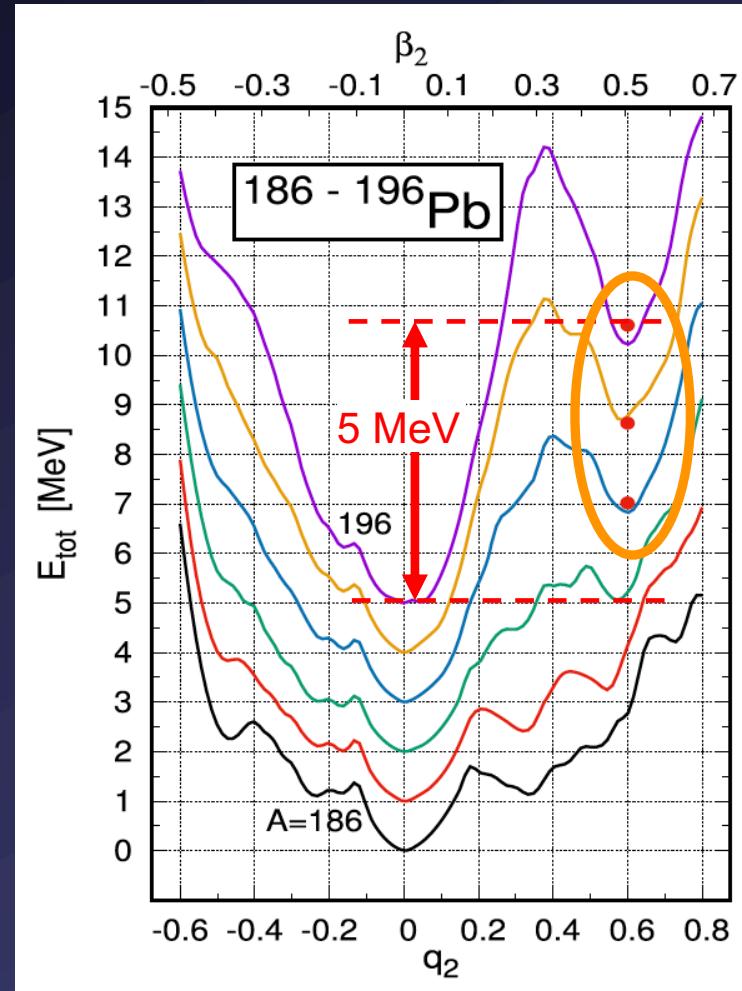


**No retardation in  $\gamma$  decay is observed !!!**  
 Potential barrier NOT sizable enough to prevent fast shape changes

# Where to search for other strongly hindered $\gamma$ decays from $0^+$ states located in deep secondary minima ?

Several predictions for heavy systems

- **very difficult to populate**  
(high density of states)
- **No specific tagging**  
(delayed  $\gamma$  rays on huge background, no fission tag)



# Searching for SHAPE ISOMERS at Spin 0 in other regions

cases where wave functions are well localized  
in different PES minima  
separated by a sizable barrier

$$B(E2) \ll 1 \text{ W.u., HF} > 10$$

# Predictions for SHAPE ISOMERISM at I = 0

## (Microscopic Hartree-Fock plus BCS calculations)

Nuclear Physics A500 (1989) 308-322  
North-Holland, Amsterdam **1989**

### SUPERDEFORMATION AND SHAPE ISOMERISM AT ZERO SPIN\*

P. BONCHE<sup>1</sup>, S.J. KRIEGER, P. QUENTIN<sup>2</sup> and M.S. WEISS

Department of Physics, Lawrence Livermore National Laboratory, Livermore, CA 94550, USA

J. MEYER, M. MEYER and N. REDON

Institut de Physique Nucléaire (et IN2P3), Université Lyon 1, F-69622 Villeurbanne Cedex, France

H. FLOCARD

Division de Physique Théorique<sup>3</sup>, Institut de Physique Nucléaire, F-91406 Orsay Cedex, France

P.-H. HEENEN<sup>4</sup>

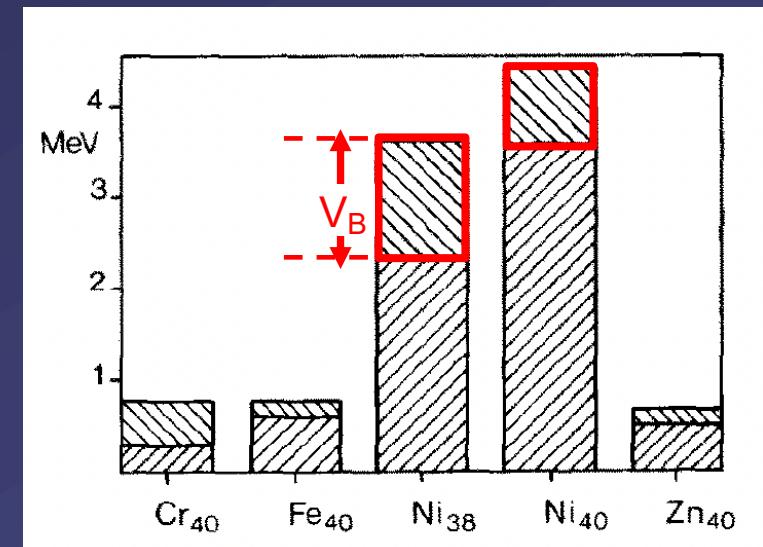
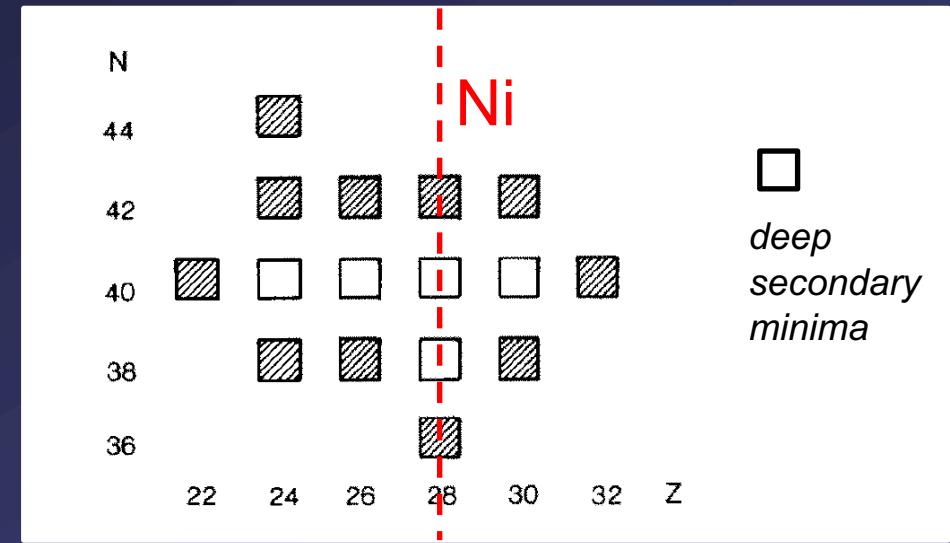
Physique Nucléaire Théorique, Université Libre de Bruxelles, CP 229, B-1050 Brussels, Belgium

Received 7 March 1989

### Candidates for the presence of deep, secondary minima:

**<sup>66</sup>Ni, <sup>68</sup>Ni, <sup>66</sup>Fe, <sup>64</sup>Cr, <sup>70</sup>Zn, <sup>190,192</sup>Pt, <sup>206,208,210</sup>Os, <sup>194,196,214</sup>Hg**

$\sim Z=28, N=40$



# Predictions based on Mean Field and EDF for existence of DEEP Secondary Minima

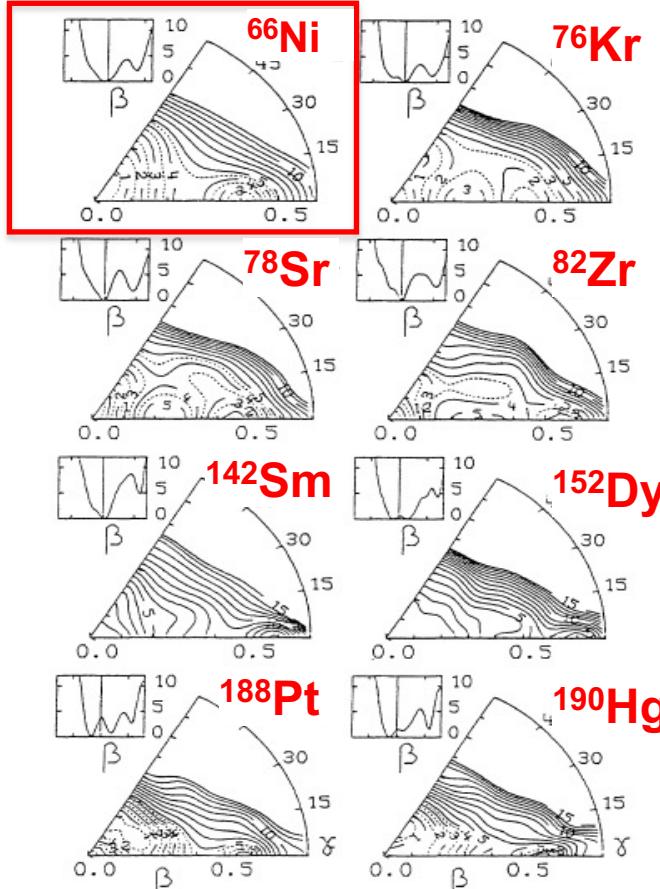
## Mean-Field based predictions

VOLUME 62, NUMBER 21 PHYSICAL REVIEW LETTERS 1989

### Hartree-Fock-Bogoliubov Predictions for Shape Isomerism in Nonfissile Even-Even Nuclei

M. Girod, J. P. Delaroche, D. Gogny, and J. F. Berger

Service de Physique et Techniques Nucléaires, Centre d'Etudes de Bruyères-le-Châtel, BP 12, 91680  
Bruyères-le-Châtel, France  
(Received 28 December 1988)



## Macro-Microscopic Model – P. Moeller et al., 2012

PRL 103, 212501 (2009)

PHYSICAL REVIEW LETTERS

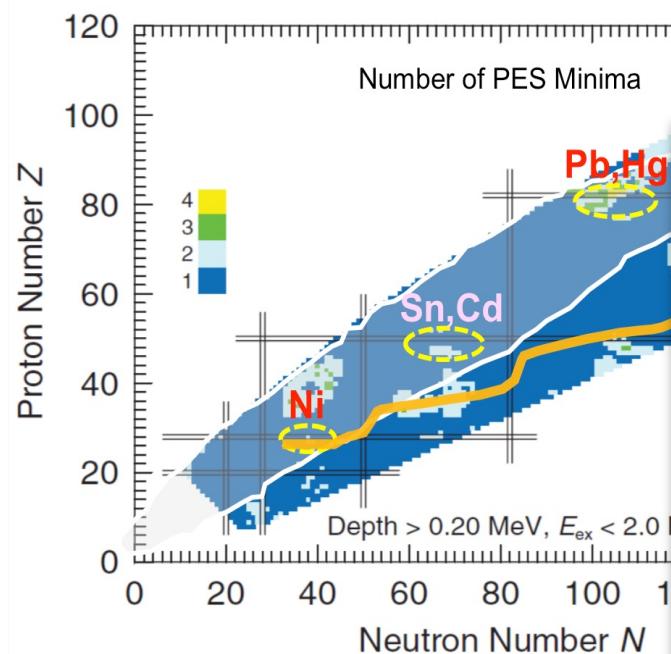
week ending  
20 NOVEMBER 2009

2009

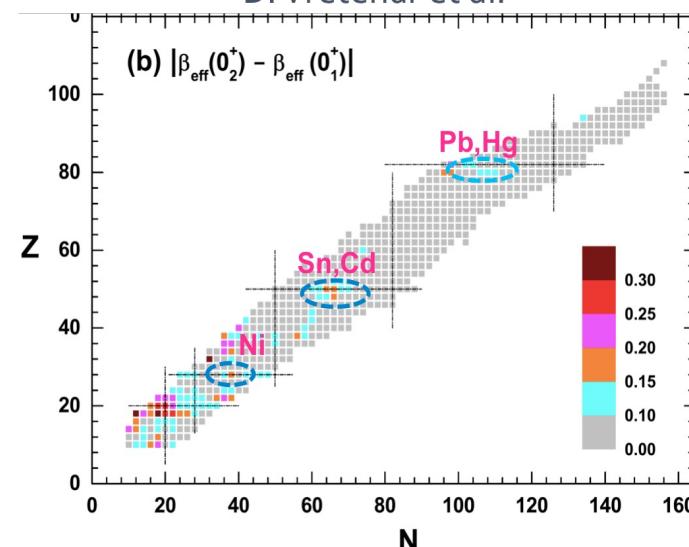
### Global Calculation of Nuclear Shape Isomers

Peter Möller,<sup>1,\*</sup> Arnold J. Sierk,<sup>1</sup> Ragnar Bengtsson,<sup>2</sup> Hiroyuki Sagawa,<sup>3</sup> and Takatoshi Ichikawa<sup>4,†</sup>

*Study of 7206 nuclei from A=31 to A=209*



Predictions of SHAPE ISOMERS in Pb-Hg and Sn-Cd by  
UNIVERSAL ENERGY DENSITY FUNCTIONALS  
and the quadrupole collective model  
D. Vretenar et al.



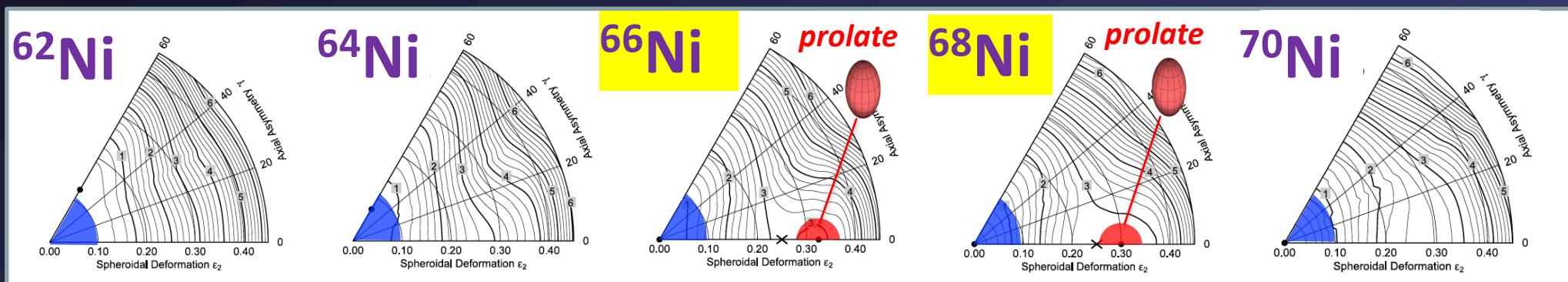
**Pb-Hg-Pt**     $A \sim 190$   
**Sn-Cd-Pd**     $A \sim 110$   
**Ni**                 $A \sim 68$

# We focus on the Ni chain

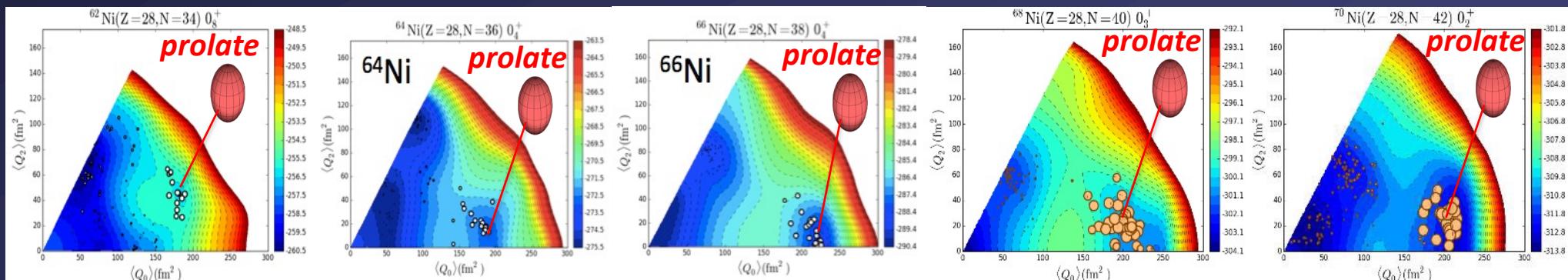


## Monte Carlo Shell Model

- Large configuration space:  
 $f_{7/2}, p_{3/2}, f_{5/2}, p_{1/2}, g_{9/2}, d_{5/2}, g_{7/2}$
- Number of configurations  $10^{20}$   
MICROSCOPIC understanding  
wave functions,  $B(E\lambda/M\lambda)$  ...



