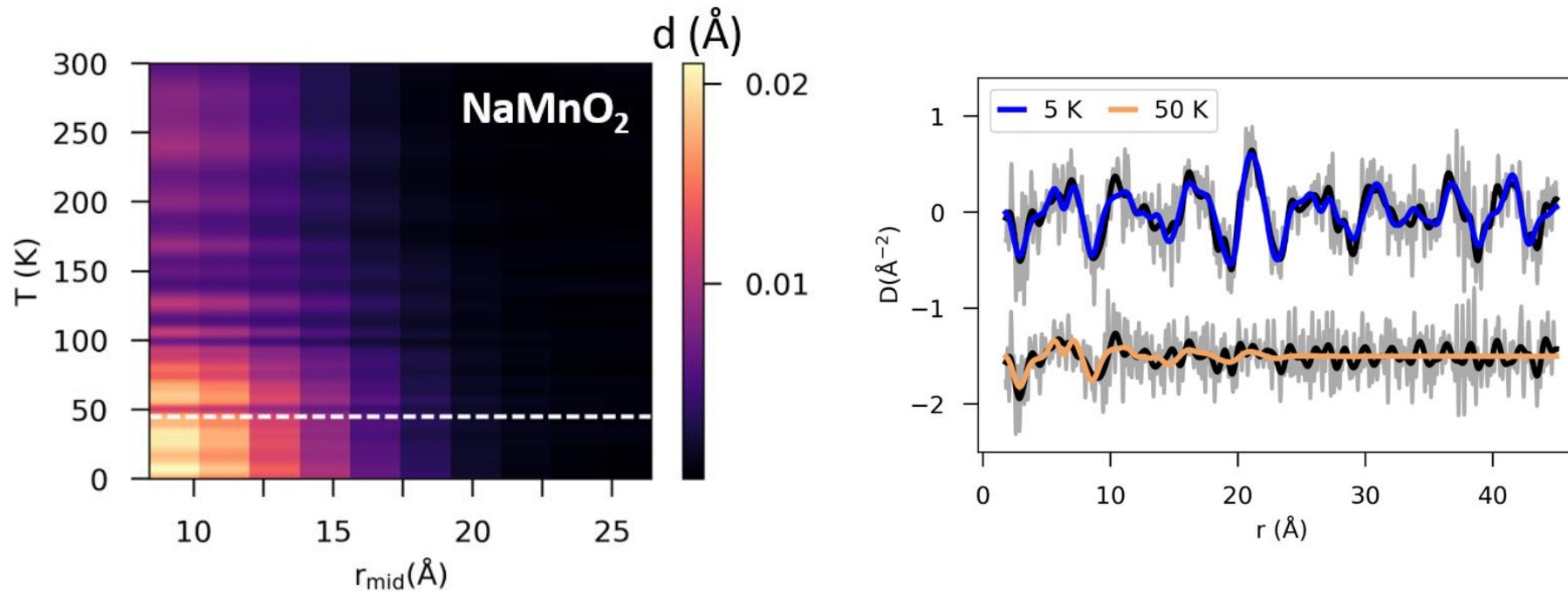


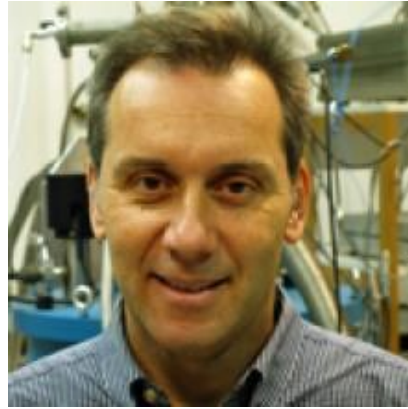
Nanoscale degeneracy lifting in triangular antiferromagnets studied by combined PDF+mPDF



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- Dave Keen (ISIS/RAL)
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Reference: Frandsen, Bozin, Lappas, et al; under review.

