

# Structural Evolution of the Neutron-Rich Calcium Isotopes

Pieter Doornenbal

ピーター ドーネンバル



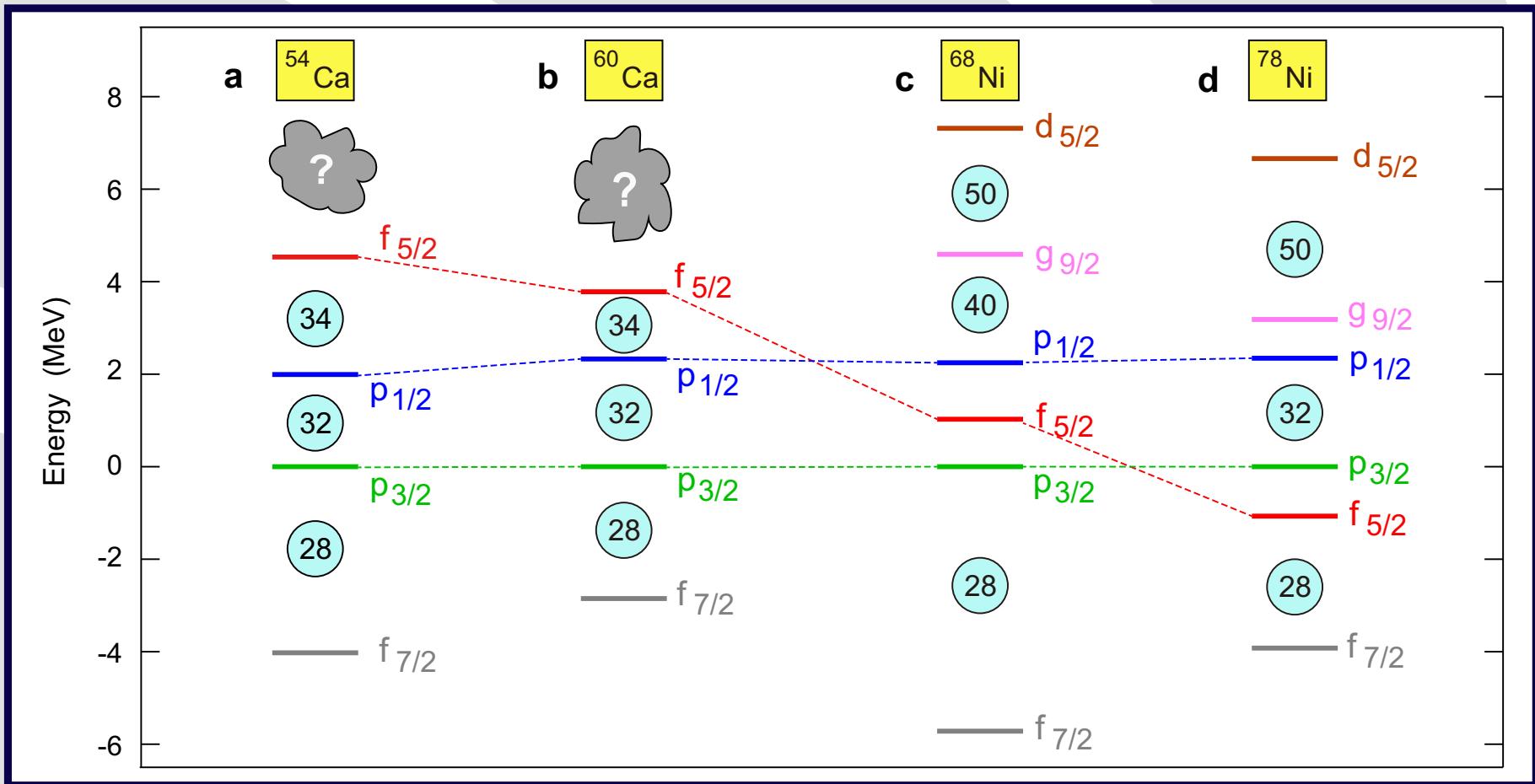


# Outline

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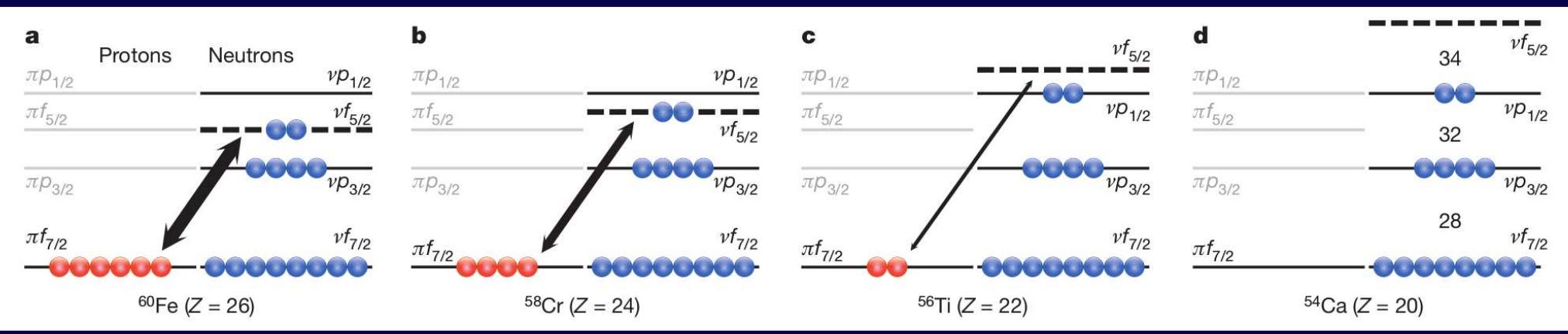
- Motivation
  - ◆ The  $N = 32, 34, 40$  magic numbers
  - ◆ Evolution of neutron single particle energies
- Experimental description
  - ◆ RIBF, DALI2<sup>+</sup>, MINOS, SAMURAI, NeuLAND/NEBULA
- Results
  - ◆ Detailed spectroscopy of  $^{54}\text{Ca}$  from (p,pn) and (p,2p) reactions
  - ◆ First spectroscopy of  $^{56,58}\text{Ca}$  from (p,2p) reactions
  - ◆ Neutron single particle states in  $^{51,53,55}\text{Ca}$
- Summary

# Effective Neutron Single Particle Energies



- ESPE calculations with A3DA-t and A3DA-m Hamiltonian
- Influence of  $d_{5/2}$  and  $g_{9/2}$ ? Is  $N = 40$  magic?
- How “magic” are  $N = 32, 34$  in  $^{52,54}\text{Ca}$ ?
- Ca: Closed proton shell → Structure dominated by valence neutrons

# Shell Evolution at $N = 32, 34$



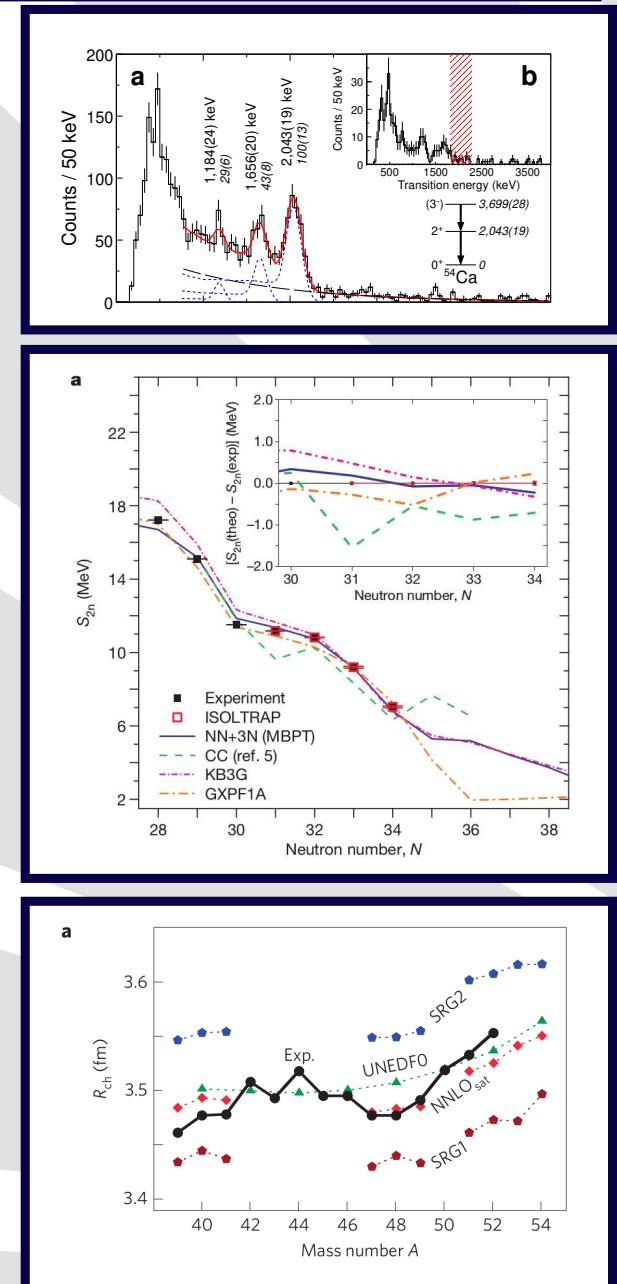
- Reduced attractive interaction between  $\pi f_{7/2}$  and  $\nu f_{5/2}$
- Possible development of new sub-shell closures at  $N = 32$  and  $N = 34$
- Observation of  $N = 32$  sub-shell closure for  $^{52}\text{Ca}$ ,  $^{54}\text{Ti}$
- A single proton in  $\pi f_{7/2}$  destroys  $N = 34$  magicity!

D. Steppenbeck et al., Nature 502, 207 (2013).

Prediction for  $N = 34$  magic Number: T. Otsuka et al., PRL 87, 082502 (2001).