Mean Field  
Moeller et al.



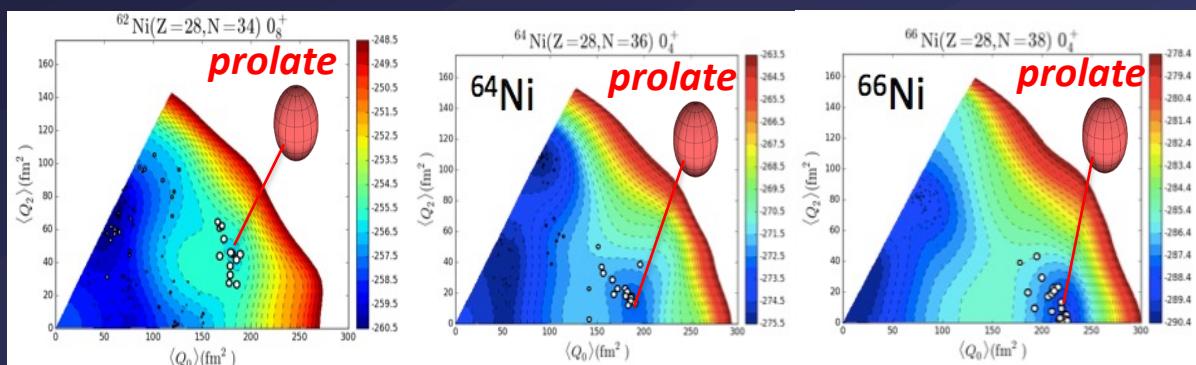
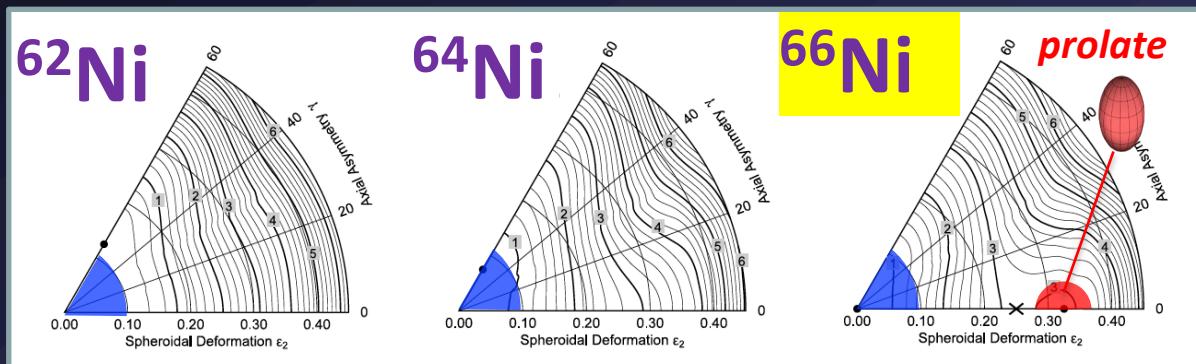
Monte Carlo  
SHELL Model  
Y. Tsunoda,  
T. Otsuka et al.

# We focus on the Ni chain



## Monte Carlo Shell Model

- Large configuration space:  
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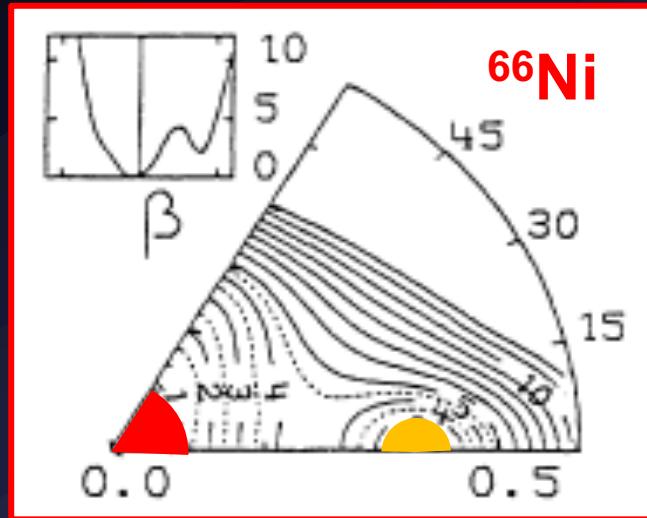
experimental  
investigation  
with STABLE beams

Mean Field  
Moeller et al.

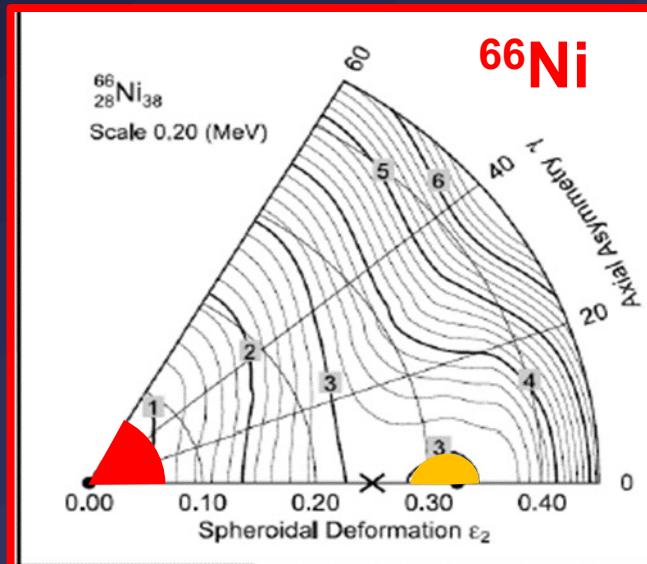
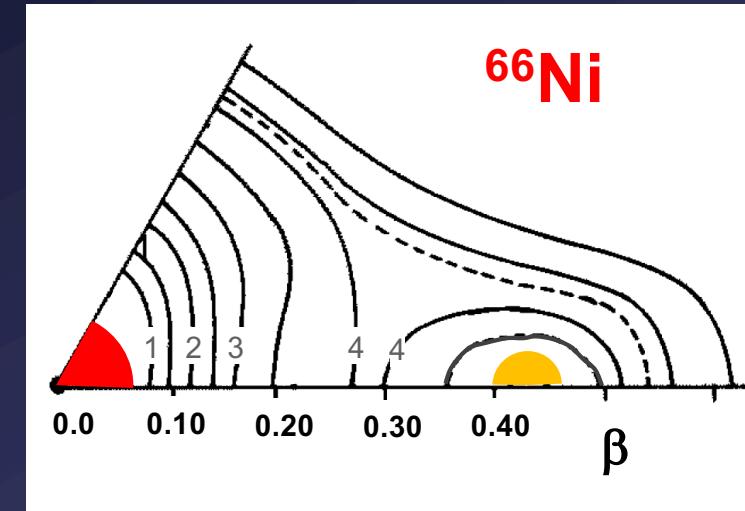
Monte Carlo  
SHELL Model  
Y. Tsunoda,  
T. Otsuka et al.

# Predictions of the FOUR models for $^{66}\text{Ni}$

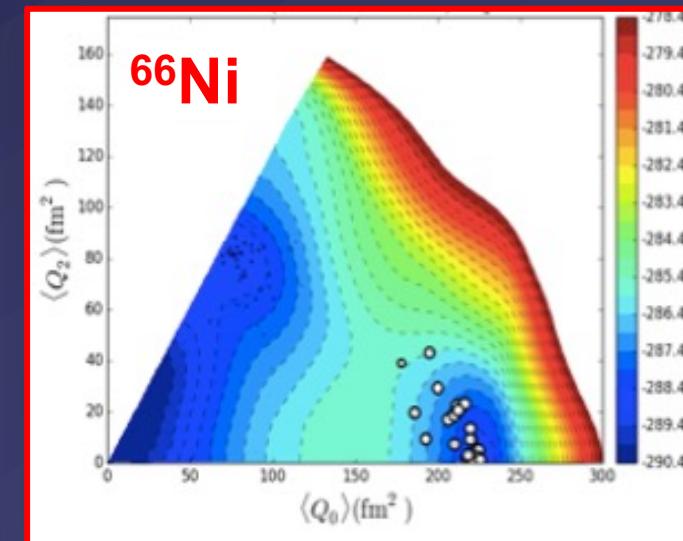
Microscopic Hartree-Fock-Bogoliubov



Microscopic Hartree-Fock plus BCS

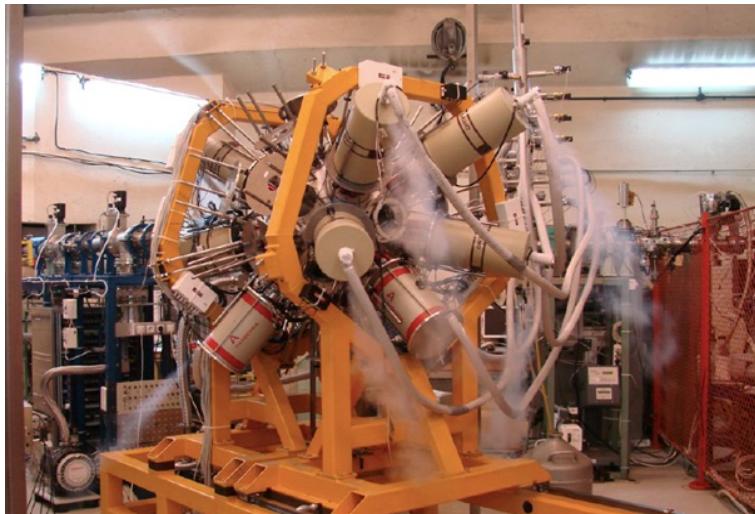


Macro-Microscopic Model



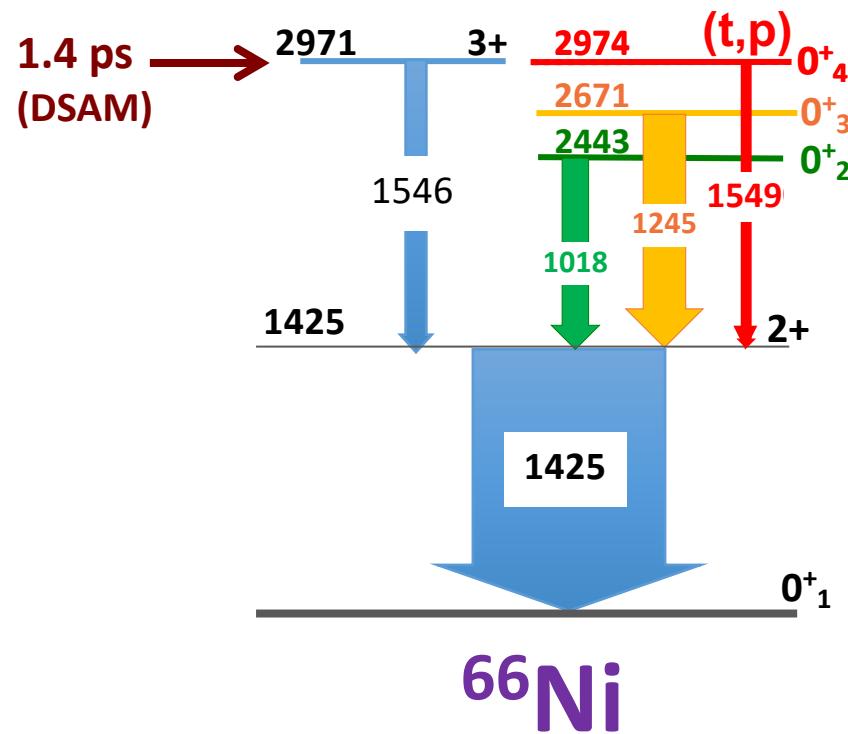
Monte Carlo Shell Model

2016



## ROSPHERE

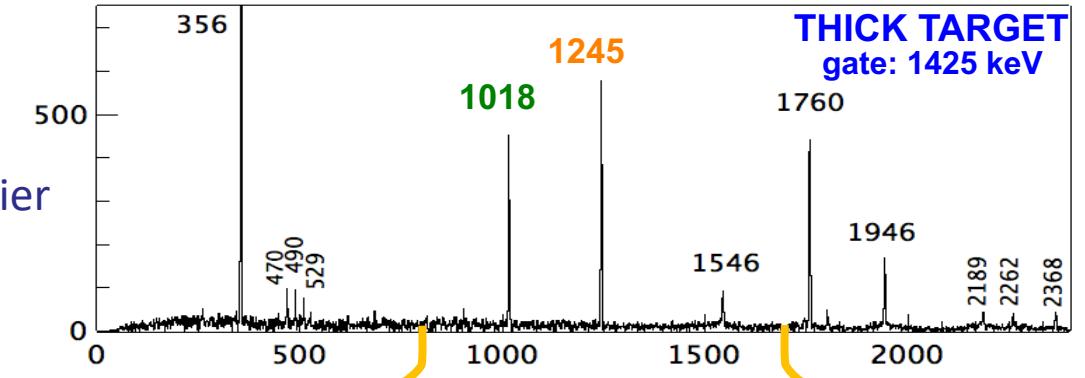
14 HPGe - 1.1% eff  
11 LaBr<sub>3</sub>(Ce) - 1.75% eff