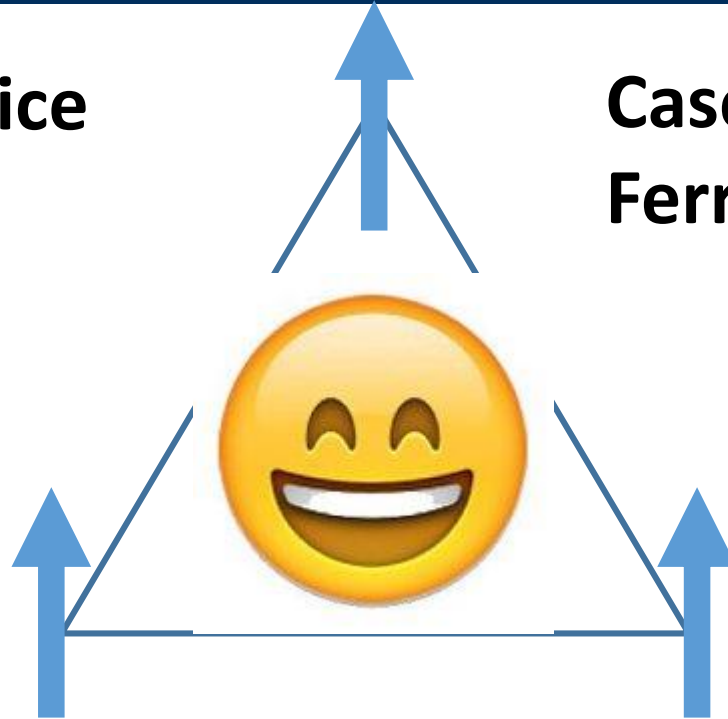


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Geometrically Frustrated Magnetism