# Observations for Ca Isotopes

- Significant  $N = 32, 34$  shell closures:
  - ◆ Large  $E(2_1^+)$ :
    - $^{52}\text{Ca}$ : A. Huck et al., PRC 31, 2226 (1985).
    - $^{52}\text{Ca}$ : A. Gade et al., PRC 74, 021302 (2006).
    - $^{54}\text{Ca}$ : D. Steppenbeck et al., Nature 502, 207 (2013).
  - ◆ Large shell gap  $\Delta_{2n}$ :
    - $^{54}\text{Ca}$ : F. Wienholtz et al., Nature 498, 346 (2013).
    - $^{55-57}\text{Ca}$ : S. Michimasa et al., PRL 121, 022506 (2018).
  - ◆ Small  $0f_{5/2}$  occupation in g.s. of  $^{54}\text{Ca}$ :
    - S. Chen et al., PRL 123, 142501 (2019).
- Large charge radii question  $N = 32$  shell closure:
  - $^{52}\text{Ca}$ : R.F. Garcia Ruiz et al., Nature Physics 12, 596 (2016).
- First observation of  $^{60}\text{Ca}$ :
  - O. Tarasov et al., PRL 121, 022501 (2018).

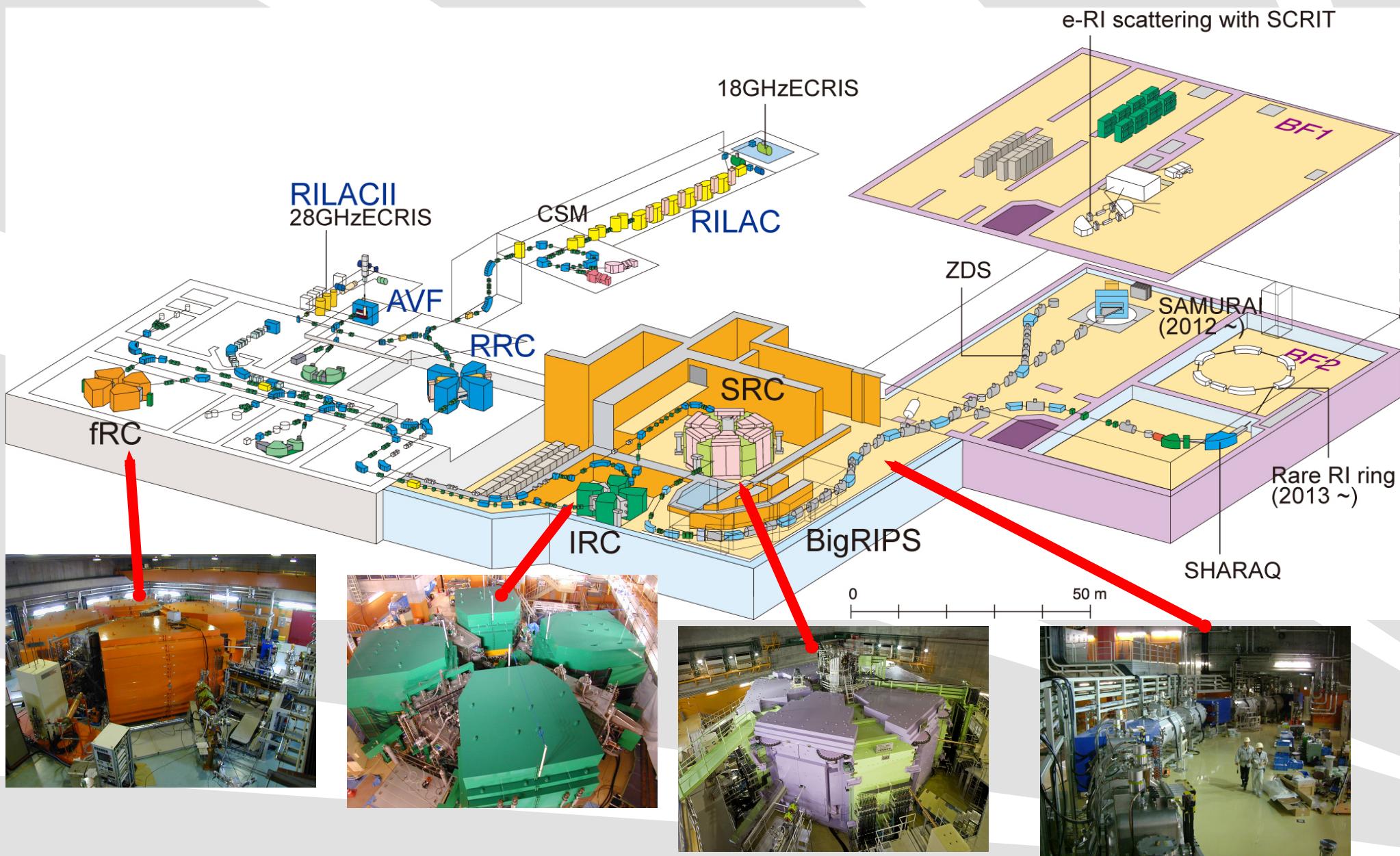




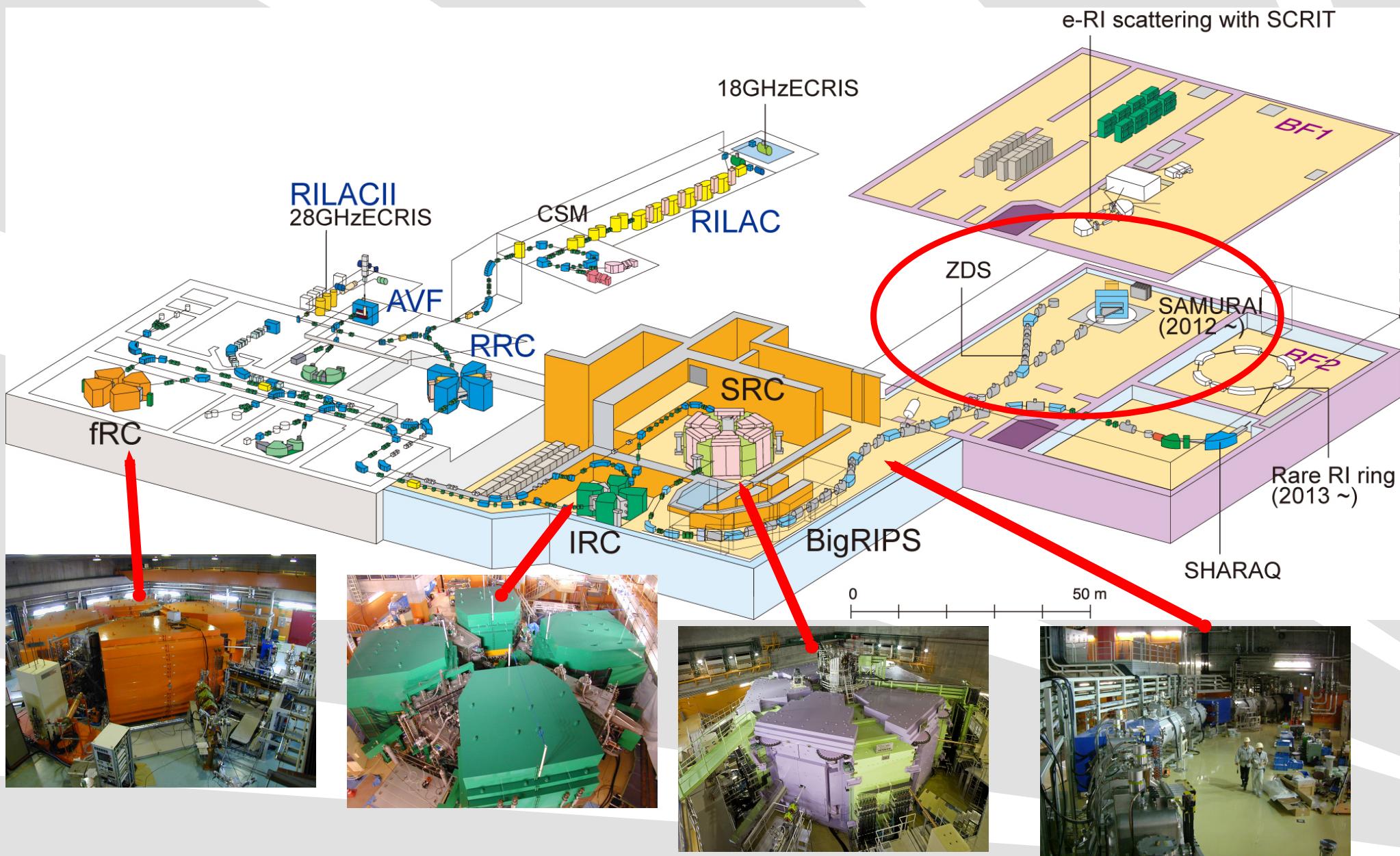
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# Experimental Setup