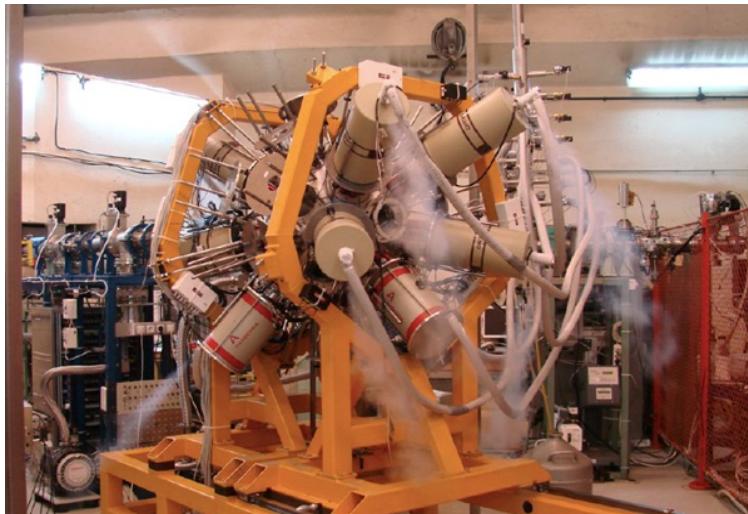
$E_{\text{beam}} = 39 \text{ MeV}$

2n transfer below Coulomb Barrier  
at IFIN HH Bucharest

> 1.5 months, 30 pnA

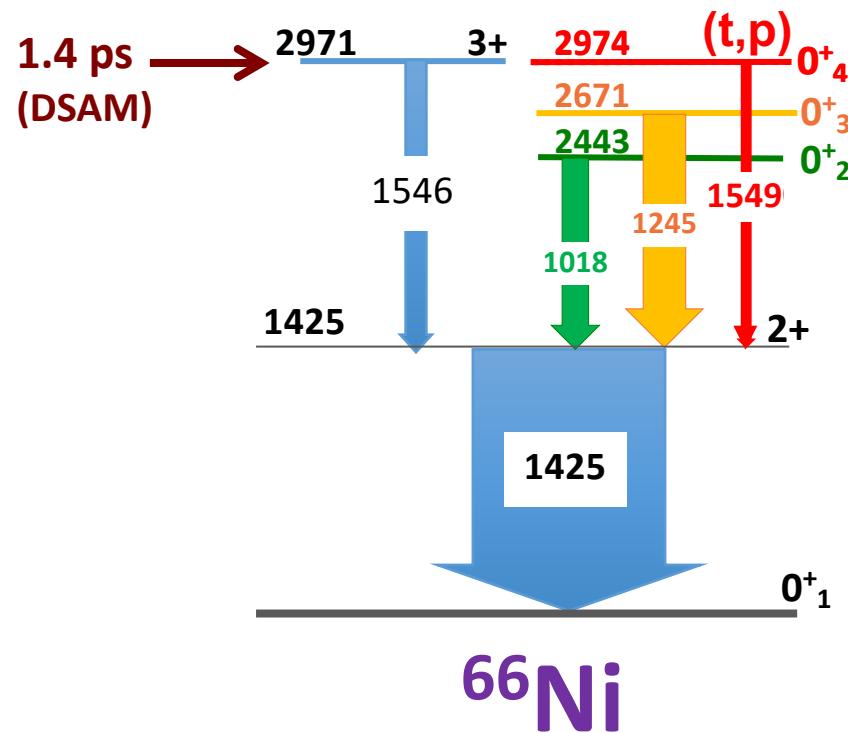


2016



## ROSPHERE

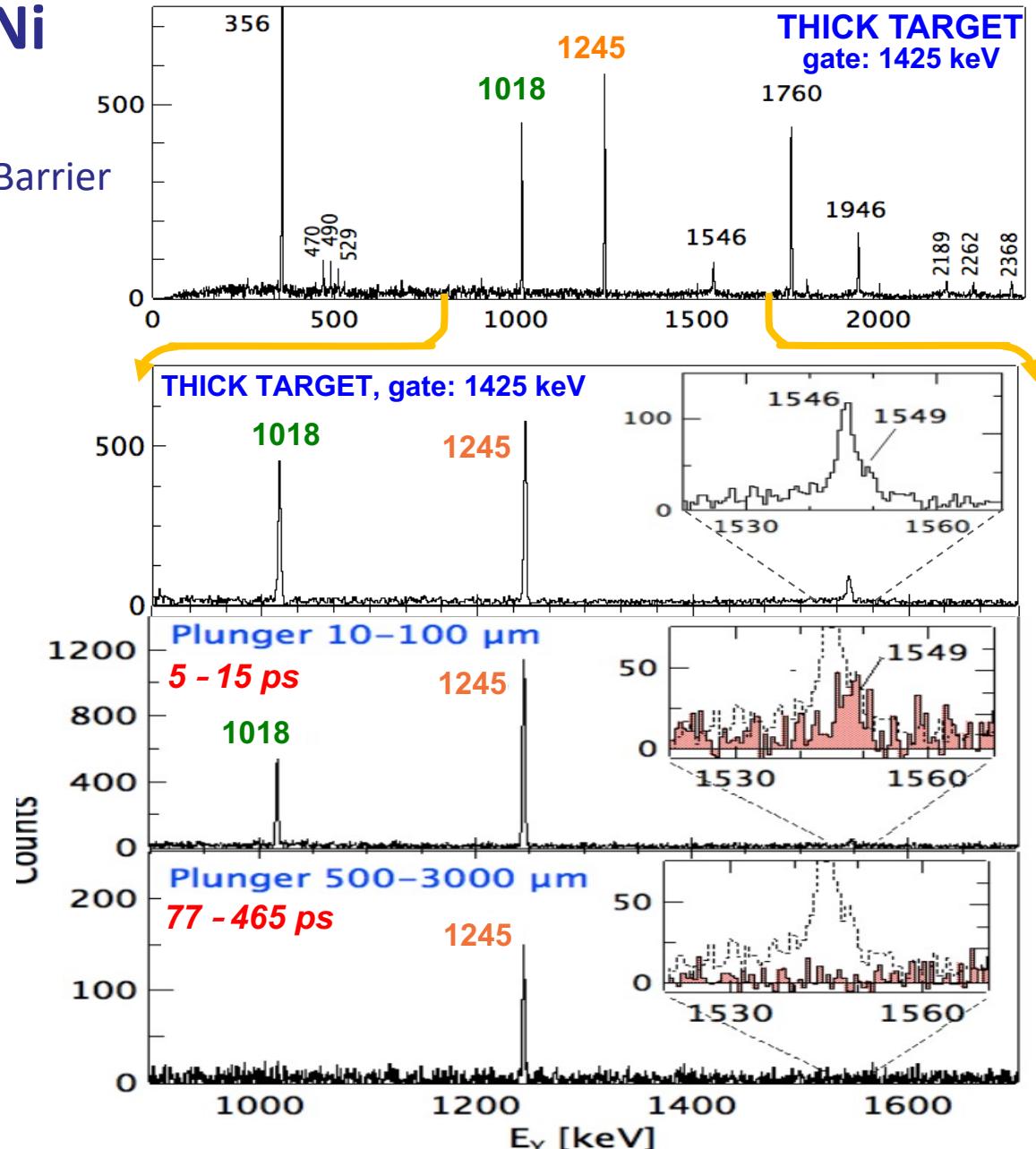
14 HPGe - 1.1% eff  
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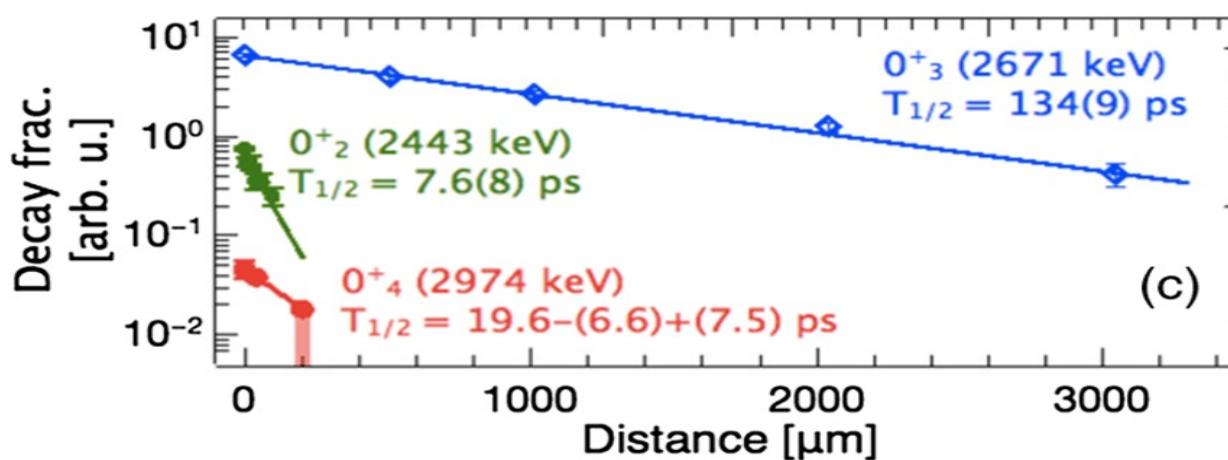


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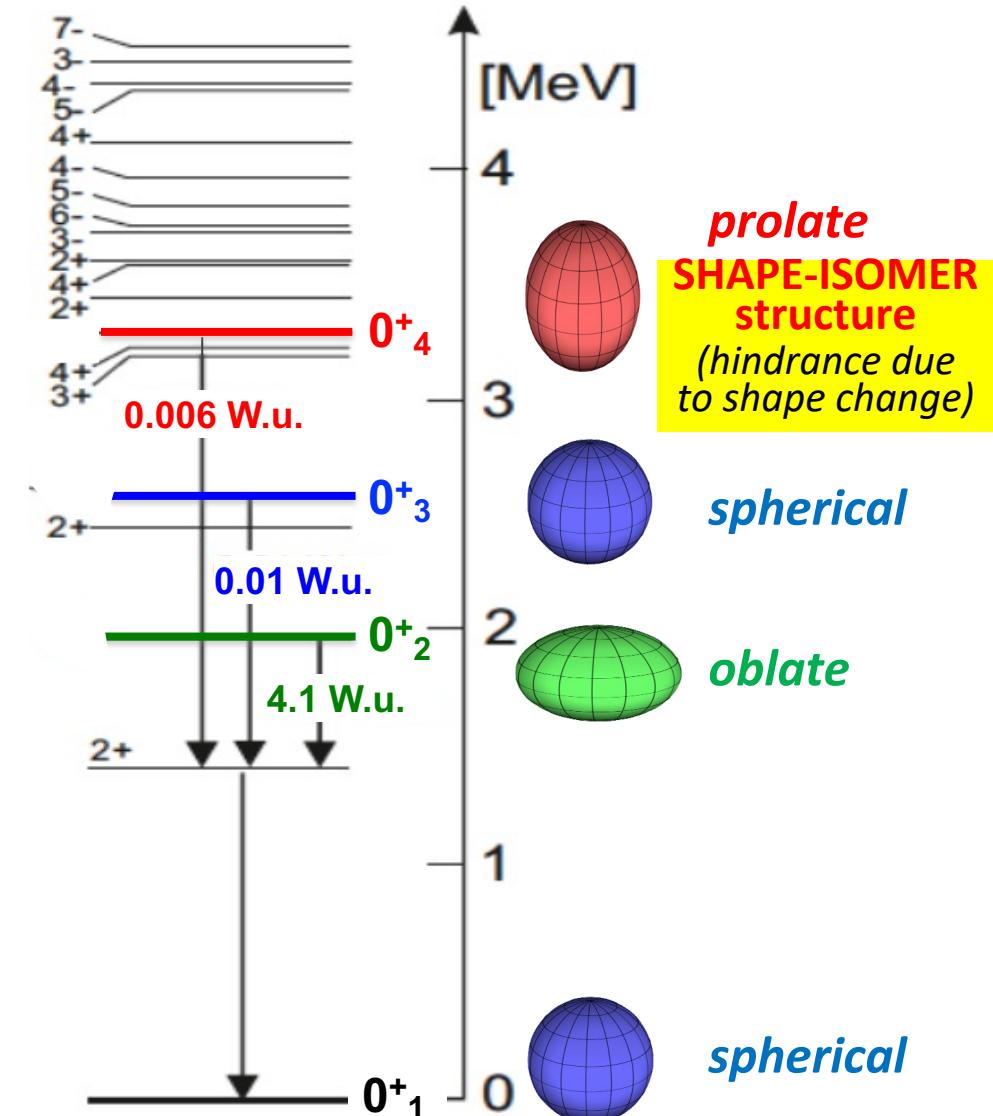
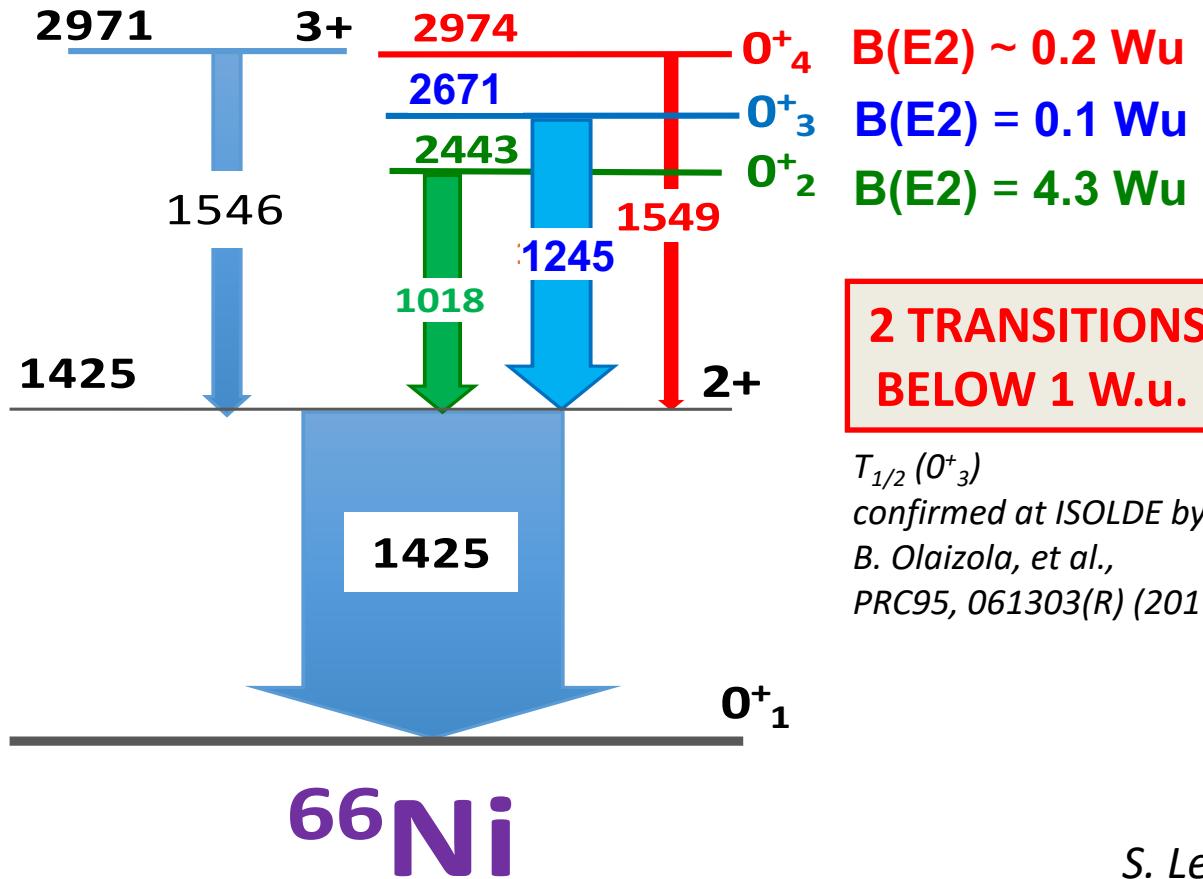
2n transfer below Coulomb Barrier  
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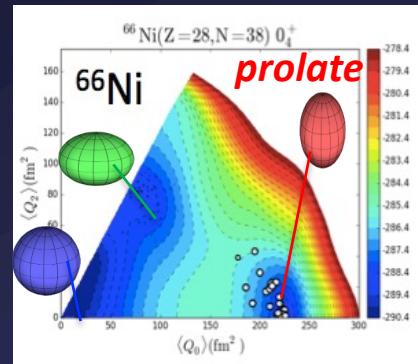