Spins on a triangular lattice

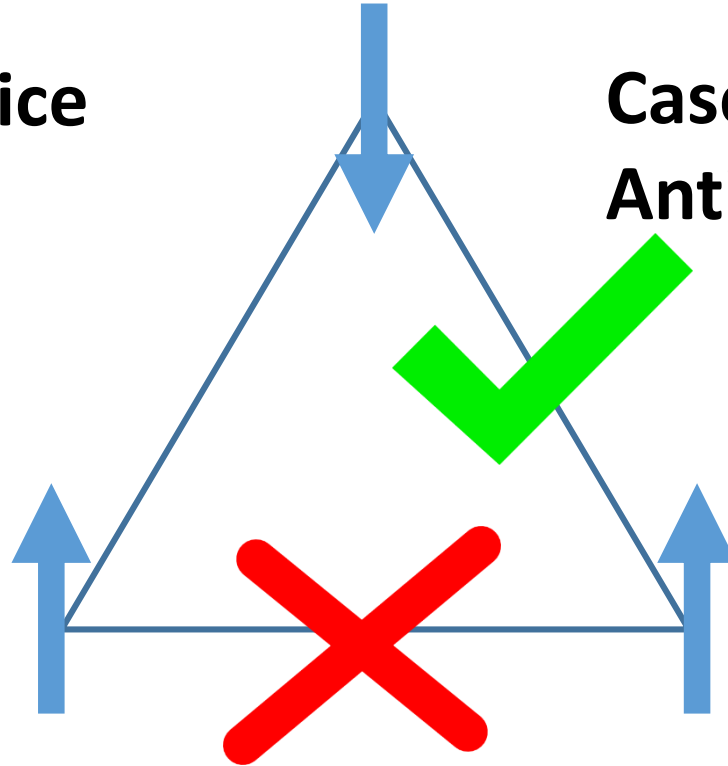
**Case 1:
Ferromagnetic interactions**



Geometrically Frustrated Magnetism

Spins on a triangular lattice

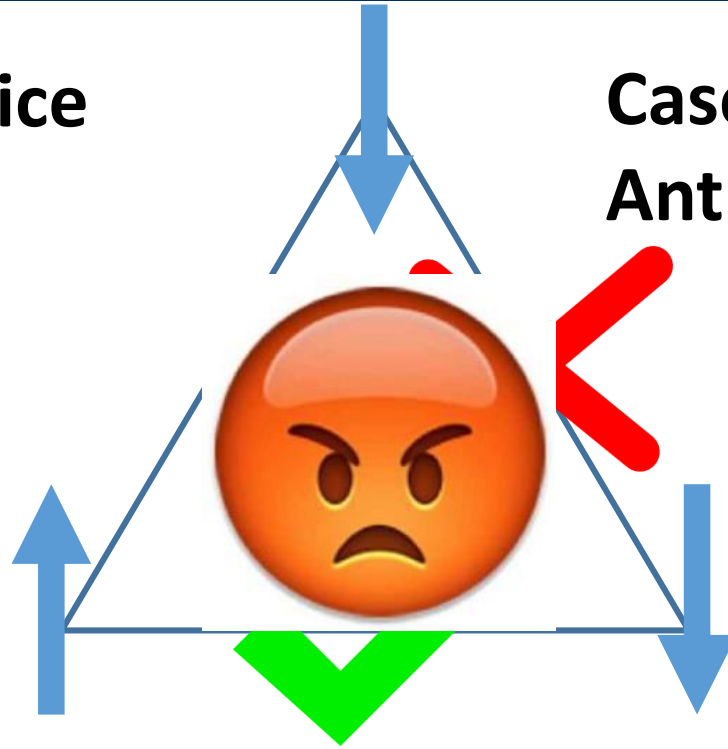
Case 2:
Antiferromagnetic interactions



Geometrically Frustrated Magnetism

Spins on a triangular lattice

**Case 2:
Antiferromagnetic interactions**

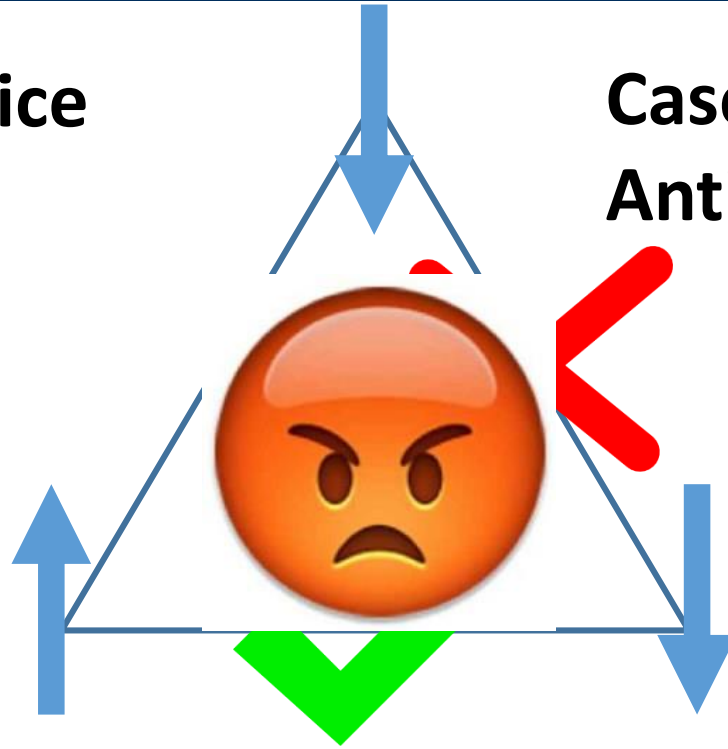


Geometrically frustrated magnets: The geometry of the lattice prevents competing magnetic interactions from being simultaneously satisfied, often with surprising consequences!