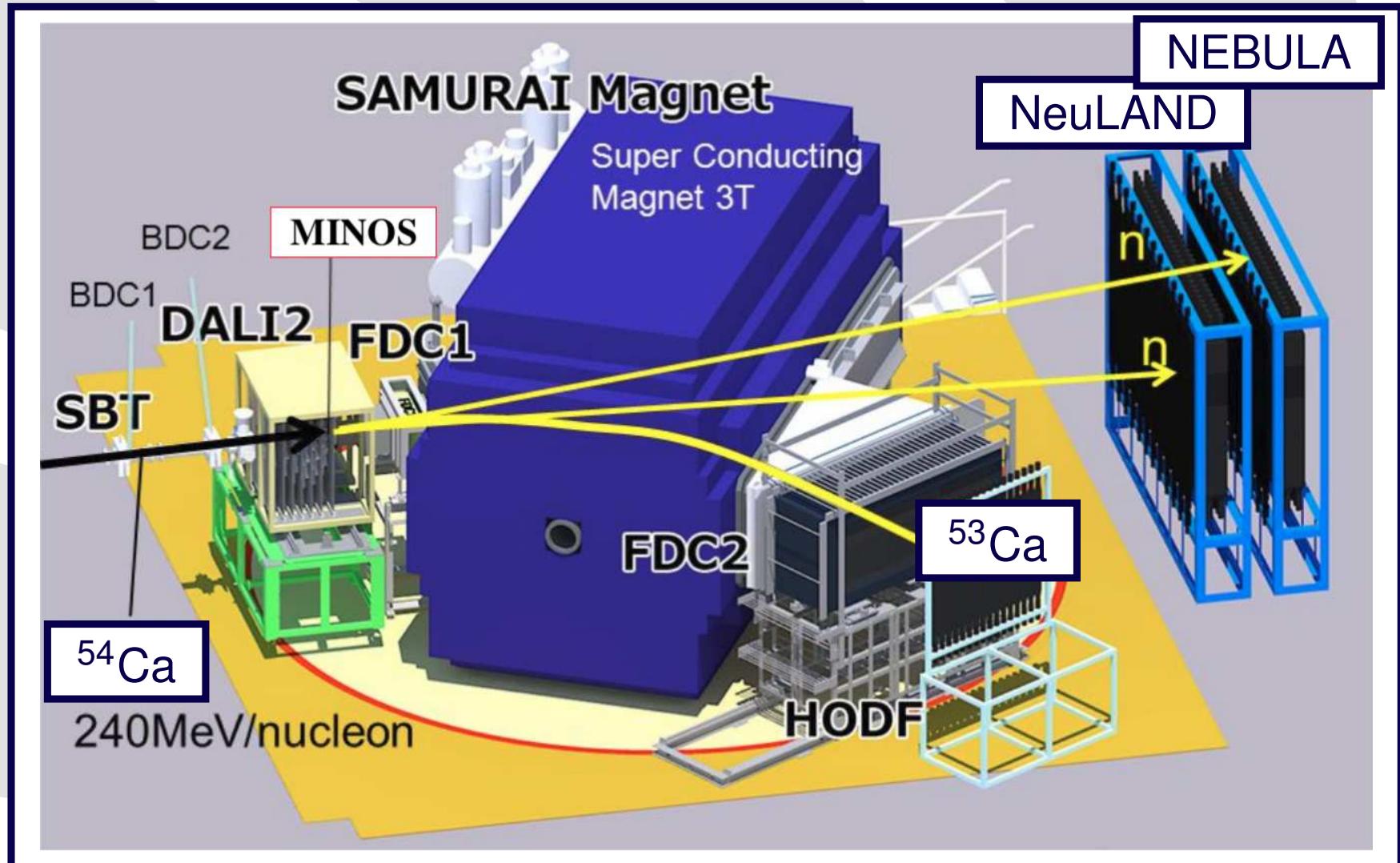
# RIBF Overview



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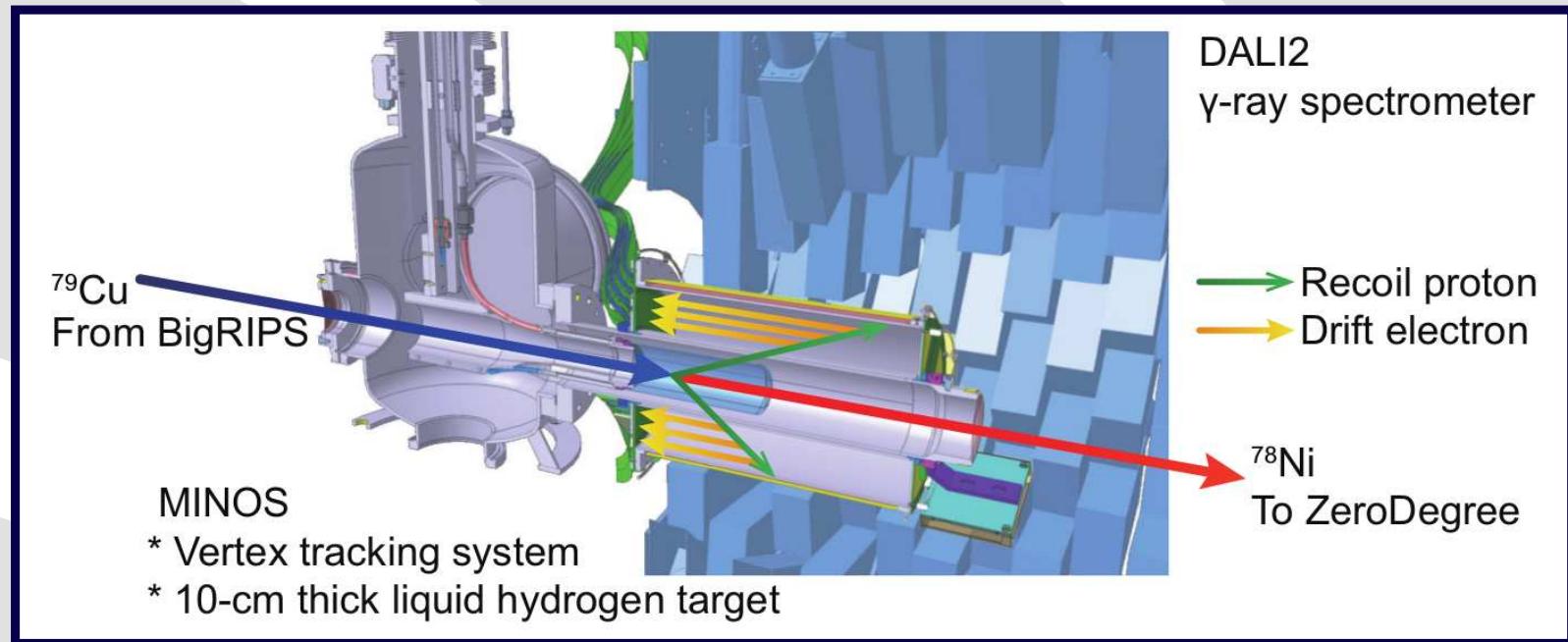


# Shell Evolution And Search for Two-plus energies At RIBF (SEASTAR) at SAMURAI



- Large acceptance
  - ◆ Simultaneous  $E(2_1^+)$  measurement of  $^{52}\text{Ar}$ ,  $^{56,58}\text{Ca}$ , and  $^{62}\text{Ti}$
  - ◆ Many other isotopes within acceptance

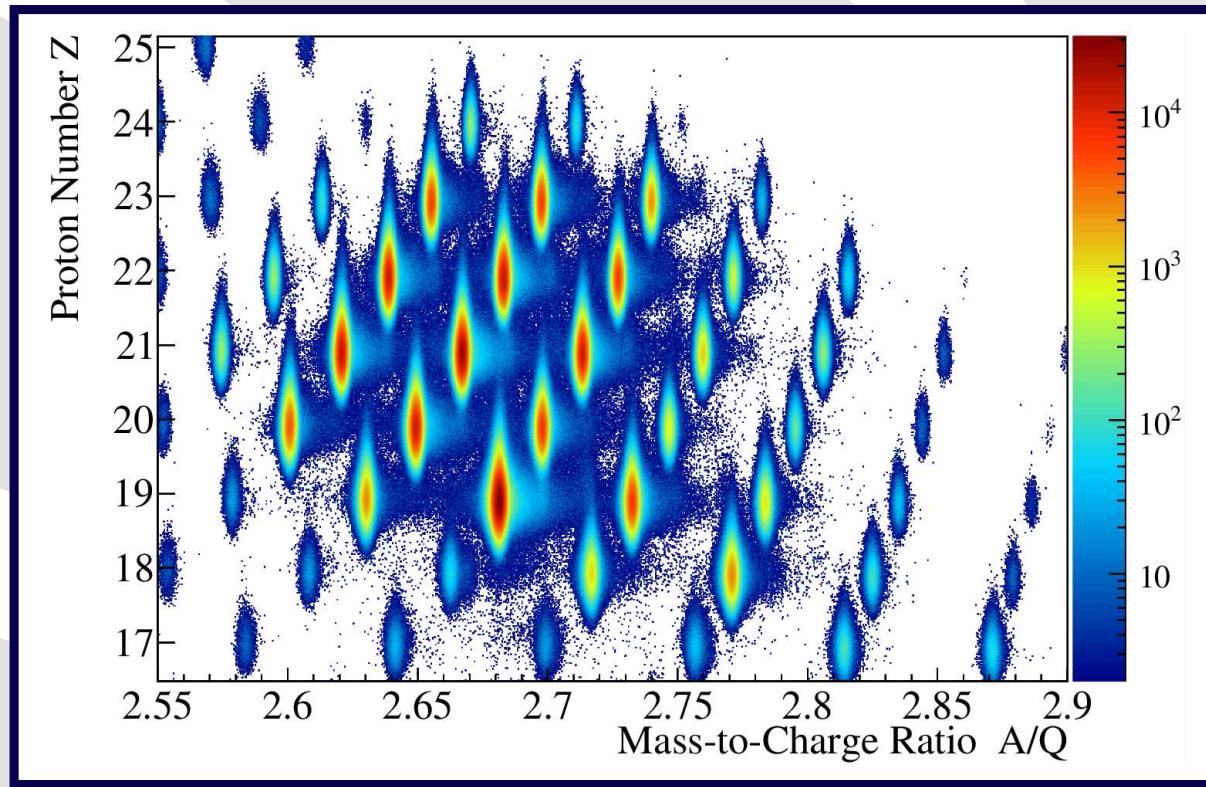
# In-Beam Gamma-Ray Spectroscopy With a Liquid Hydrogen Target



- MINOS, Magic Numbers Off Stability
  - ◆ up to  $1 \text{ g/cm}^2$  (150 mm) liquid hydrogen target, velocity  $\beta \approx 0.6$
  - ◆ Position sensitive TPC, Vertex position reconstruction with  $\approx 5 \text{ mm}$  (FWHM)
- DALI2+
  - ◆ 186 (226) NaI(Tl) detectors, large solid angle coverage
  - ◆ 7 % intrinsic resolution at 1 MeV, 10(11) % at 100(250) MeV/nucleon
  - ◆ 35 % efficiency at 1 MeV with add-back