## SHAPE assignment from comparison with theory predictions (MCSM)



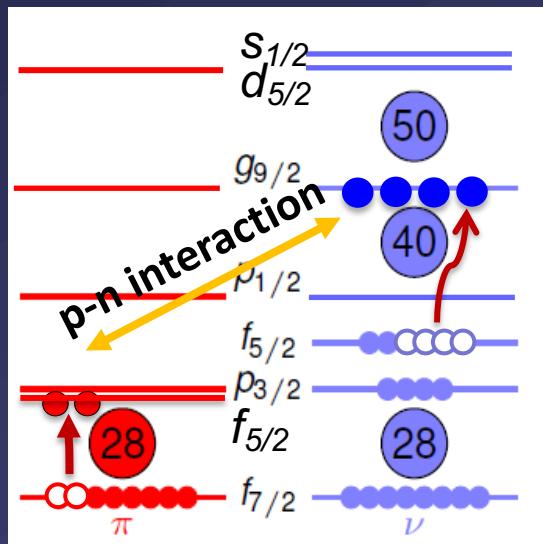
# PROLATE $0^+$ state

**$^{66}\text{Ni}$**



$0^+_4$ :  
well localized wave function  
in prolate minimum

and proton  
in  $p_{3/2}$ ,  $f_{5/2}$   
orbitals

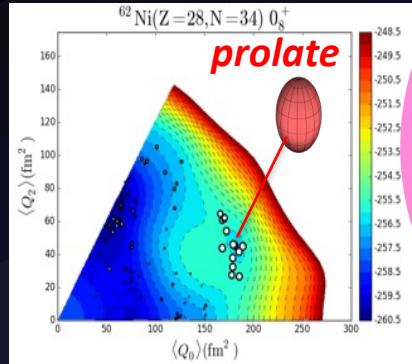


Sizable occupation of  
neutron in  $g_{9/2}$

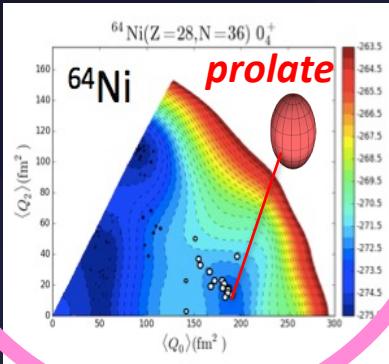
*proton-neutron interaction*  
(**monopole tensor force**) induces  
**Spontaneous Symmetry Breaking**  
*Type II SHELL Evolution* - Y. Tsunoda, T. Otsuka

# Same features of PROLATE $0^+$ states along the Ni chain:

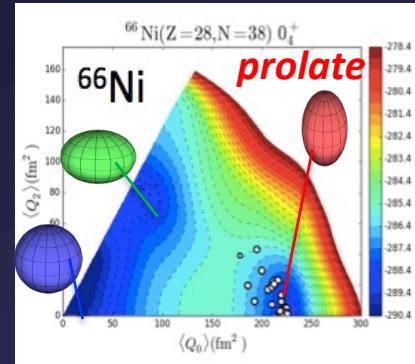
$^{62}\text{Ni}$



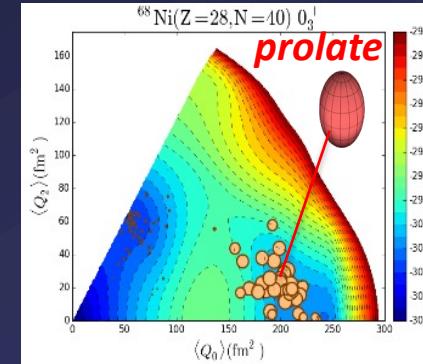
$^{64}\text{Ni}$



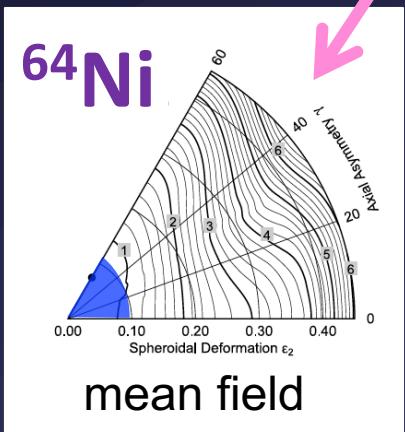
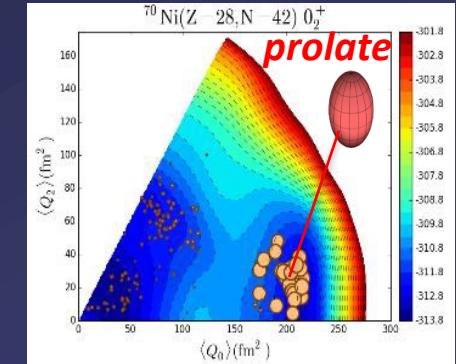
$^{66}\text{Ni}$



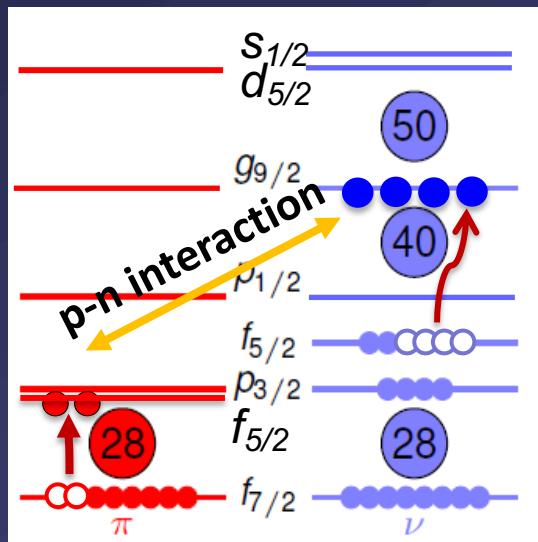
$^{68}\text{Ni}$



$^{70}\text{Ni}$



and proton in  $p_{3/2}$ ,  $f_{5/2}$  orbitals



Sizable occupation of neutron in  $g_{9/2}$

*proton-neutron interaction (**monopole tensor force**) induces Spontaneous Symmetry Breaking*  
*Type II SHELL Evolution - Y. Tsunoda, T. Otsuka*

# **$^{64}\text{Ni}$ : 4 experiments in 4 laboratories**

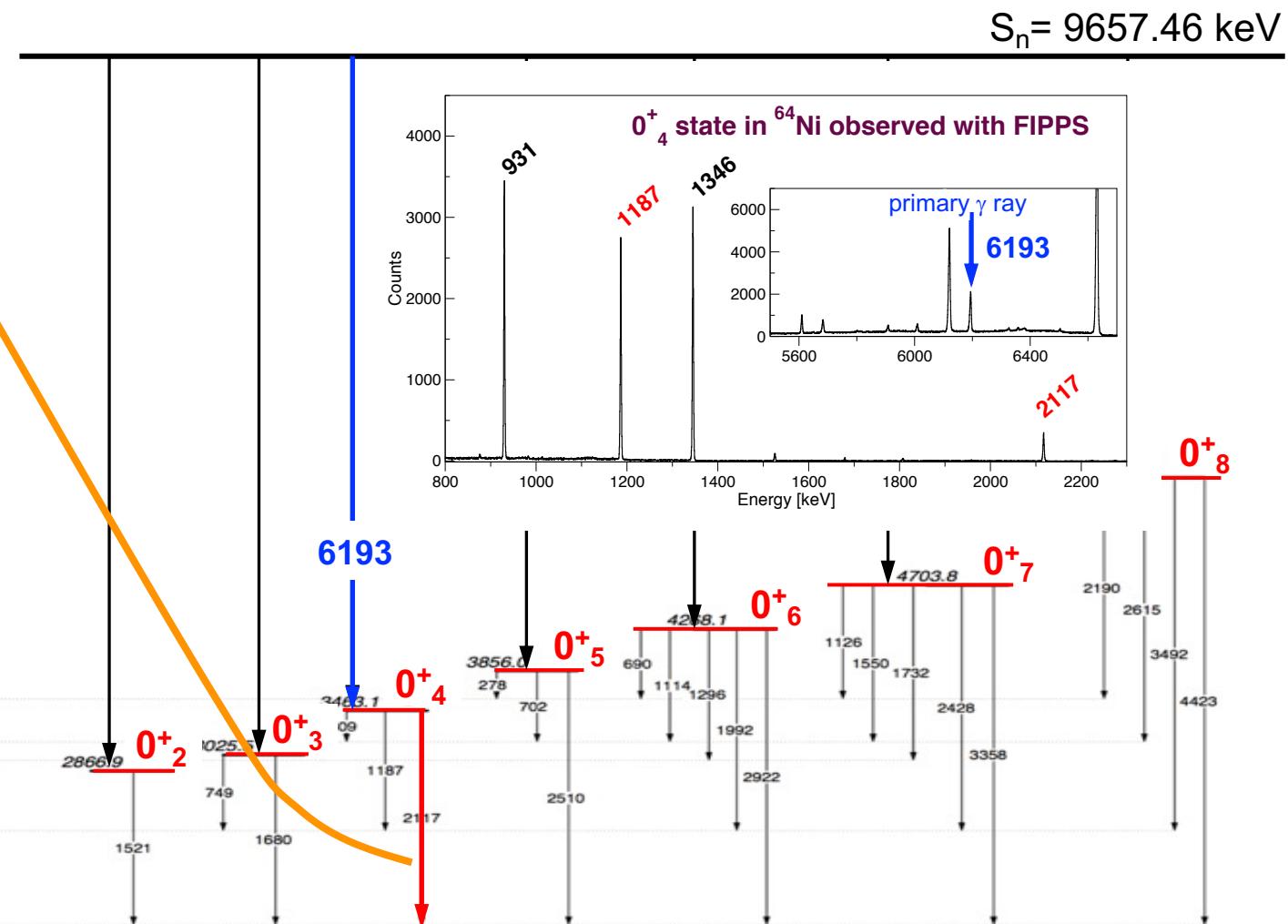
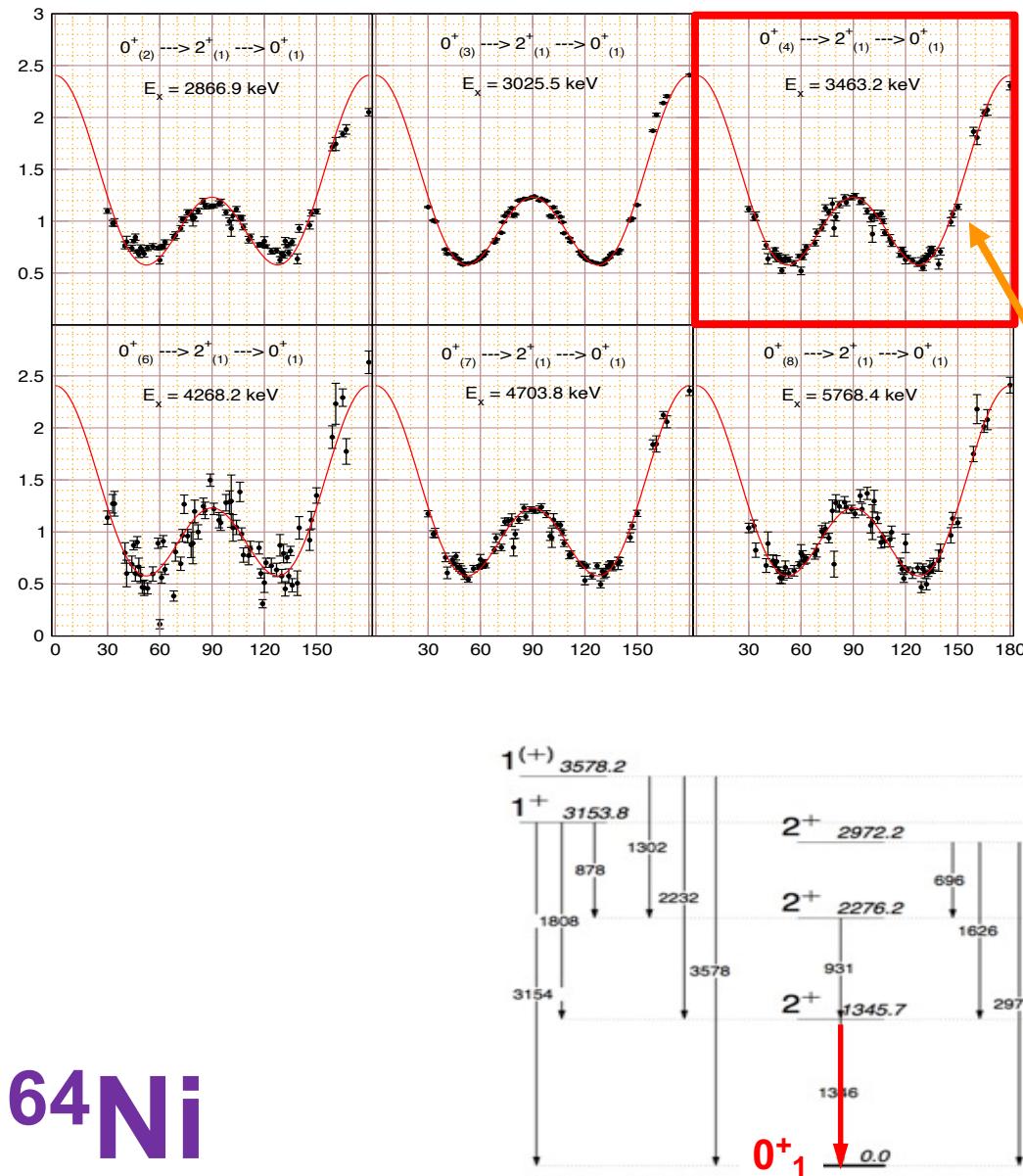
**to achieve the required experimental sensitivity**

- 1) IFIN-HH (ROSPHERE):** sub-barrier transfer ( $1\text{p}, 2\text{n}$ )
- 2) ILL (FIPPS):** neutron capture
- 3) Argonne (GRETINA):** Coulomb excitation
- 4) TUNL:** ( $\gamma, \gamma'$ )

**a multimessenger approach ...**

*(79 co-authors from 25 Institutions)*

# The most complex level scheme: (n, $\gamma$ ) experiment with FIPPS array at ILL (2019) - 2 GigaBq $^{63}\text{Ni}$ target



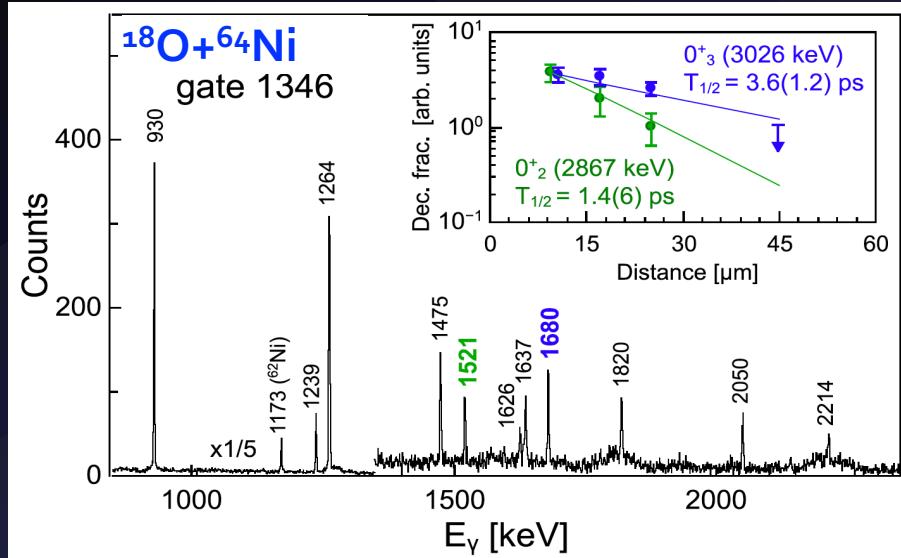
extended decay pattern: seven  $0^+$  states, six  $2^+$  states, ....