Geometrically Frustrated Magnetism

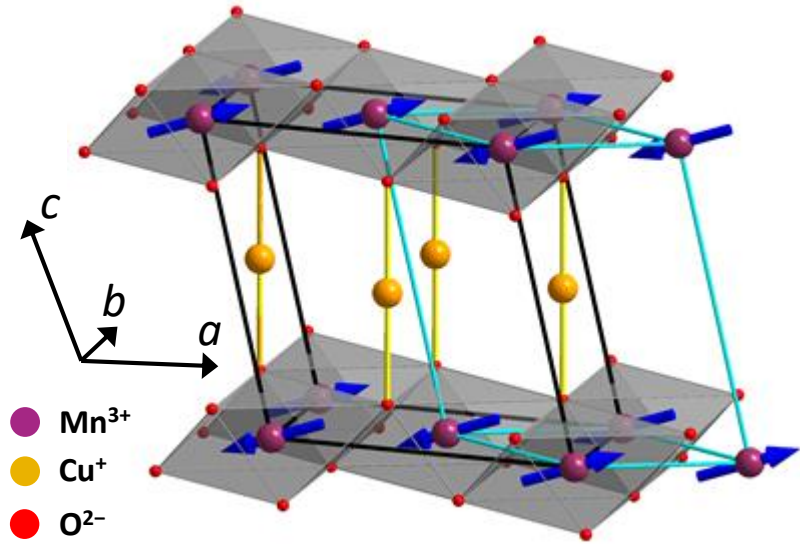
Spins on a triangular lattice

**Case 2:
Antiferromagnetic interactions**

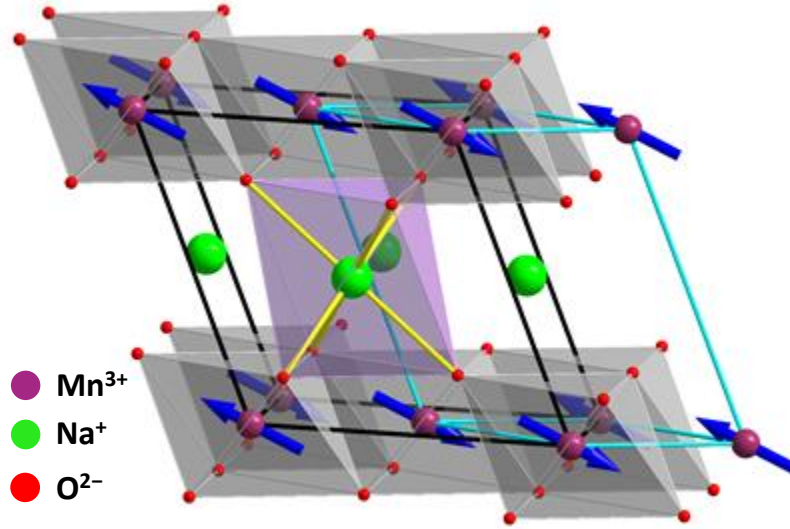


Macroscopic ground-state degeneracy; ground states lacking long-range order; quantum spin liquids; unconventional transition mechanisms; extreme sensitivity to perturbations

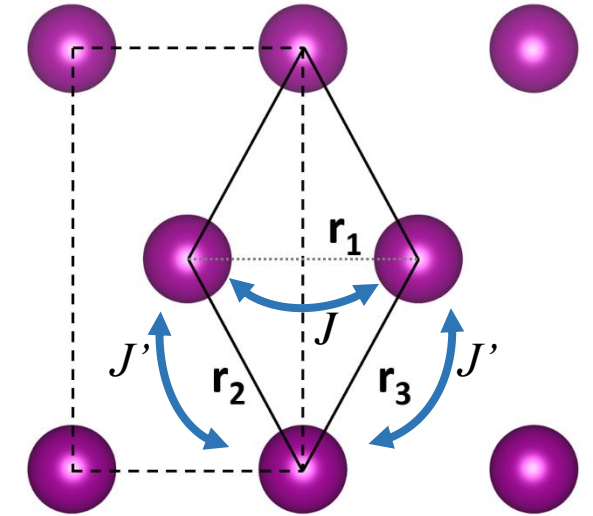
CuMnO₂ and NaMnO₂: Case studies of frustrated magnetism in strongly correlated TMOs



CuMnO₂



NaMnO₂

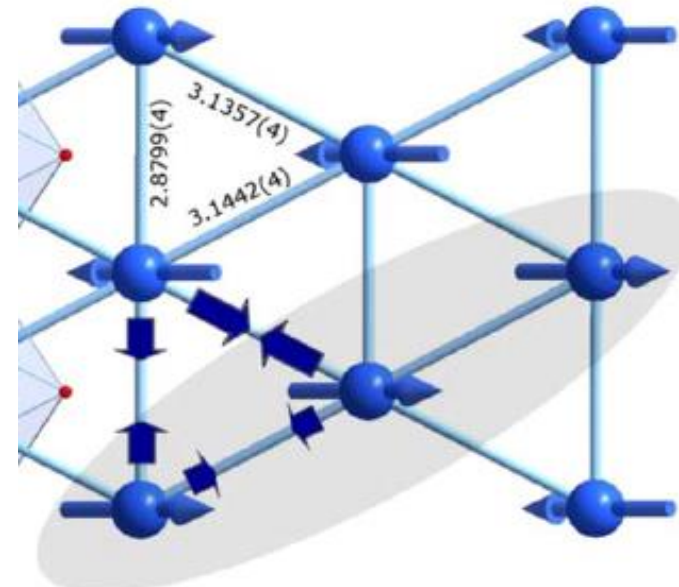
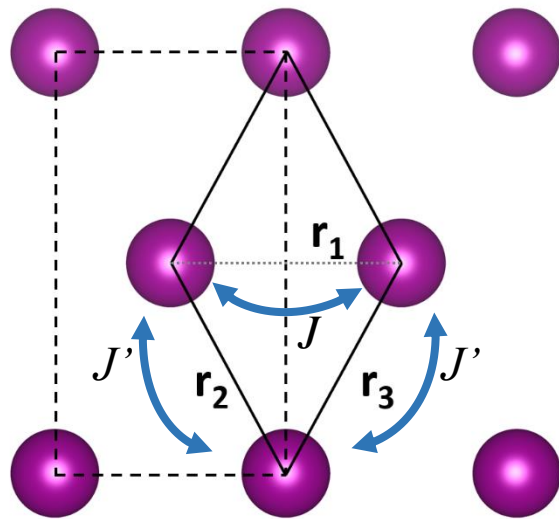


- Triangular network of Mn³⁺ S = 2 spins hosted by monoclinic lattice
- Geometrical frustration is partially relieved at ambient conditions
 - $r_1 < r_2 = r_3$
 - $J'/J = 0.27$ for Cu, 0.44 for Mn
- Both achieve long-range antiferromagnetic order ($T_N = 65$ K for Cu, 45 K for Na)
- Transition mechanisms show interesting differences

Achieving LRO in CuMnO_2

A conventional magnetoelastic mechanism leads to long-range AF order in CuMnO_2

- Monoclinic-to-triclinic structural phase transition further distorts the triangles such that $r_1 < r_2 < r_3$, fully lifting the degeneracy
- AF alignment along short bonds, ferro alignment along long bond



Damay et al, *PRB* **80**, 094410 (2009)



How about NaMnO_2 ?