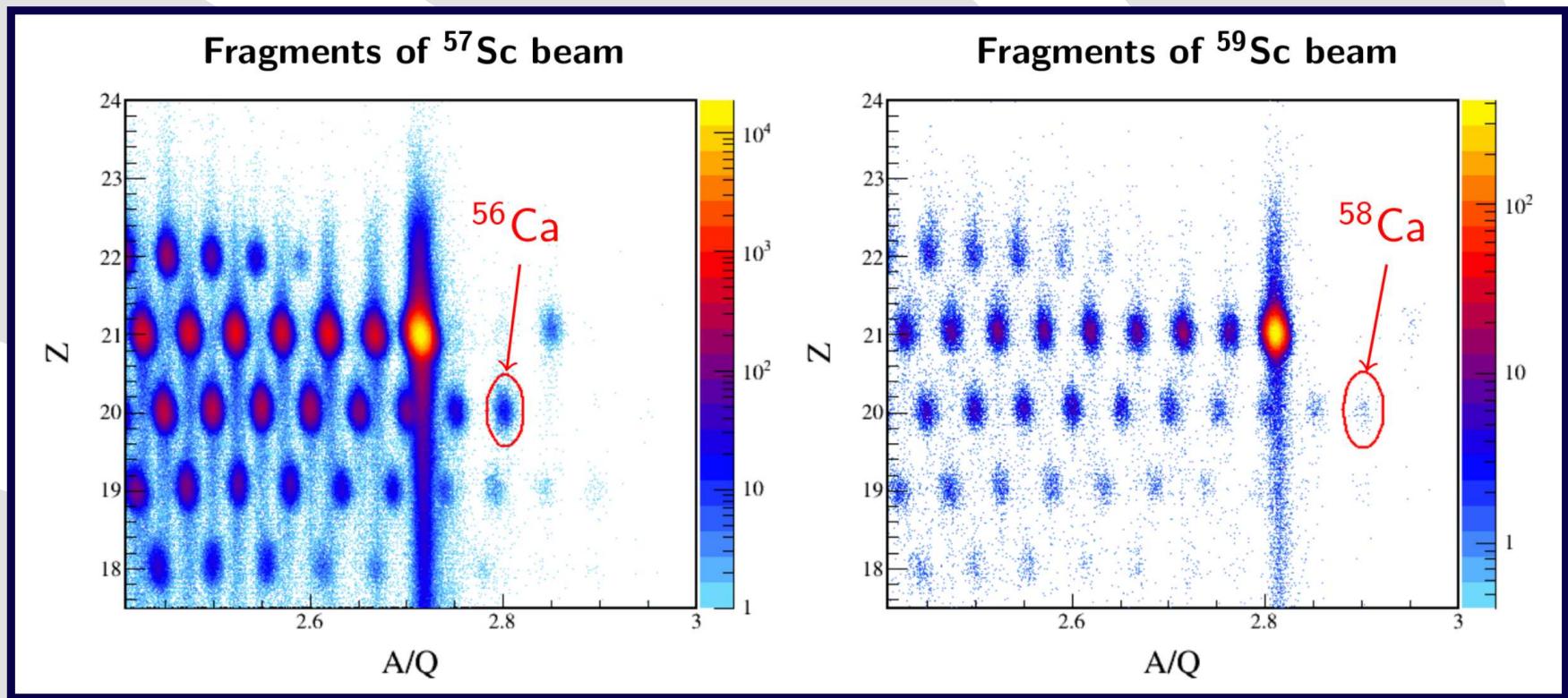
A. Obertelli et al., EPJA 50, 8 (2014), S. Takeuchi et al., NIMA 763, 596 (2014).

# SEASTAR III at SAMURAI Particle Identification



- $^{70}\text{Zn}$  primary beam, 345 MeV/nucleon, 240 pnA, 8 days
- Secondary beam at 240 MeV/nucleon,  $\delta p/p = \pm 3\%$
- ONE unique setting
- Total beam intensity: 200 pps
- $^{53}\text{K}$ : 0.8 pps,  $^{57}\text{Sc}$ : 13.6 pps,  $^{59}\text{Sc}$ : 0.3 pps,  $^{63}\text{V}$ : 3 pps

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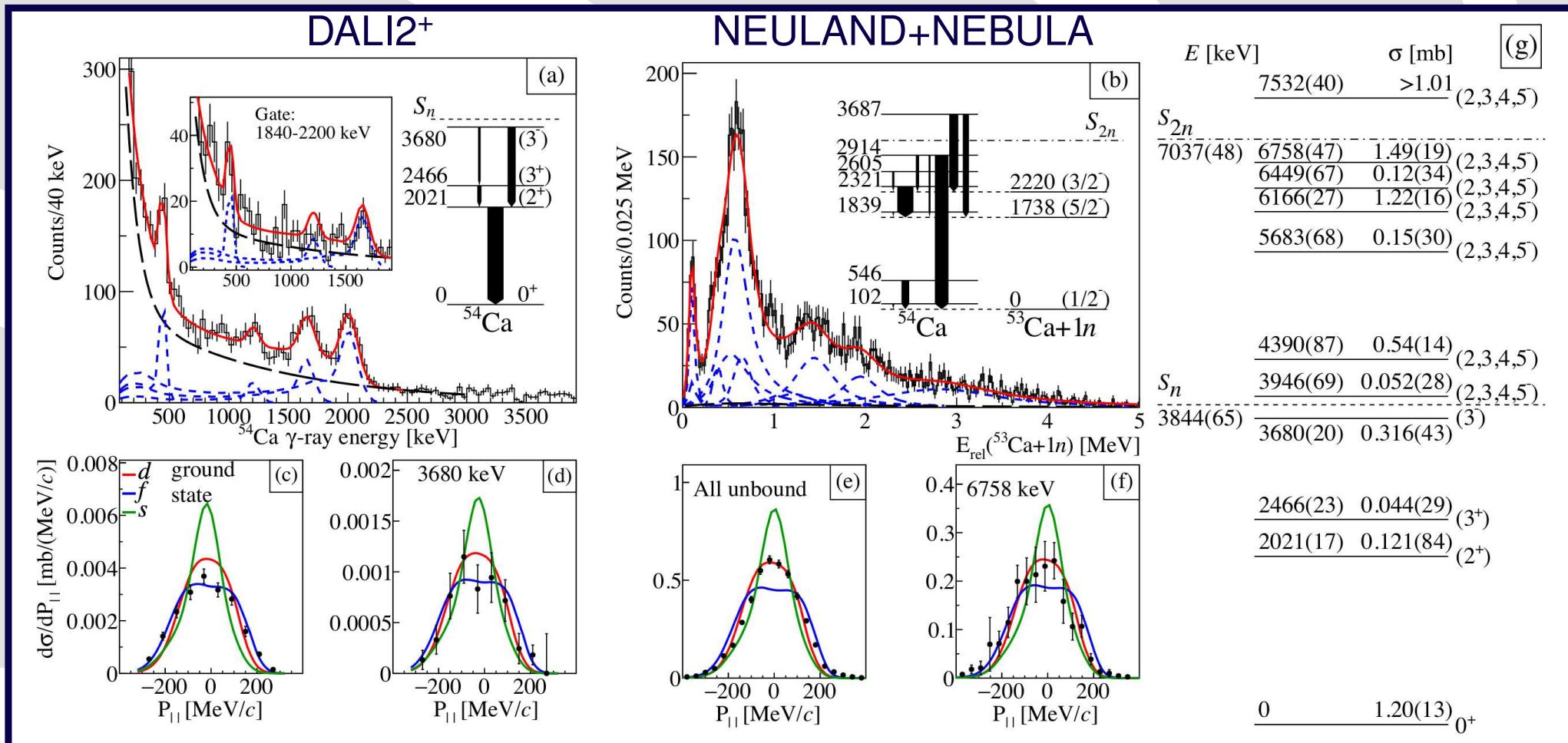


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# Detailed Spectroscopy of $^{54}\text{Ca}$

# Detailed Spectroscopy of $^{54}\text{Ca}$ from $^{55}\text{Sc}(\text{p},2\text{p})^{54}\text{Ca}$ and $^{55}\text{Ca}(\text{p},\text{pn})^{54}\text{Ca}$

$^{55}\text{Sc}(\text{p},2\text{p})^{54}\text{Ca}$  case:

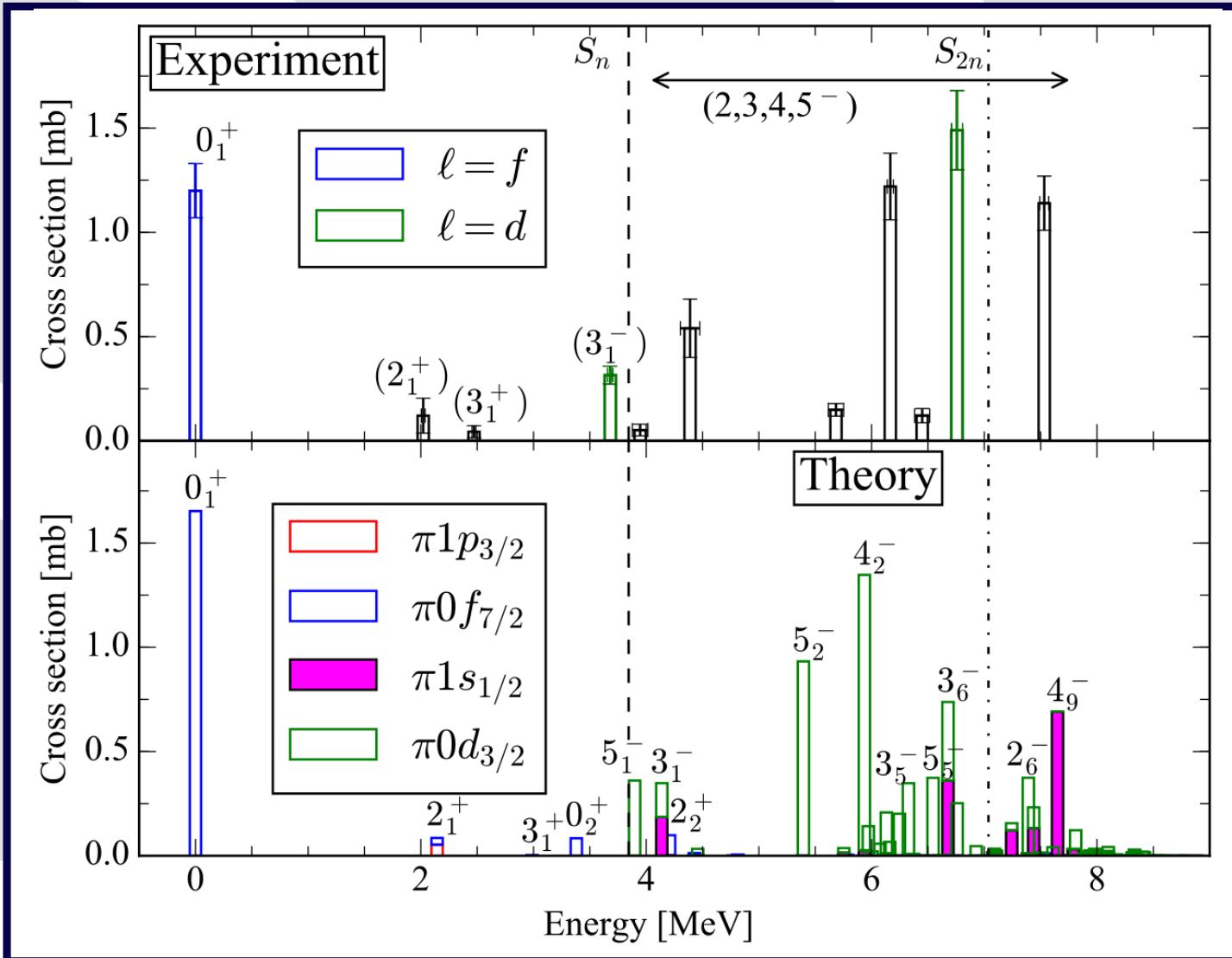


First Spectroscopy of  $^{54}\text{Ca}$ : D. Steppenbeck, S. Takeuchi et al., Nature 502, 207 (2013).

This work: F. Browne, S. Chen et al., PRL 126, 252501 (2021).

Theory: GXPF1Br interaction in full  $sd - pf - gds$  model space, DWIA for  $\sigma_{sp}$  and  $P_{||}$

# Detailed Spectroscopy of $^{54}\text{Ca}$ from $^{55}\text{Sc}(\text{p},2\text{p})^{54}\text{Ca}$ and $^{55}\text{Ca}(\text{p},\text{pn})^{54}\text{Ca}$



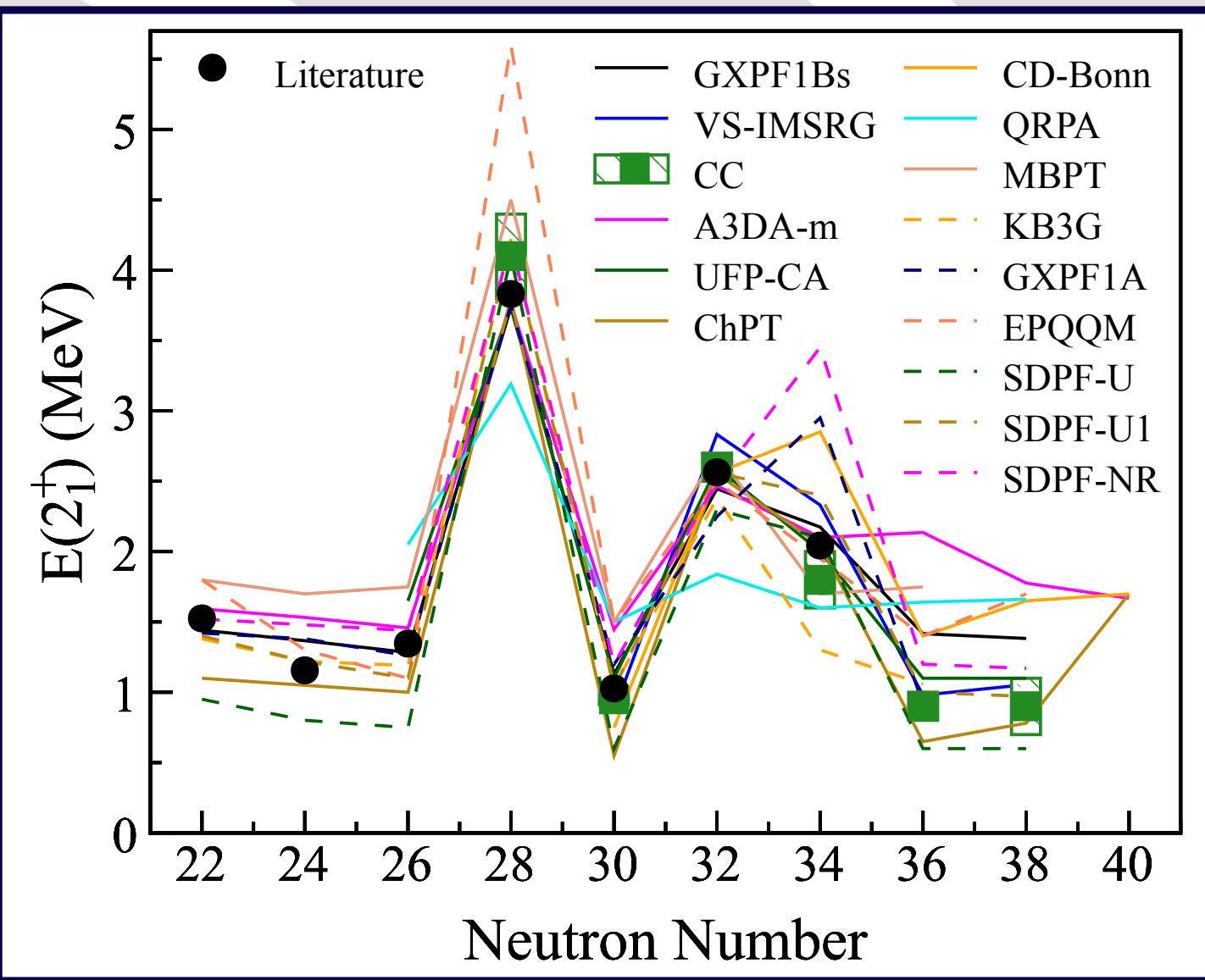
First Spectroscopy of  $^{54}\text{Ca}$ : D. Steppenbeck, S. Takeuchi et al., Nature 502, 207 (2013).  
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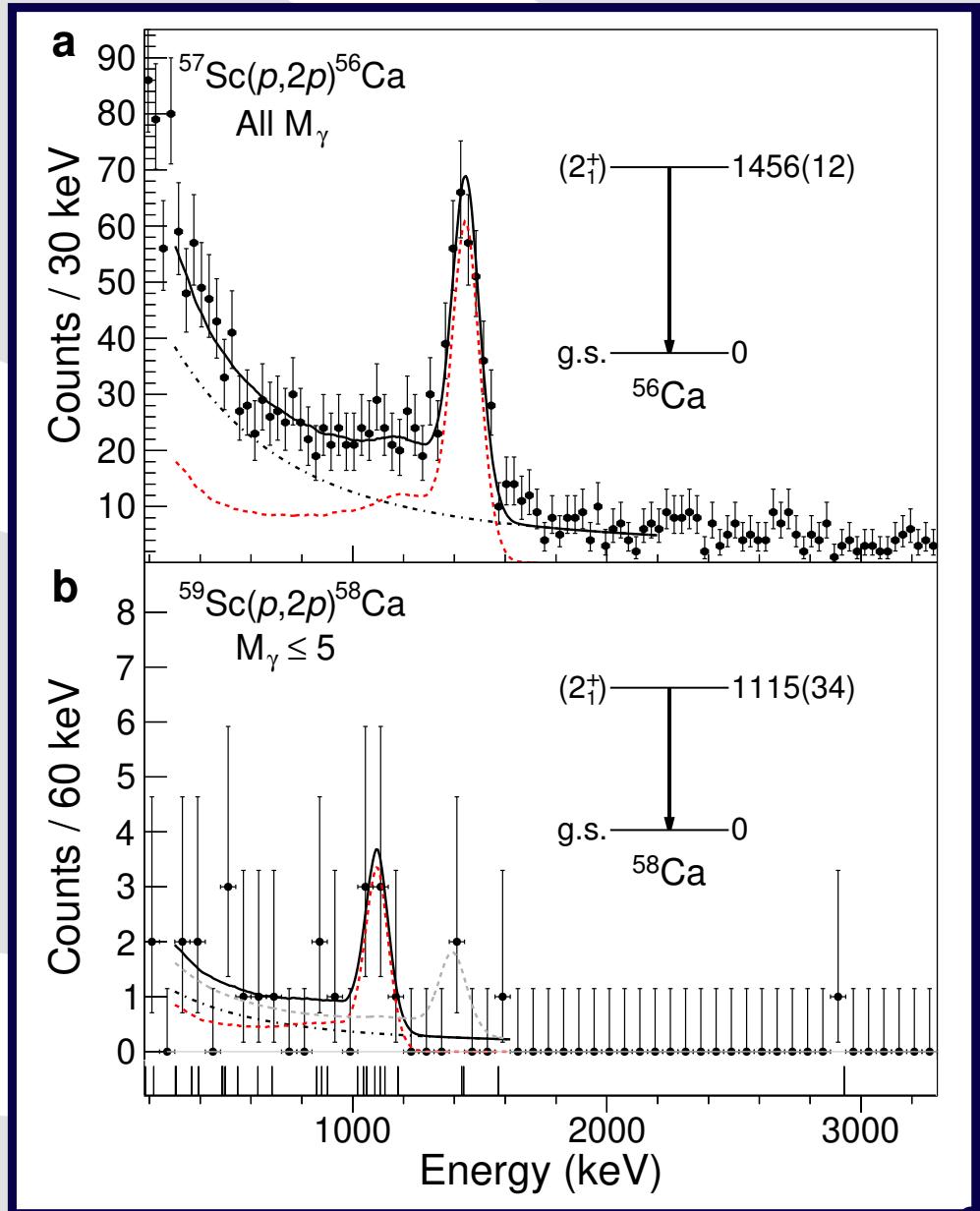
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# First Spectroscopy of $^{56,58}\text{Ca}$