$^{64}\text{Ni}$

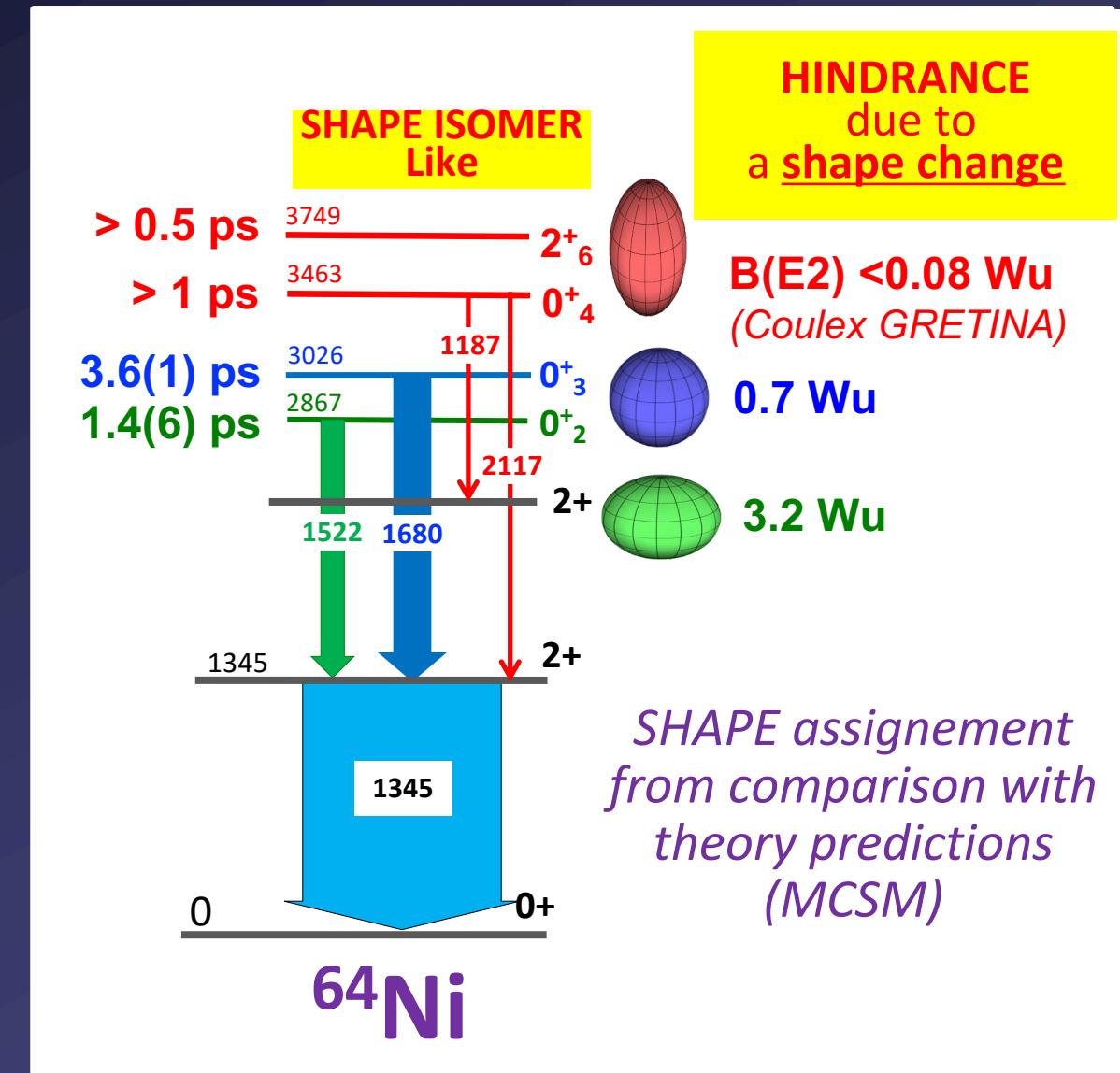
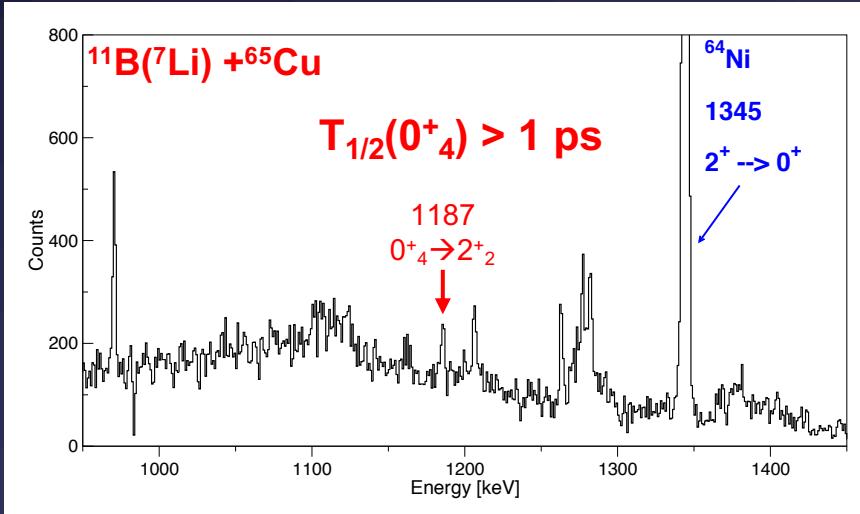
- IFIN-HH – Lifetimes measurements
- Argonne (GRETINA) – Coulomb Excitations

**64Ni**

**2n**



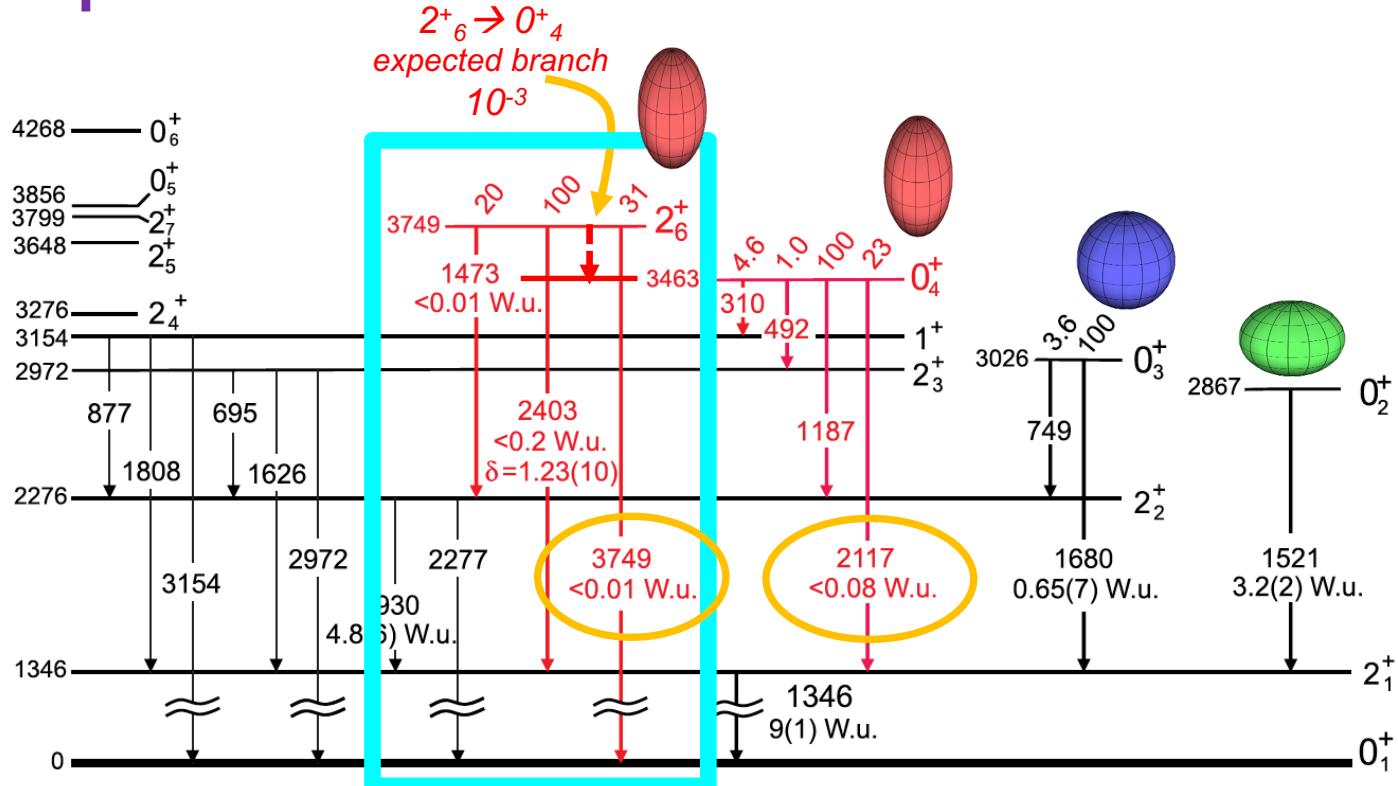
**1p**



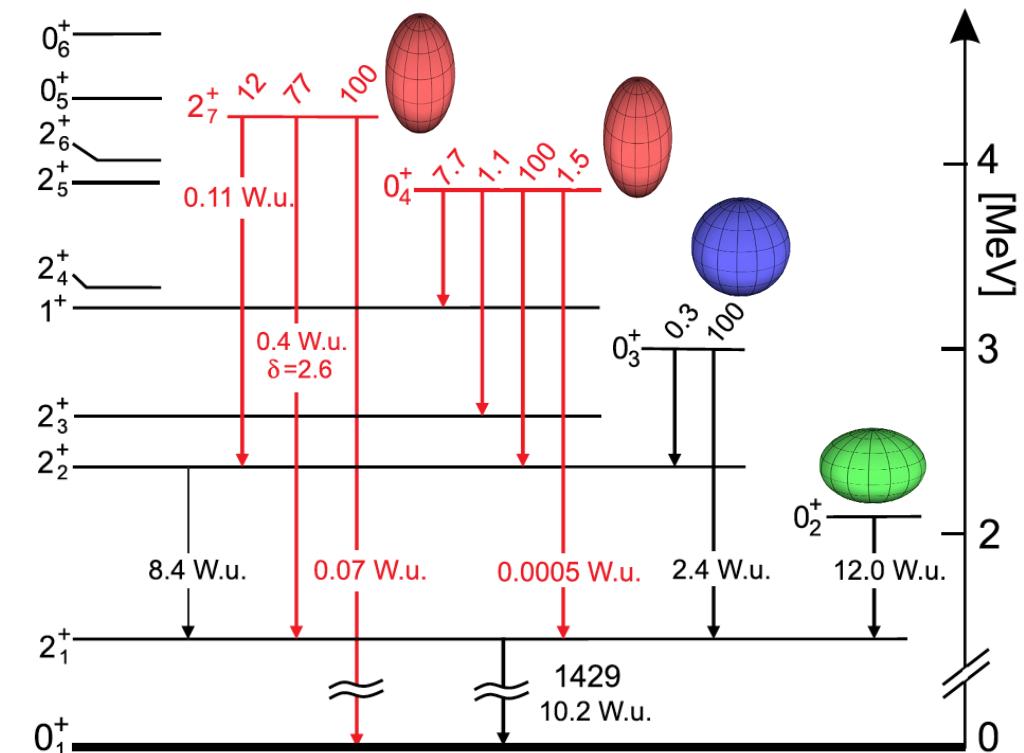
# Extended comparison with Theory

microscopic interpretation of the nature of  $0^+$  excitations

## Experiment



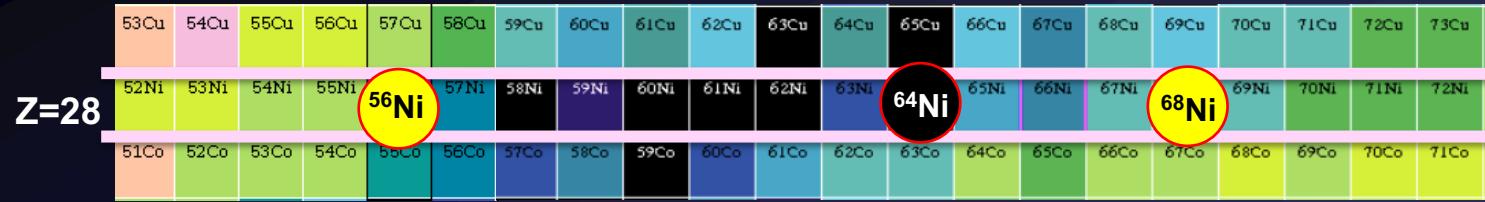
## Theory MCSM



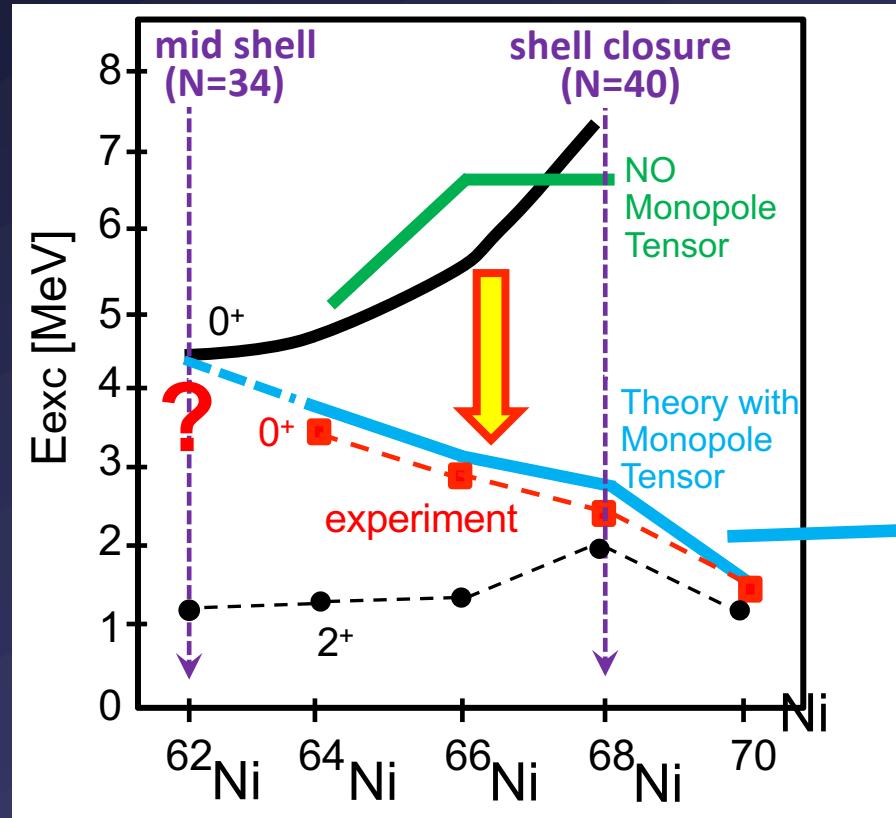
$\rightarrow 0^+_4 \rightarrow 2^+_1$  and  $2^+_6 \rightarrow 0^+_1$ : two transitions strongly hindered !!  
 $\rightarrow$  The TENSOR FORCE is responsible for the coexistence of shapes in  $^{64}\text{Ni}$  otherwise expected to be spherical !!!