Long-range AF order occurs below $T_N = 45$ K, but no long-range structural transition occurs.

By what mechanism is the triangular degeneracy lifted if the average structure remains monoclinic at all temperatures?

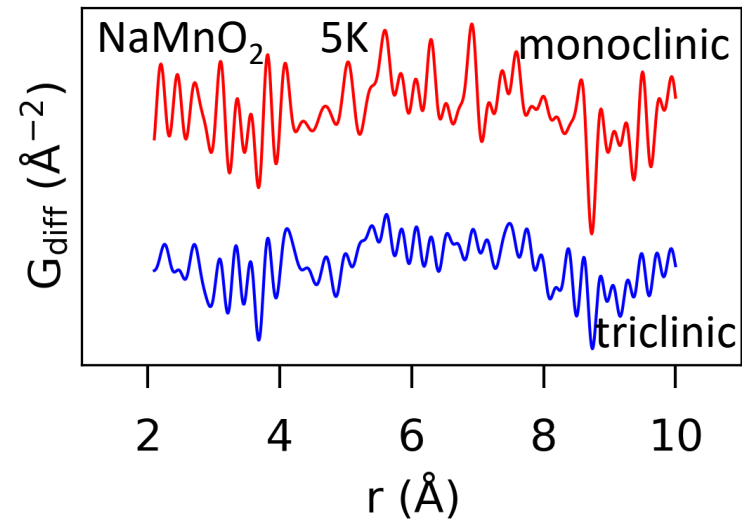
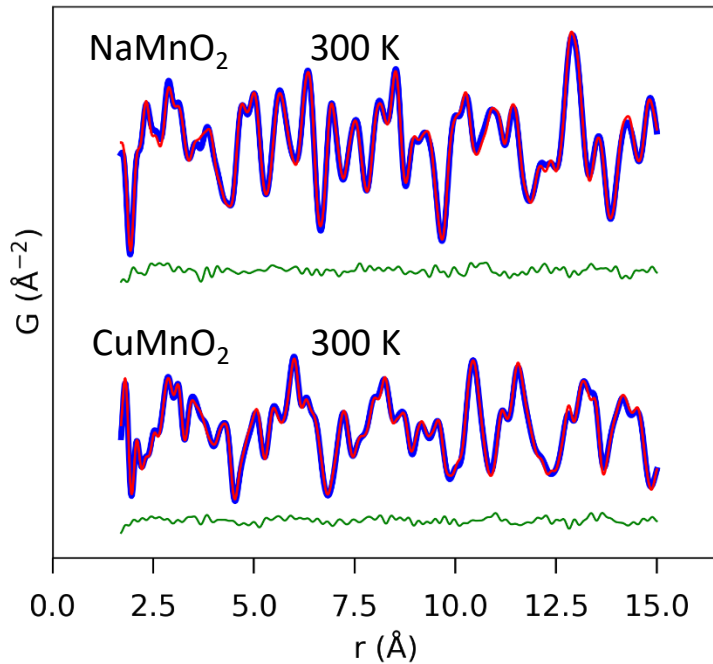
Potentially relevant experimental facts:

- Strong diffuse magnetic scattering survives into the paramagnetic state
- Bragg peaks show subtle anisotropic broadening at low T
- Significant disorder in the form of Na vacancies and planar defects

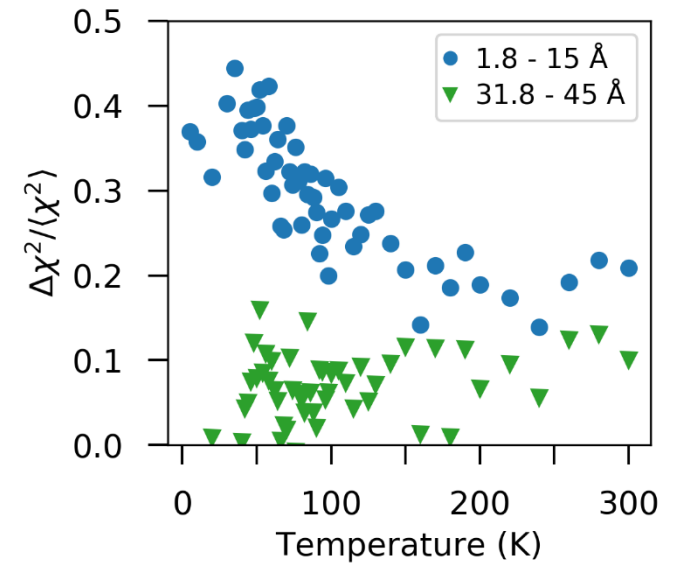
Perhaps PDF can solve the riddle!