# $E(2_1^+)$ Predictions in N-Rich Calcium Isotopes



# $E(2_1^+)$ in $^{56,58}\text{Ca}$ from $^{57}\text{Sc}(\text{p},2\text{p})^{56}\text{Ca}$ and $^{59}\text{Sc}(\text{p},2\text{p})^{58}\text{Ca}$

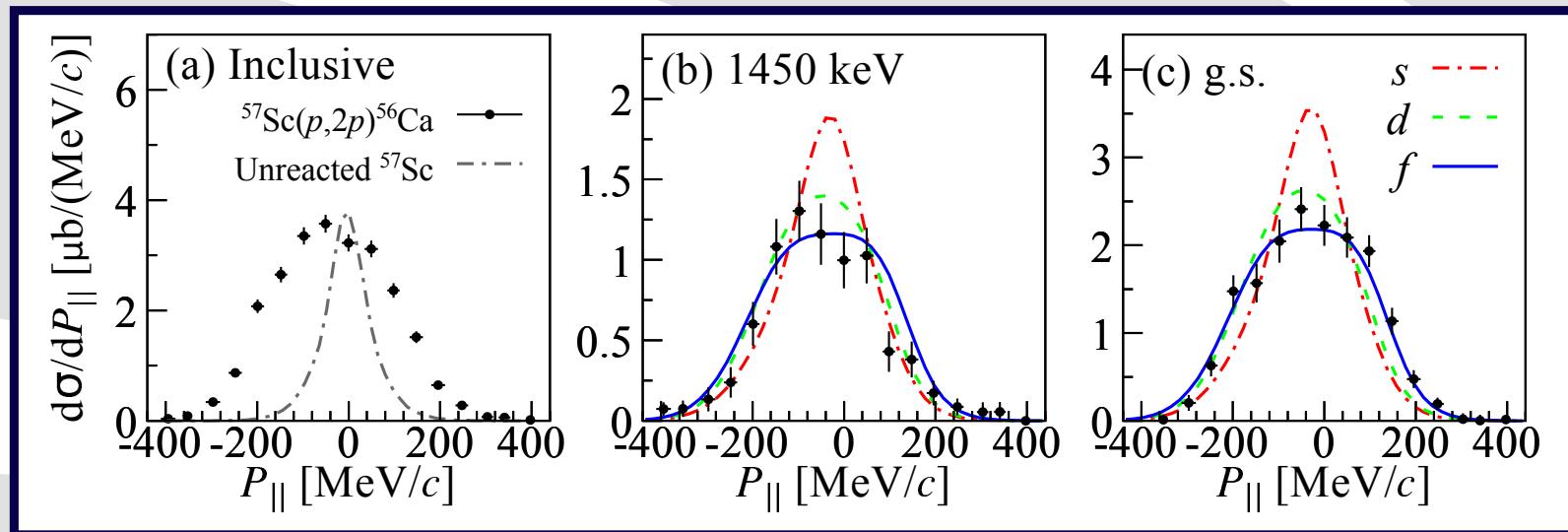


- 13.6 particles/s for  $^{57}\text{Sc}$
- 0.3 particles/s for  $^{59}\text{Sc}$
- $E(2_1^+)$  differ by  $\approx 440$  keV
- S.L. =  $2.8 \sigma$  for  $E(2_1^+)$  of  $^{58}\text{Ca}$
- particle hole symmetry of  $0f_{5/2}$
- ◆ if  $N = 40$  closed, constant energy expected
- ◆ (doubly)-magic  $^{60}\text{Ca}$  disfavored?
- Development of fitted interaction A3DA-t

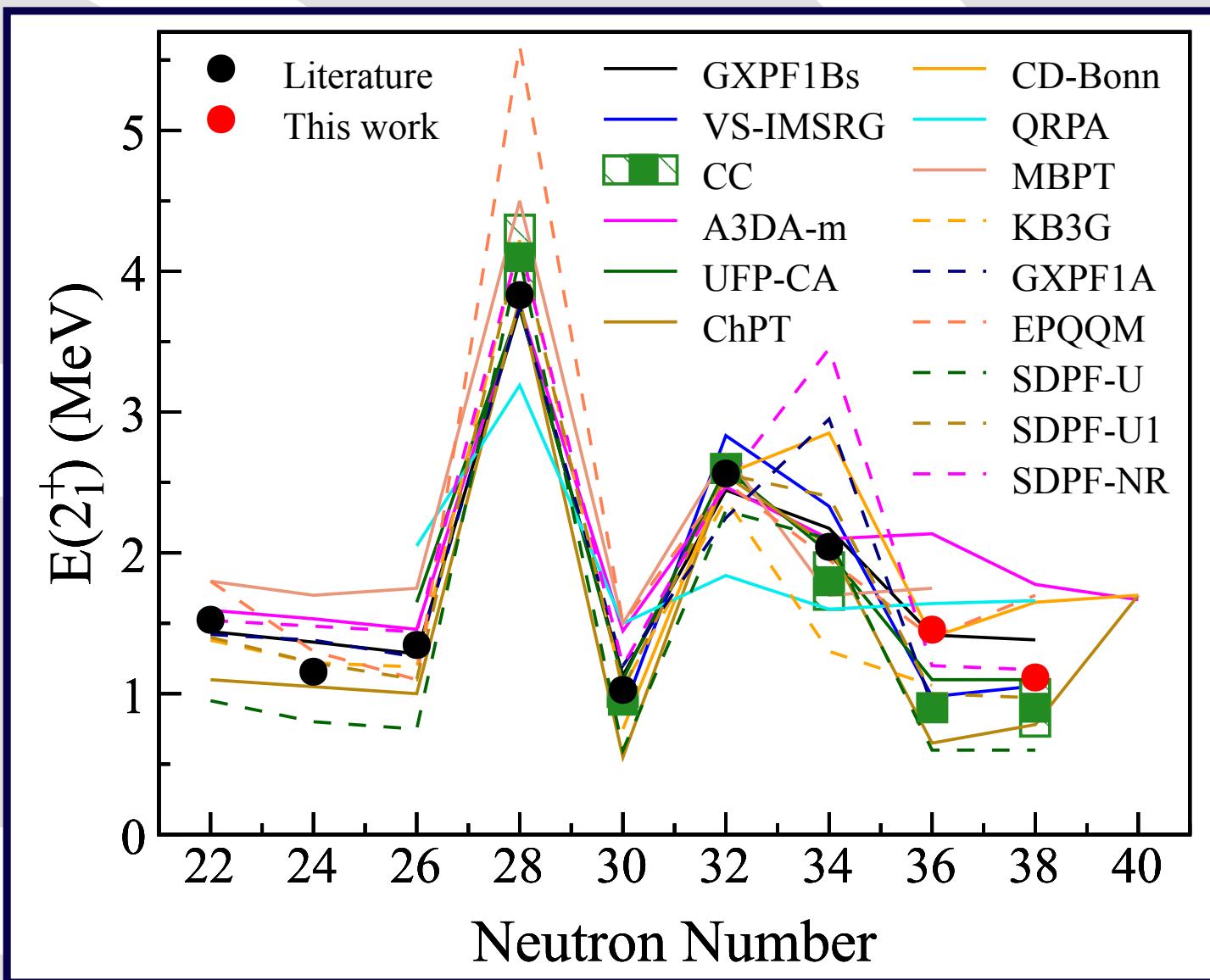
S. Chen, F. Browne et al., PLB 843 138025 (2023).