# Evolution of the energies of PROLATE $0^+$ states in the Ni chain

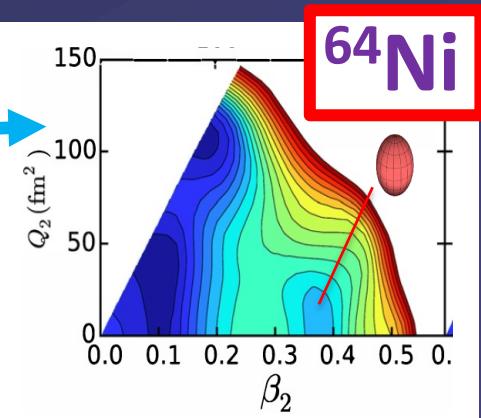
## Impact of Monopole Tensor Term



Traditional view of  
PARABOLA behavior of  
deformed bands:  
 $2p-2h, 4p-4h, \dots$   
excitations across the energy gap



**EXTRA BINDING**  
given by  
**MONOPOLE-TENSOR PART**  
of nucleon-nucleon force



DEEP prolate minimum in PES

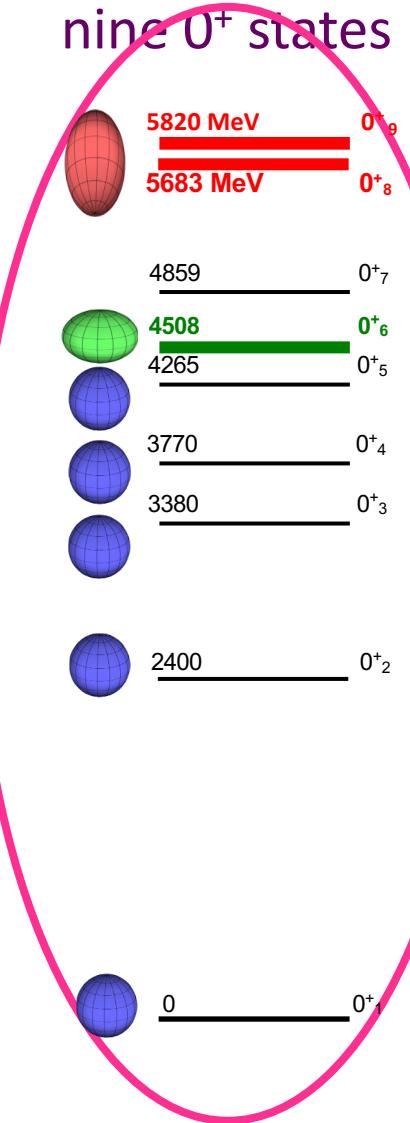
# Current Investigation

**$^{62}\text{Ni}$**

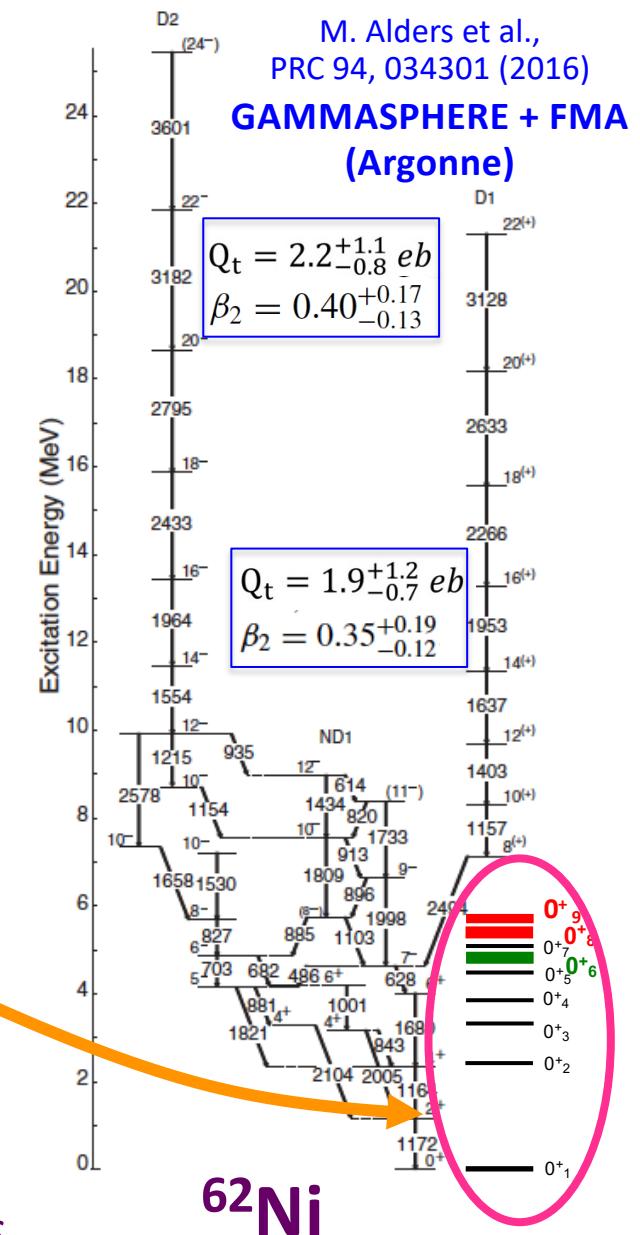
at  $N=34$   
mid shell

## $^{62}\text{Ni} - \text{MCSM}$ (very preliminary)

nine  $0^+$  states

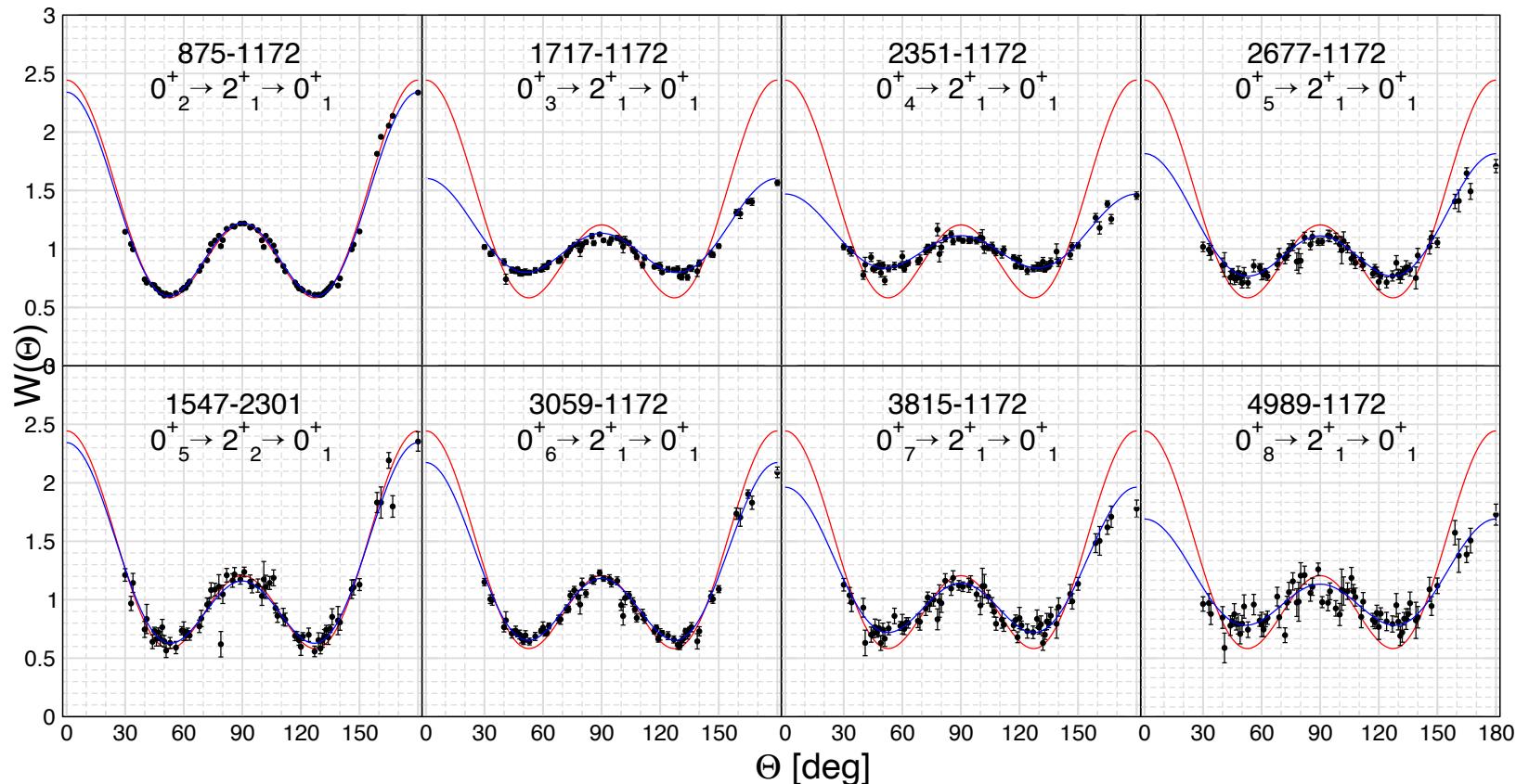


*deformed  $0^+$  states  
could be the  
**BANDHEADS**  
of rotational structures  
observed at higher spins*

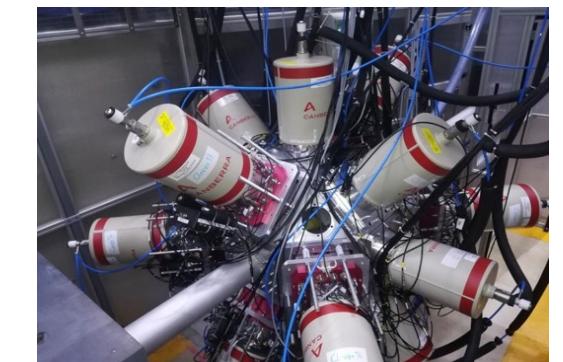
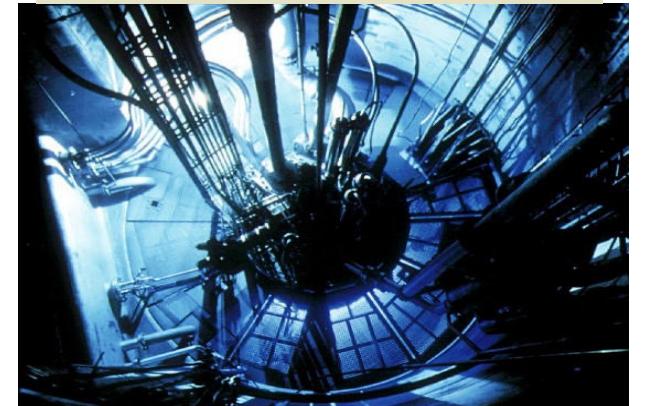


# $^{62}\text{Ni}$ data from $^{61}\text{Ni}(\text{n},\gamma)$ reaction with FIPPS at ILL

Large statistics and high-precision angular correlations



Pencil-like intense thermal neutron beam



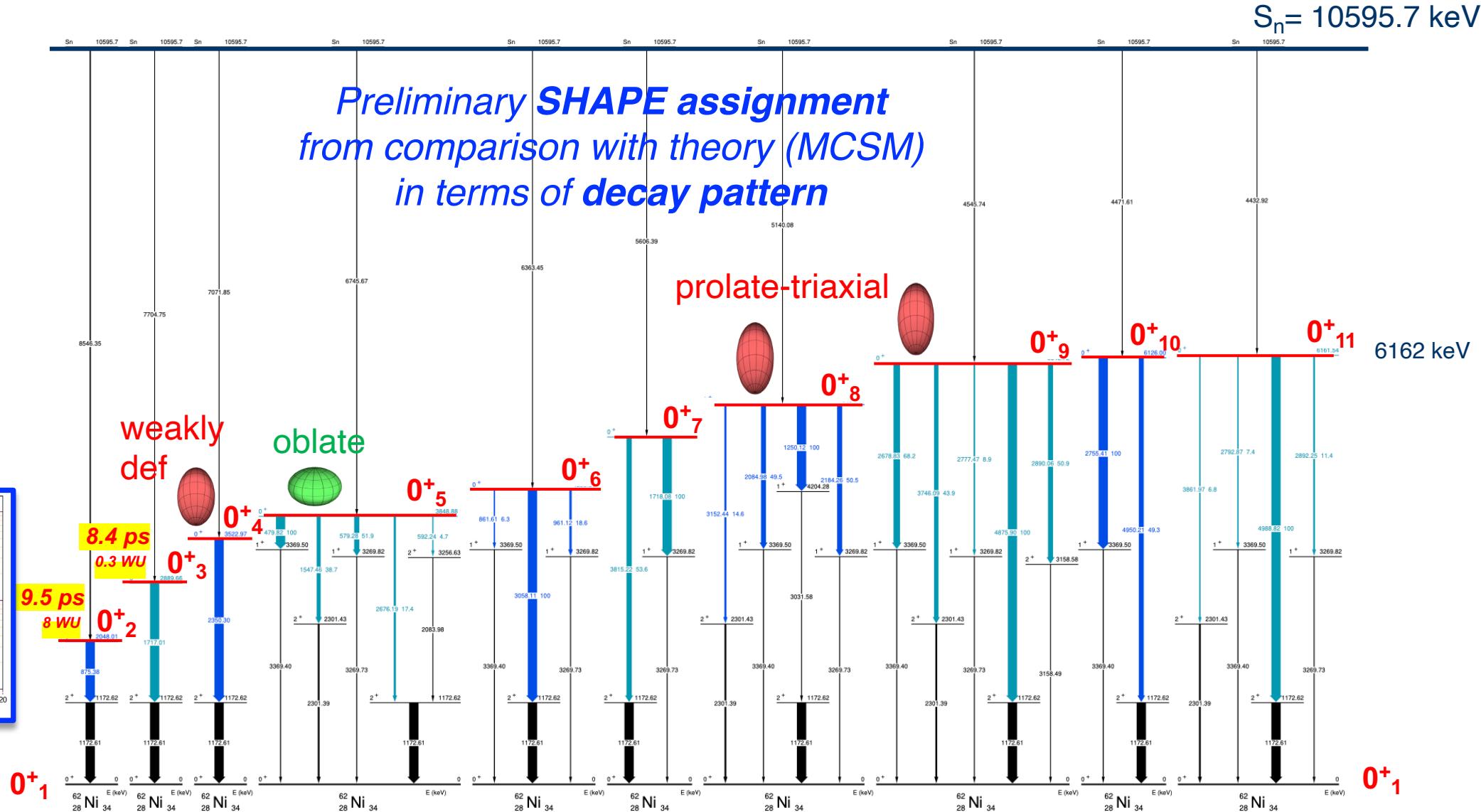
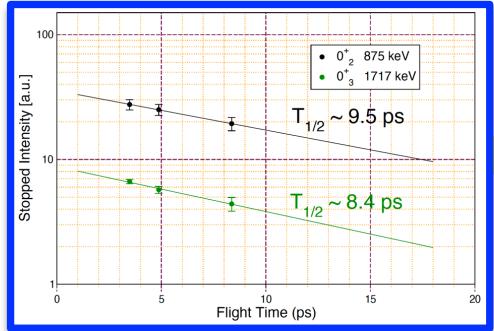
16 HPGe clovers (8 from IFIN-HH) high resolution and efficiency  $\gamma$  detector array

# 10 excited $0^+$ states observed in $^{62}\text{Ni}$

Preliminary, C. Costache and N. Marginean, IFIN-HH, Bucharest

*lifetime  
measurements  
with DSAM  
(2n transfer)  
Orsay Data  
NUBALL 1  
June 2018*

*lifetime  
measurements  
with PLUNGER  
(2n transfer)  
ROSPHERE  
July 2023-ongoing*