Results of atomic PDF analysis



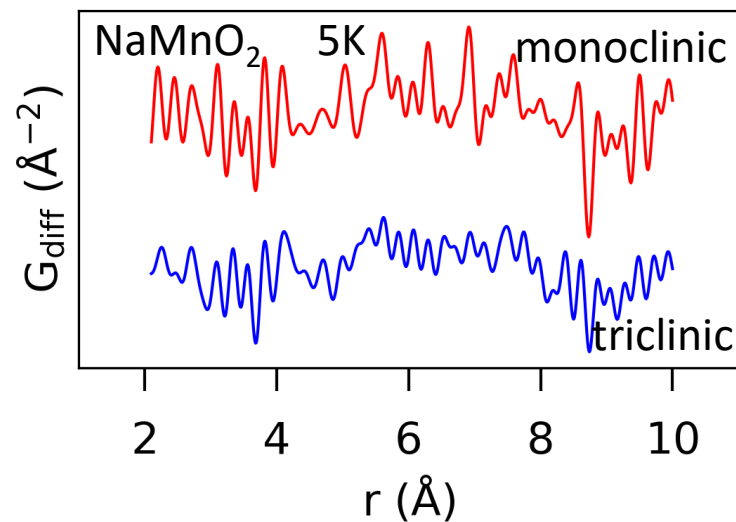
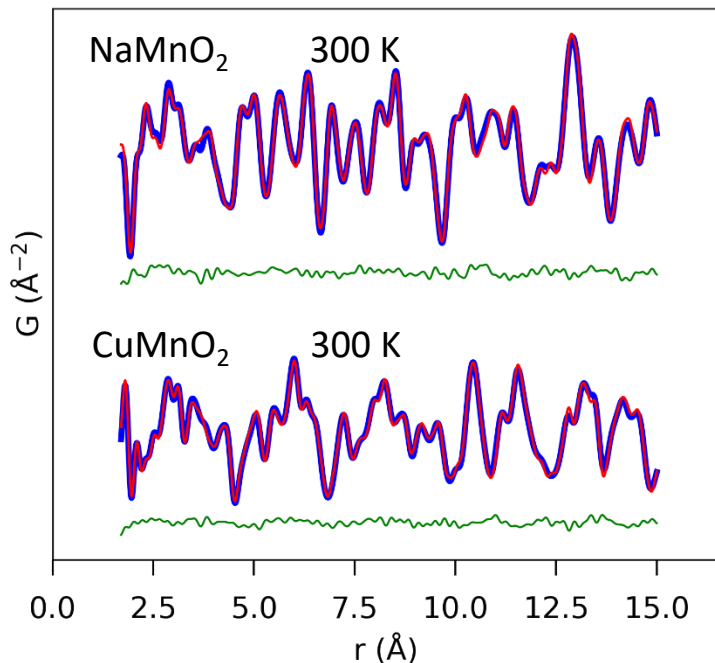
Triclinic model is significantly better