# $E(2_1^+)$ in $^{56,58}\text{Ca}$ from $^{57}\text{Sc}(p,2p)^{56}\text{Ca}$ and $^{59}\text{Sc}(p,2p)^{58}\text{Ca}$

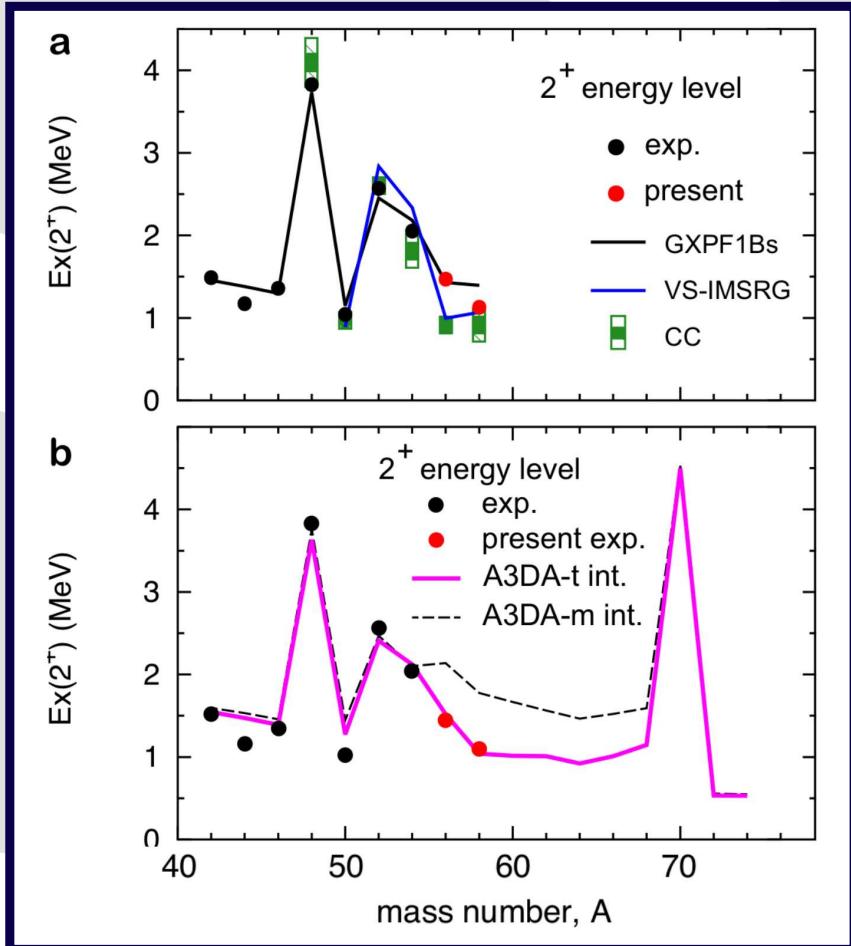
Experiment				DWIA	VS-IMSRG			GXPF1Bs			
	$E_{\text{exp}}$	$\sigma_{\text{exp}}$	$J^\pi$	$nl_j$	$\sigma_{\text{sp}}$	$E_x$	$C^2 S_{\text{th}}$	$\sigma_{\text{th}}$	$E_x$	$C^2 S_{\text{th}}$	
$^{56}\text{Ca}$	0	0.80(6)	$0_{\text{g.s.}}^+$	$0f_{7/2}$	1.80	0	0.61	1.10	0	0.69	1.24
	1456(12)	0.43(4)	$2_1^+$	$0f_{7/2}$	1.74	1002	0.29	0.50	1416	0.25	0.44
			$4_1^+$	$0f_{7/2}$	1.73	1307	0.05	0.09	1776	0.02	0.04
	Inclusive	1.23(5)						1.69			1.72
$^{58}\text{Ca}$	0	0.66(24)	$0_{\text{g.s.}}^+$	$0f_{7/2}$	1.58	0	0.80	1.26	0	0.83	1.31
	1115(34)	0.47(19)	$2_1^+$	$0f_{7/2}$	1.54	1075	0.16	0.25	1382	0.15	0.23
			$4_1^+$	$0f_{7/2}$	1.52	1423	0.001	0.002	1772	0.001	0.002
	Inclusive	1.14(15)						1.51			1.54



# $E(2_1^+)$ Predictions in N-Rich Calcium Isotopes

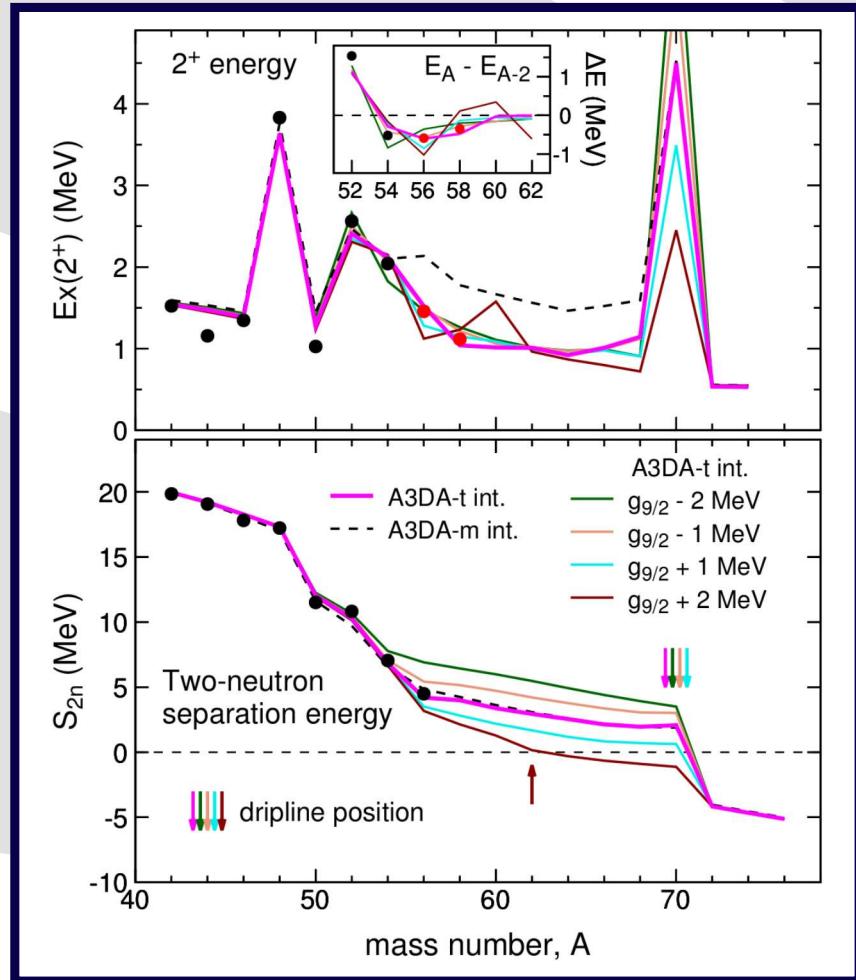


# First Spectroscopy of $^{56,58}\text{Ca}$



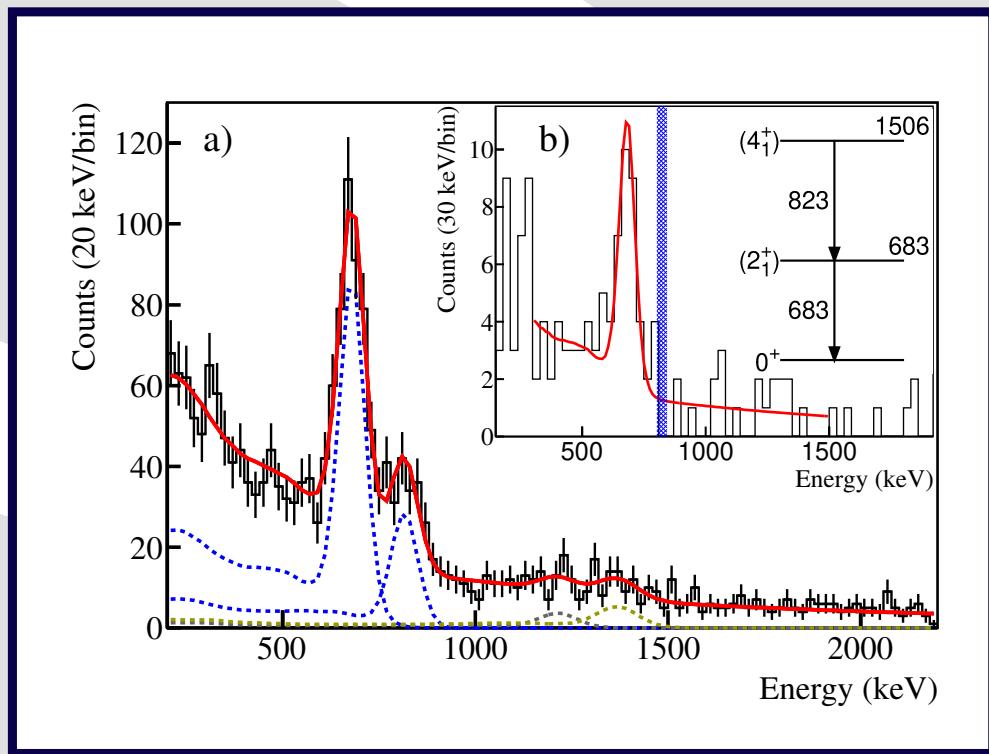
- GXPF1Bs:  
Shell-model  
neutron  $p\,f$  shell
- VS-IMSRG:  
Valence-space in-medium similarity  
renormalization group  
1.8/2.0 (EM) interaction  
neutron  $p\,f$  shell
- CC: Coupled-cluster theory  
Two-particle removed/attached  
equation-of-motion (2PR/2PA-EOM)
- A3DA-t: Revision of A3DA-m interaction  
fitted to existing  $E(2_1^+)$  and  $S_{2n}$  data  
Neutron  $p\,f - g_{9/2}d_{5/2}$  orbitals