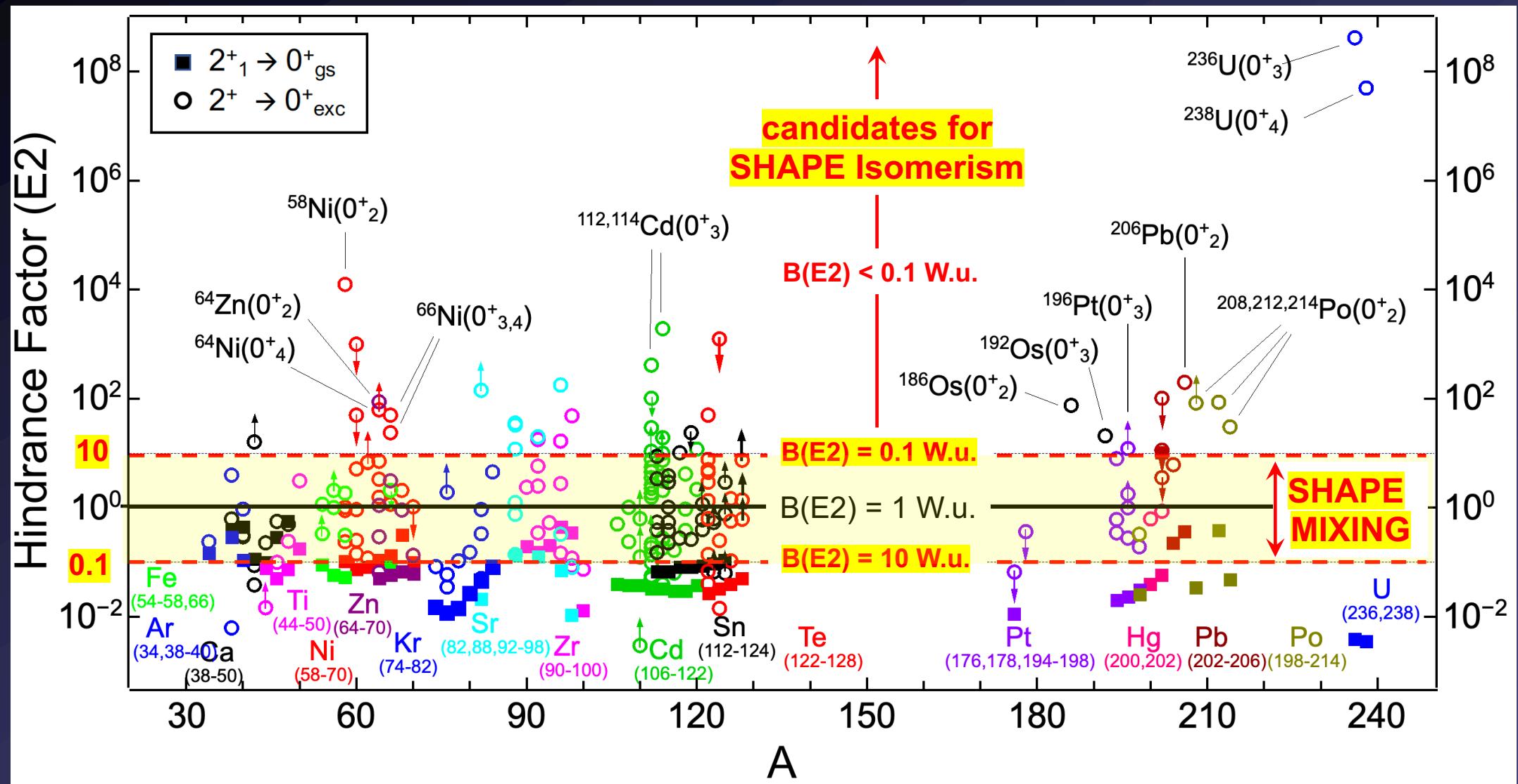
# Lesson learned from Ni studies

- 1) evidence for shape-isomer-like  $0^+$  states in  $^{64,66}\text{Ni}$   
(with  $B(E2, 0^+ \rightarrow 2^+_1) < 1 \text{ W.u.}$ )
- 2) Important role played by monopole tensor force  
in the origin of deformation  
**!!! Shape coexistence without parabola !!!**

Where to search for other shape-isomer-like  $0^+$  states?

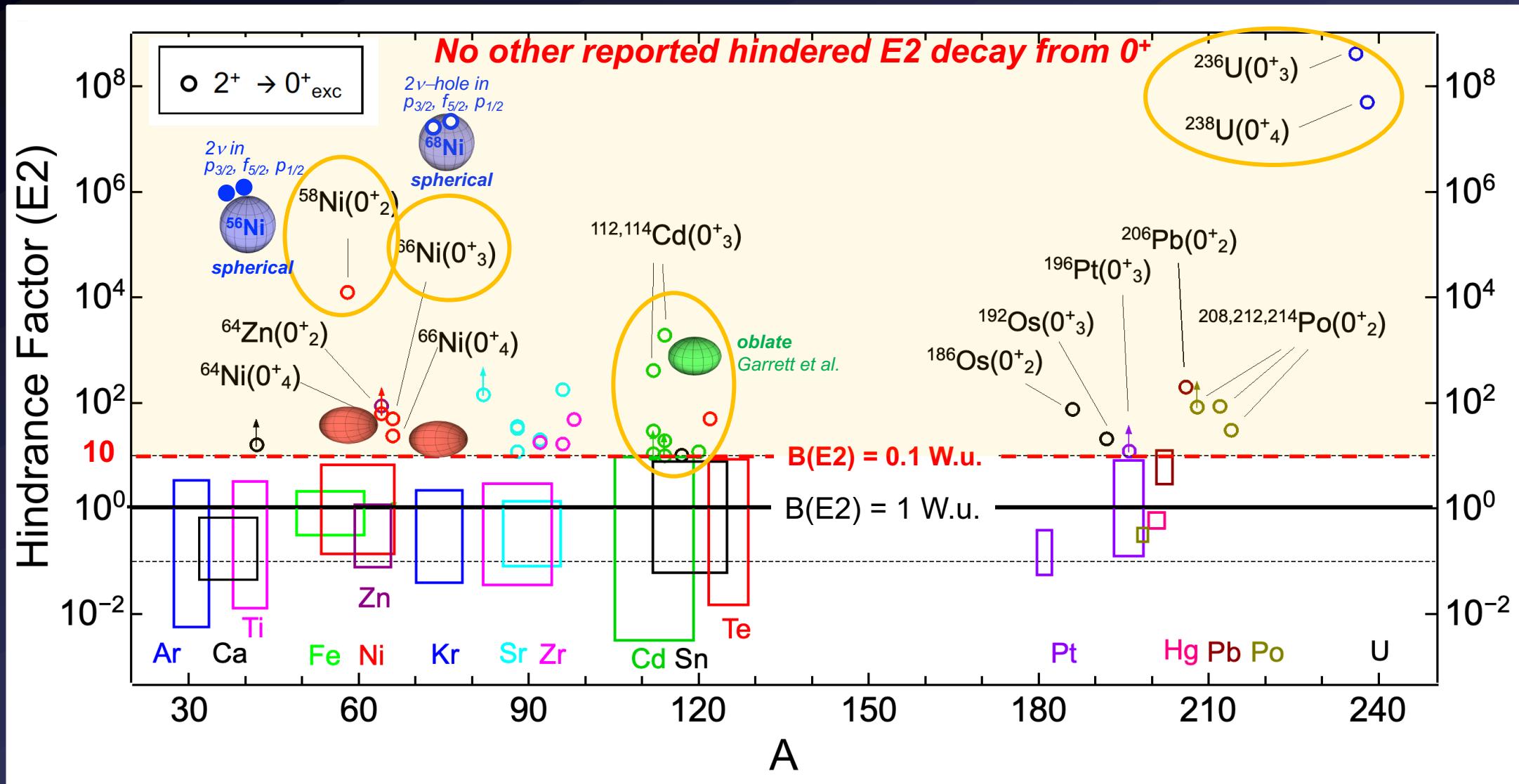
# Survey of HINDRANCE (E2) factors for $0^+$ states

in the proximity of  $Z = 20, 28, 40, 50, 82$



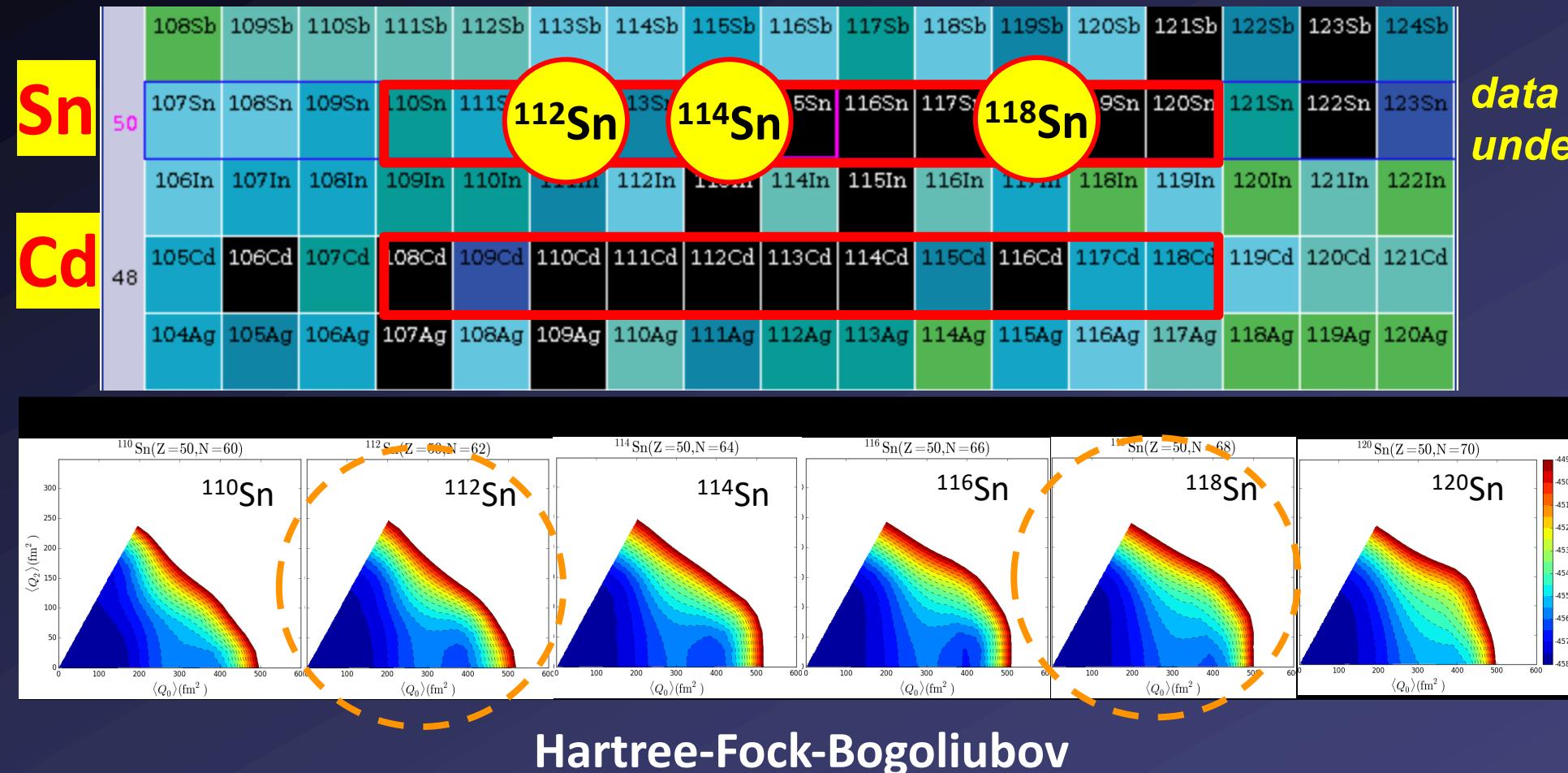
# Survey of HINDRANCE (E2) factors for $0^+$ states

in the proximity of  $Z = 20, 28, 40, 50, 82$



# Our new project: Systematic Study of Shape coexistence in Sn nuclei

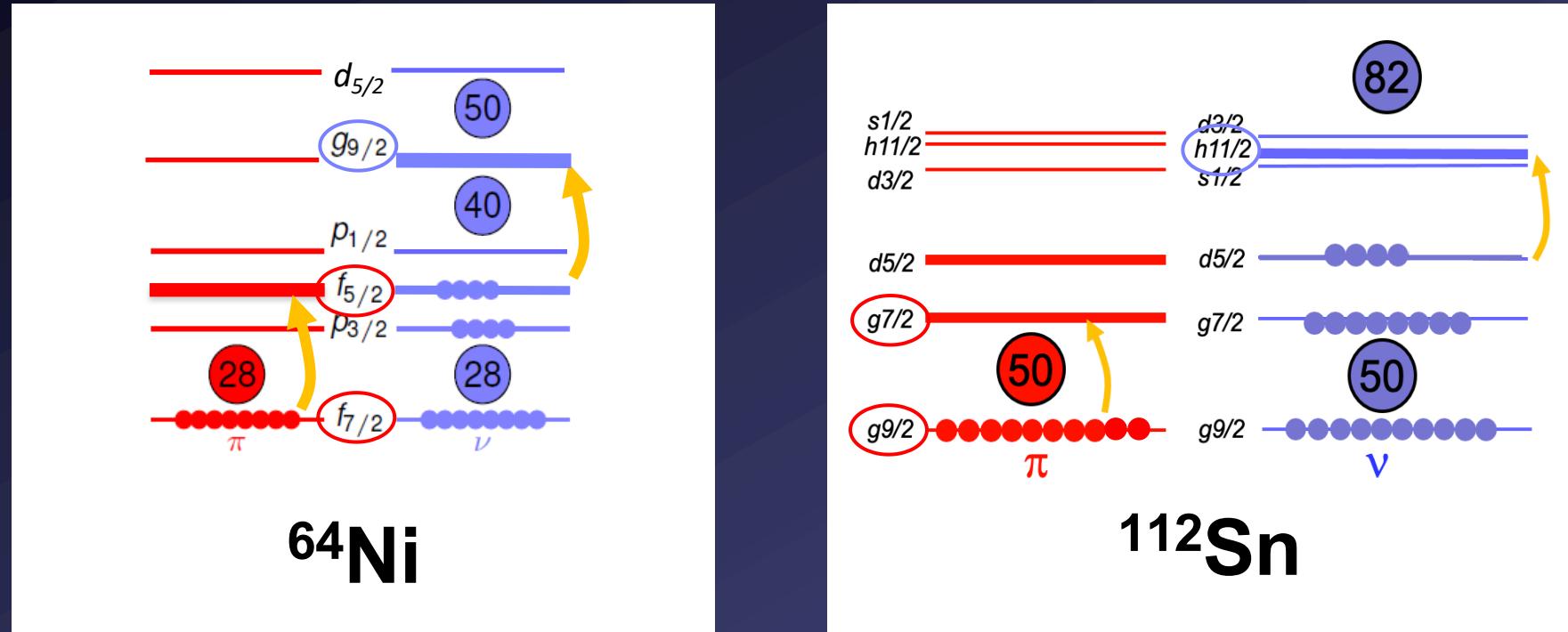
expected scenario similar to Ni



interaction from Togashi et al., PRL121, 062501 (2018)