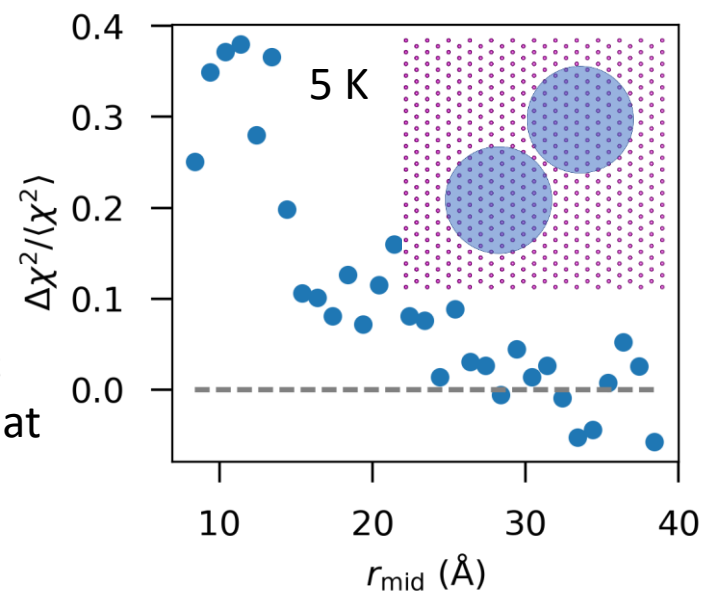
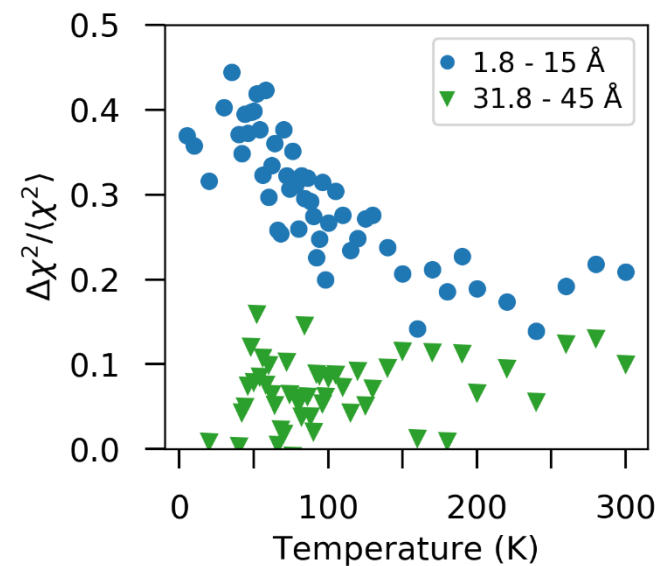
$$\frac{\chi_{\text{mono}}^2 - \chi_{\text{tri}}^2}{\frac{1}{2}(\chi_{\text{mono}}^2 + \chi_{\text{tri}}^2)}$$



Results of atomic PDF analysis



Triclinic model is significantly better



$$r_1 < r_2 < r_3$$

Benefit of triclinic model is greatest at low r and low T .

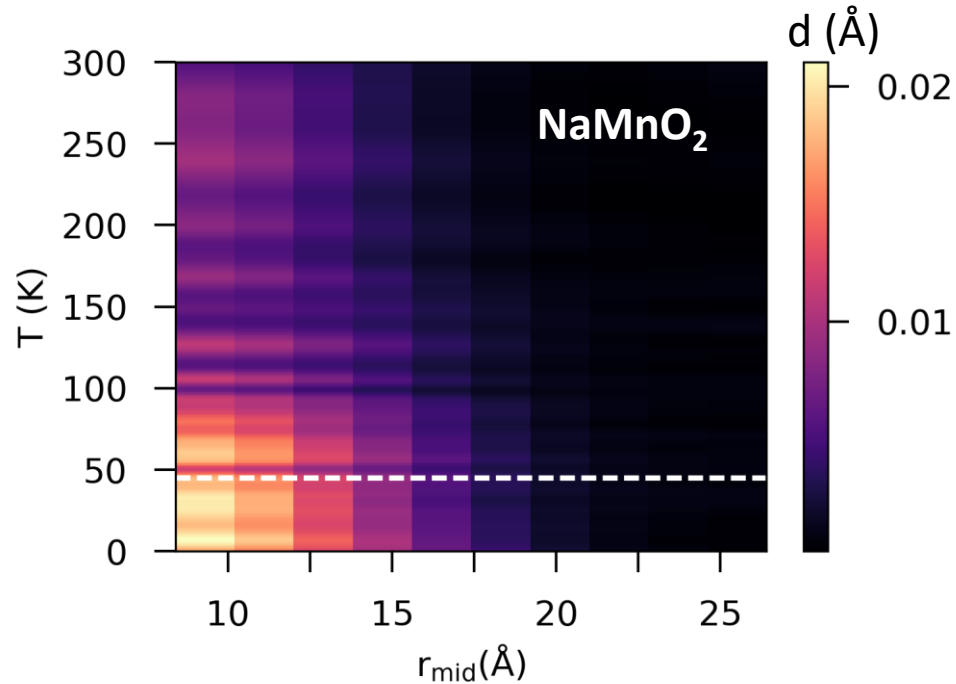
Local structure of NaMnO₂ is triclinically distorted, despite persistence of monoclinic symmetry in the average structure.