# First Spectroscopy of $^{56,58}\text{Ca}$



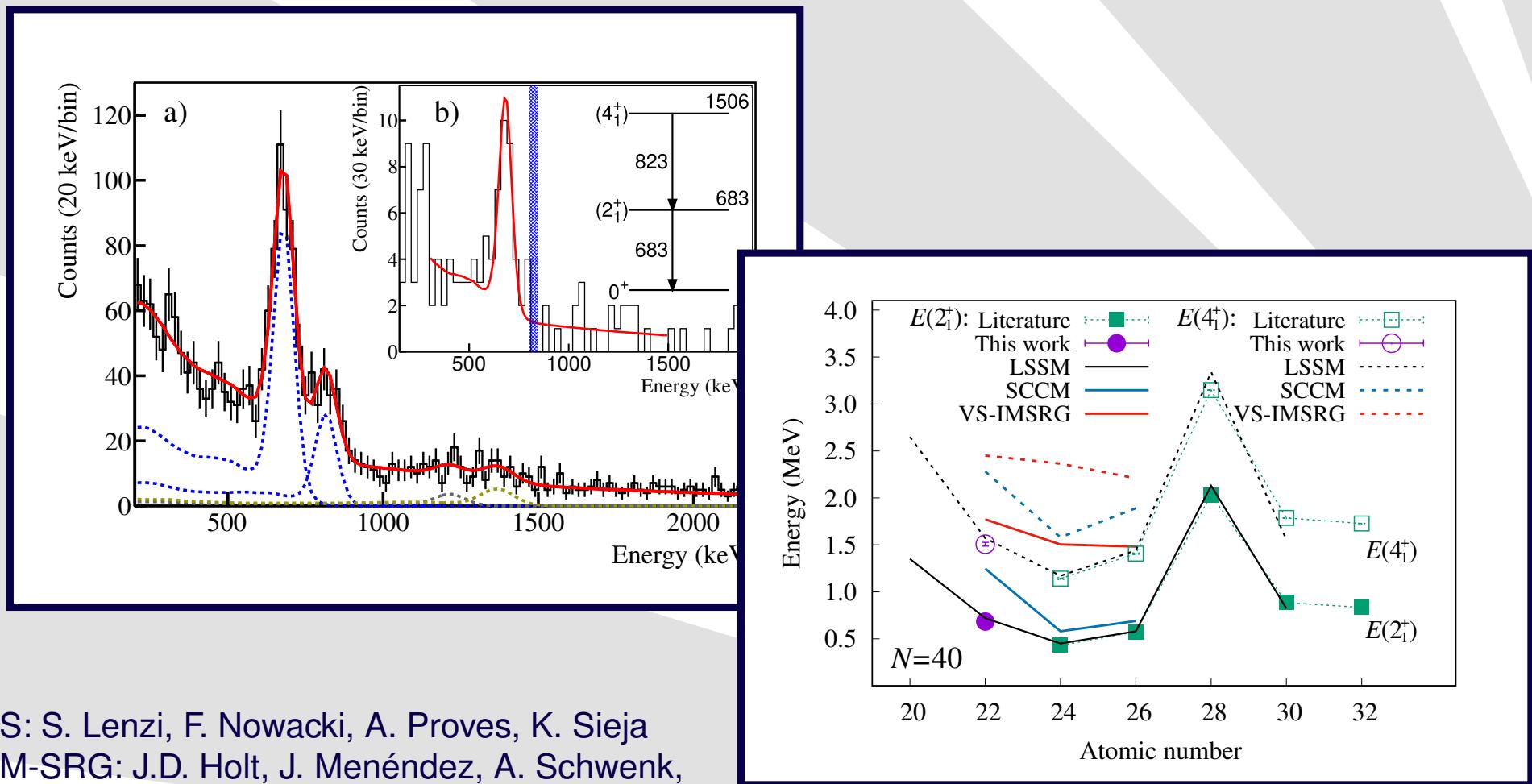
- Predictions with A3DA-T
- Sensitivity of the neutron  $0g_{9/2}$  SPE  
→ variation of up to  $\pm 2$  MeV
  - ◆ Positive shifts of  $0g_{9/2}$  SPE  
→ low  $E(2_1^+)$  and  $S_{2n}$  of  $^{56}\text{Ca}$
  - ◆ Negative shifts of  $0g_{9/2}$  SPE  
→ quenching of  $N = 34$  shell gap

# N = 40 Structure towards $^{60}\text{Ca}$ : $^{63}\text{V}(\text{p},2\text{p})^{62}\text{Ti}$



M.L. Cortés, W. Rodriguez et al., Phys. Lett. B 800, 135071 (2020).

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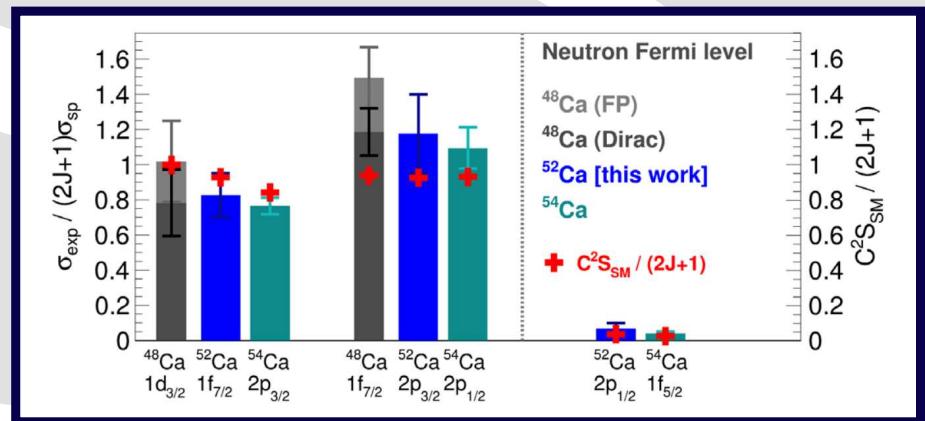
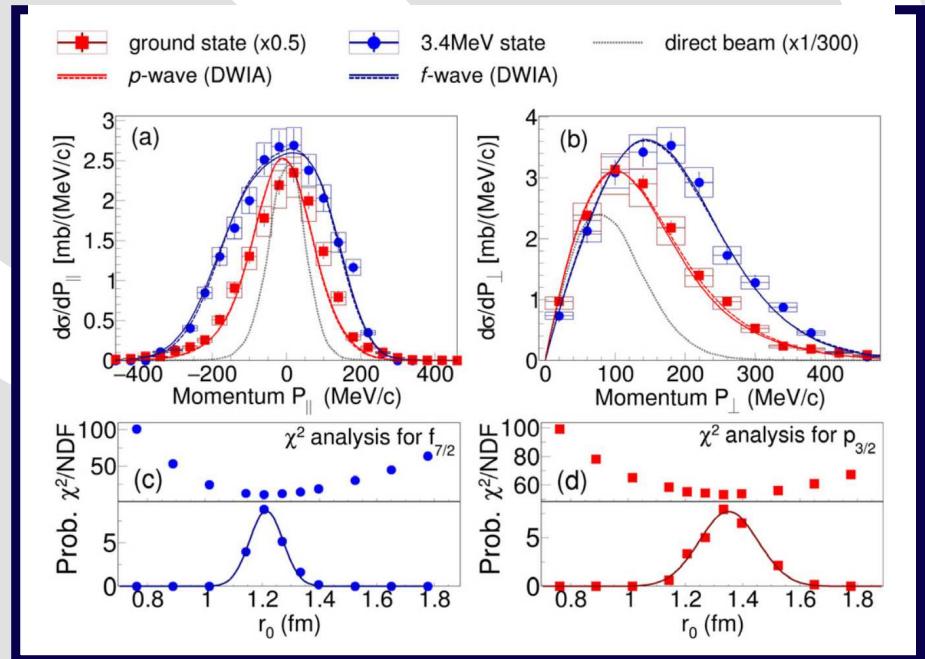
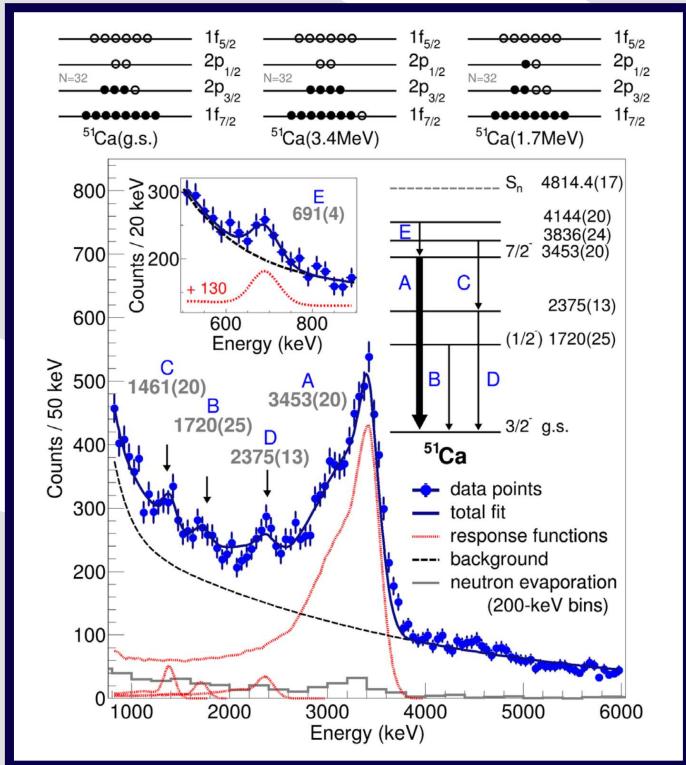
LNPS: S. Lenzi, F. Nowacki, A. Proves, K. Sieja  
 VS-IM-SRG: J.D. Holt, J. Menéndez, A. Schwenk,  
 J. Simonis, S.R. Stroberg  
 SCCM: T. Rodriguez

M.L. Cortés, W. Rodriguez et al., Phys. Lett. B 800, 135071 (2020).



# Structure of Odd Ca Isotopes $^{51,53,55}\text{Ca}$

# The $^{52}\text{Ca}(\text{p},\text{pn})^{51}\text{Ca}$ Reaction: Extended $1p_{3/2}$ Orbital and the $N = 32$ Shell Closure



- J. Bonnard et al., PRL 116, 212501 (2016):  
0.7 fm size difference between  $1p_{3/2}$  and  $0f_{7/2}$
- Experimentally deduced 0.61(23) fm
- Level energies known from  
M. Rejmund et al. PRC 76, 021304(R) (2007)
- 0.6(3) mbarn cross section to state at 1720 keV

M. Enciu, H. Liu et al., PRL 129, 262501 (2022).



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# Summary



# Summary

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- Ca isotopes ideal benchmark for nuclear structure and reaction theories
- Obtained comprehensive data set in n-rich nuclei around  $Z = 20$ 
  - ◆ Spectroscopy of  $^{51-58}\text{Ca}$
  - ◆ Many other isotopes
- $N = 32, 34$  magic numbers
  - ◆  $N = 32, 34$  shell closures as strong as  $N = 28$
  - ◆ Large rms radius for  $1p_{3/2}$  orbital
- Approaching  $^{60}\text{Ca}$ 
  - ◆ Effective interaction LNPS reproduces  $E(2_1^+)$ ,  $E(4_1^+)$  along  $N = 40$
  - ◆  $E(2_1^+)$  in Ca isotopes challenge theory
- Single particle strengths
  - ◆ Pure  $0f_{7/2}$  strength in  $^{52,54}\text{Ca}$
  - ◆ Marginal occupation of  $1p_{1/2}$  in  $^{52}\text{Ca}$  and of  $0f_{5/2}$  in  $^{54}\text{Ca}$



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# Thank You!



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# Backup slides