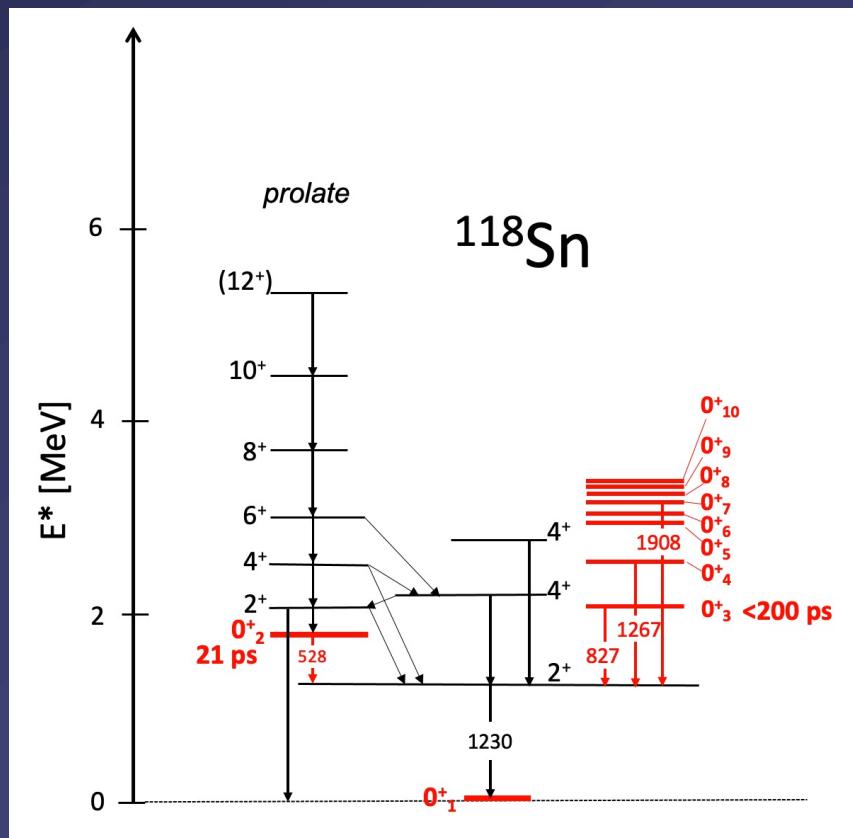
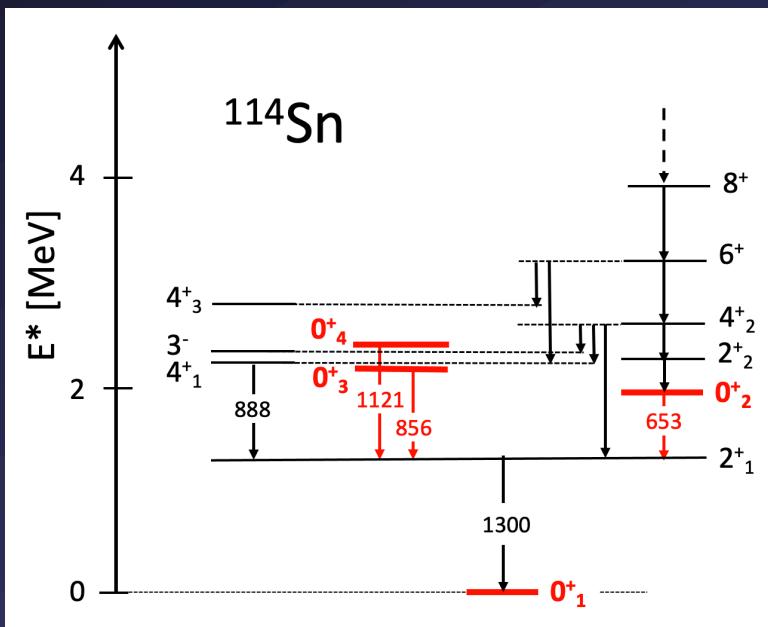
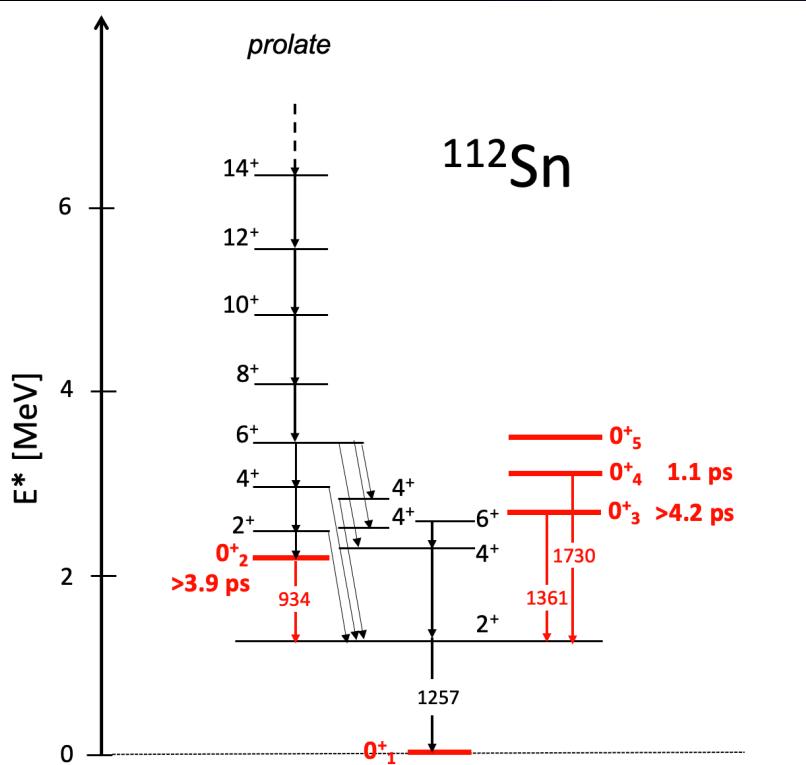
$^{112}\text{Sn}$  and  $^{118}\text{Sn}$  are first and last isotopes with an expected well-developed prolate minimum

# SIMILAR MECHANISM for Spontaneous Symmetry Breaking (spherical $\rightarrow$ deformed) induced by proton-neutron interaction



*deep prolate minima might be expected  
due to monopole tensor force*

# Several excited $0^+$ states identified in $^{112,114,118}\text{Sn}$ , but no lifetimes measured



## Performed/planned experiments:

$^{18}\text{O} + ^{112}\text{Sn} \rightarrow ^{114}\text{Sn}$ : lifetime (DSAM and Plunger), ROSPHERE (2022)

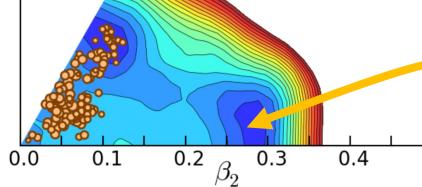
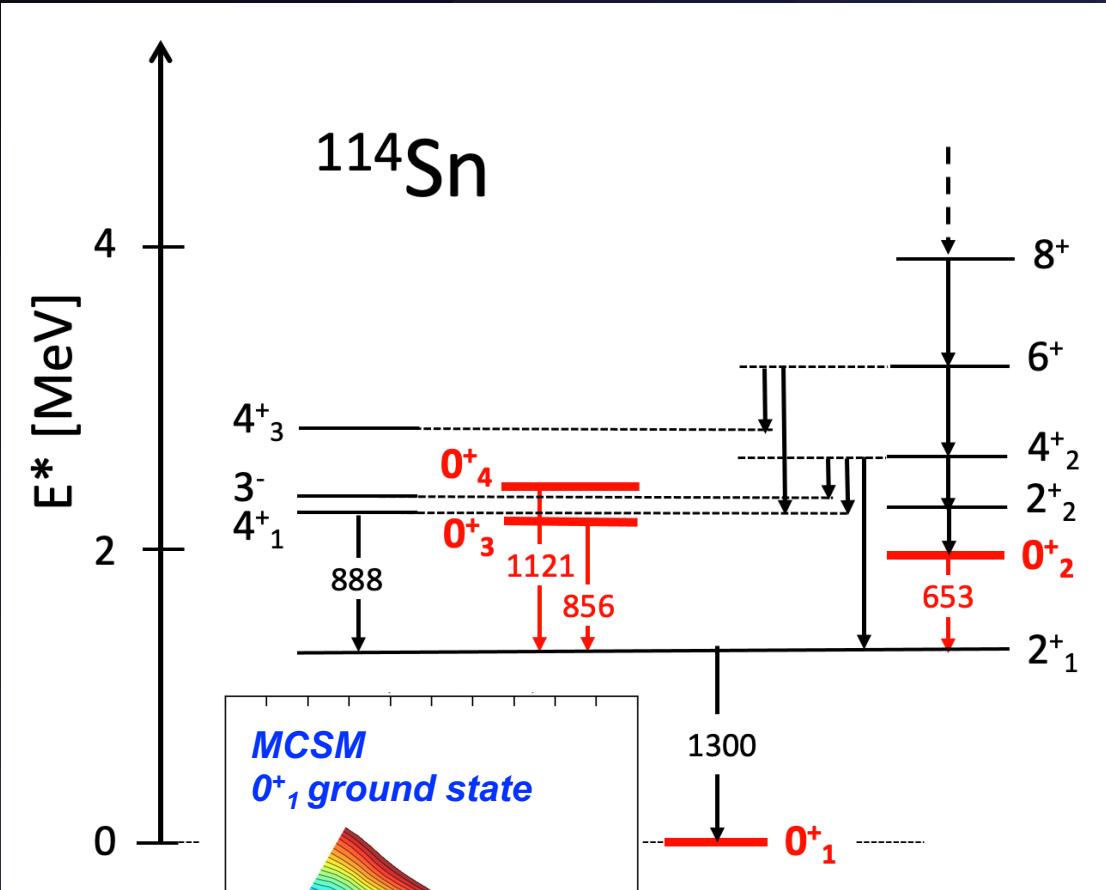
$^{32}\text{S} + ^{110}\text{Cd} \rightarrow ^{112}\text{Sn}$ : lifetime (Plunger), AGATA+PRISMA (2022)

1n, 2n, 2p, alpha transfer  $\rightarrow ^{118}\text{Sn}$ : ROSPHERE (2023)

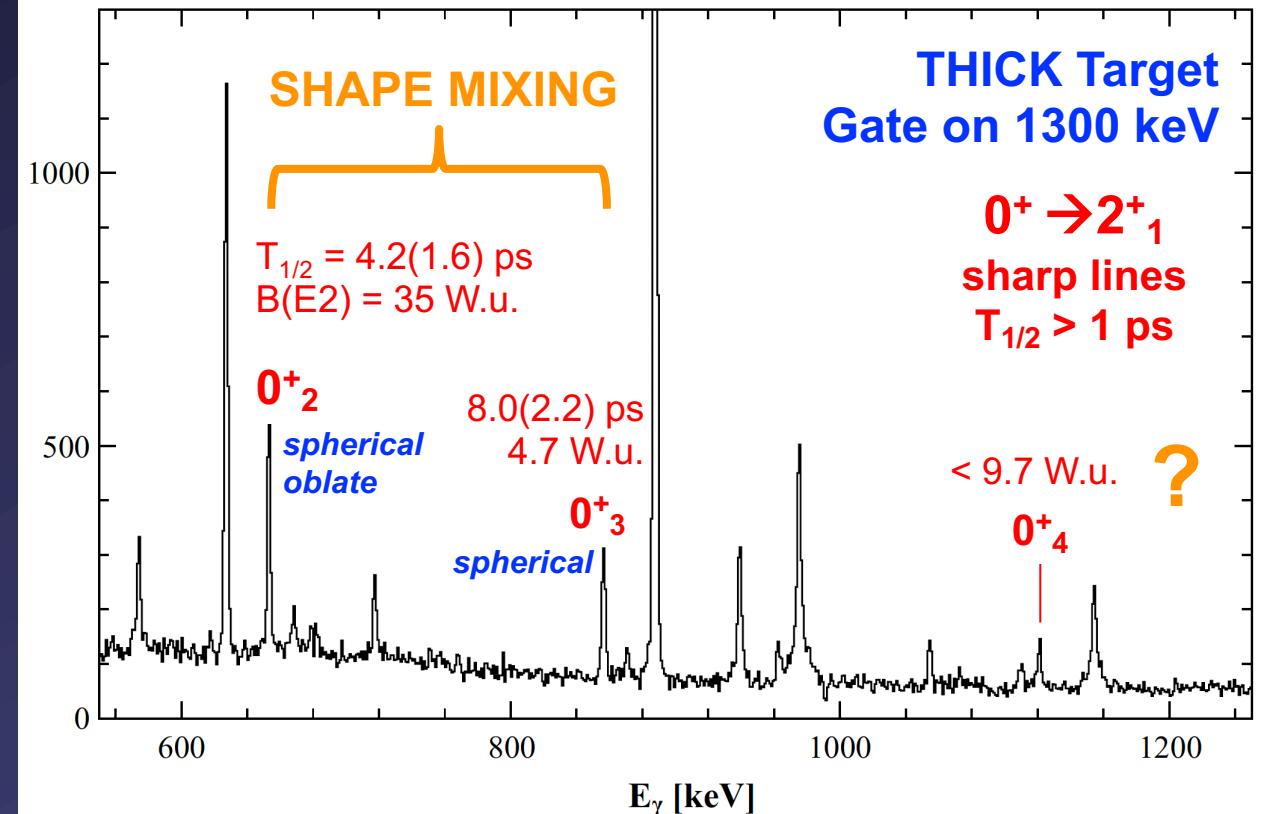
# Preliminary - $^{114}\text{Sn}$

G. Corbari PhD, Milano University

$^{18}\text{O} + ^{112}\text{Sn} \rightarrow ^{114}\text{Sn}$ :  
lifetime (DSAM and Plunger)  
ROSPHERE @ IFIN (2022)



$0^+_4$  might be a prolate shape-isomer-like structure !!!



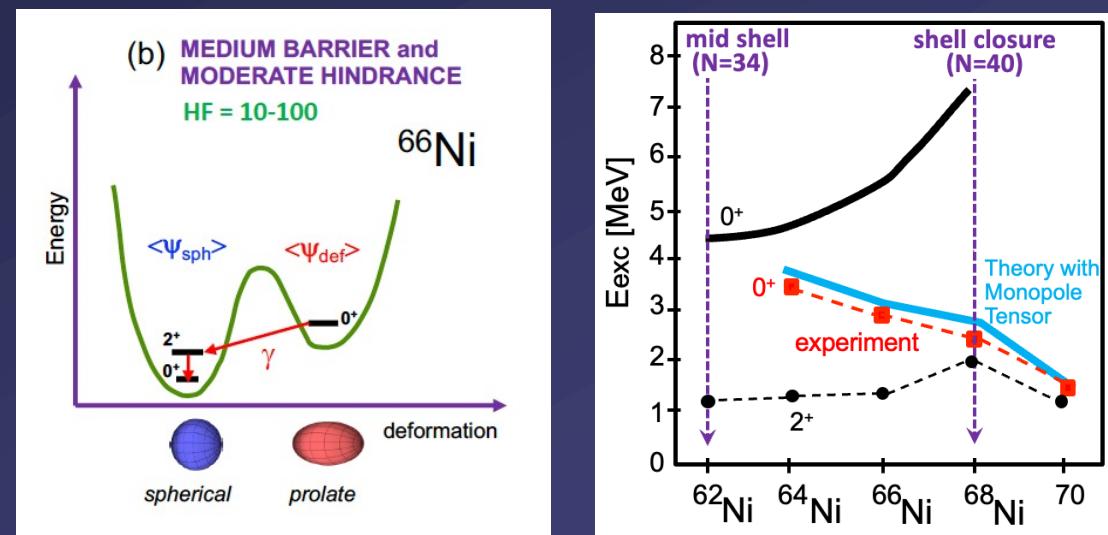
# Conclusions: search for **SHAPE ISOMERS** in medium mass nuclei

only few cases exist with  $\gamma$  decay between structures with different shapes **significantly hindered** ( $B(E2) \ll 1$ ,  $HF > 10$ )

we have focused on  $^{64}\text{Ni}$  and  $^{66}\text{Ni}$  ...  $^{62}\text{Ni}$  ongoing

## Lesson learned:

- 1) **Hindrance** results from **wave functions well localized** in different PES minima, separated by a **sizable barrier**  
The wave functions «do not talk to each other»  
This gives rise to **SHAPE ISOMERISM**
- 2) The **TENSOR force** plays a key role, **deepening the minima**:  
in Ni isotopes – Shape coexistence **WITHOUT PARABOLA**



## In general, at SPIN 0:

NO HINDRANCE for decay between different shapes  
**Wave functions NOT well localized**  $\rightarrow$  **SHAPE MIXING**  
Such states may still be ISOMERIC for other reasons.

## FUTURE PLANS: $^{112}\text{Sn}$ - $^{118}\text{Sn}$ chain

with complementary probes  
 $\rightarrow$  expected similarities with Ni isotopes