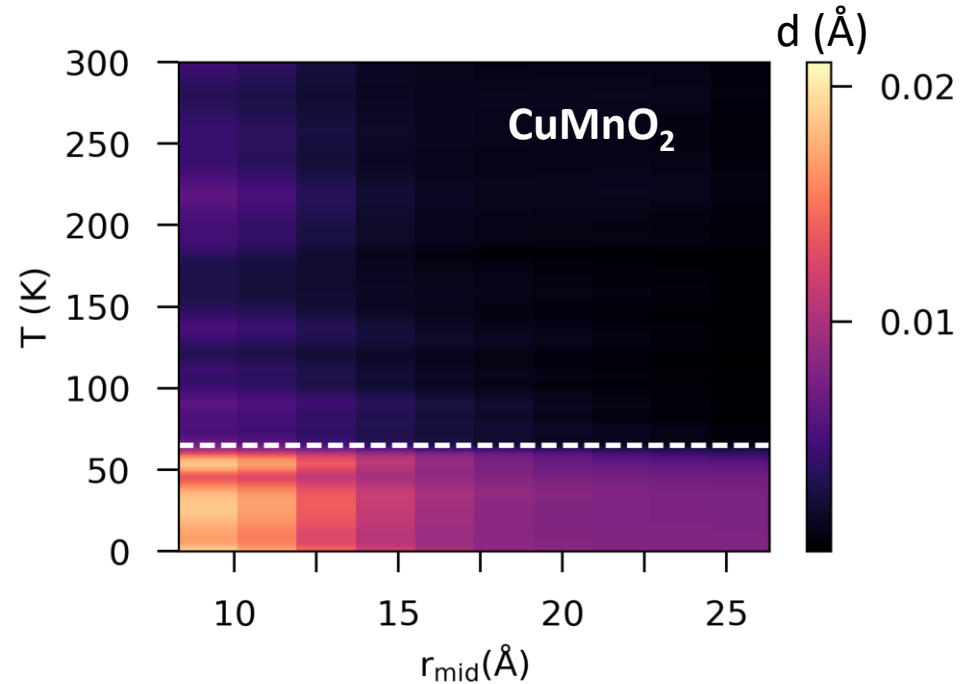
Comprehensive r - and T -dependent fits

- Boxcar fits using the monoclinic and triclinic models were carried out on a dense r and T grid
- Triclinic splitting $d = r_2 - r_3$ extracted from each refinement

Lifts degeneracy of isosceles triangles



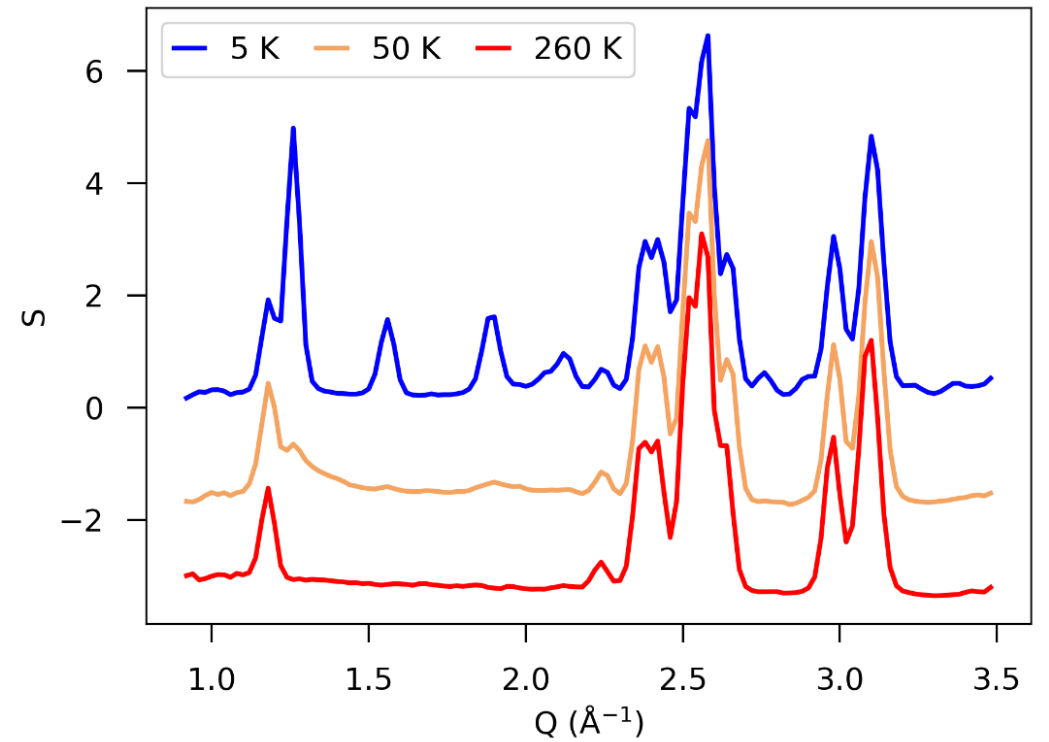
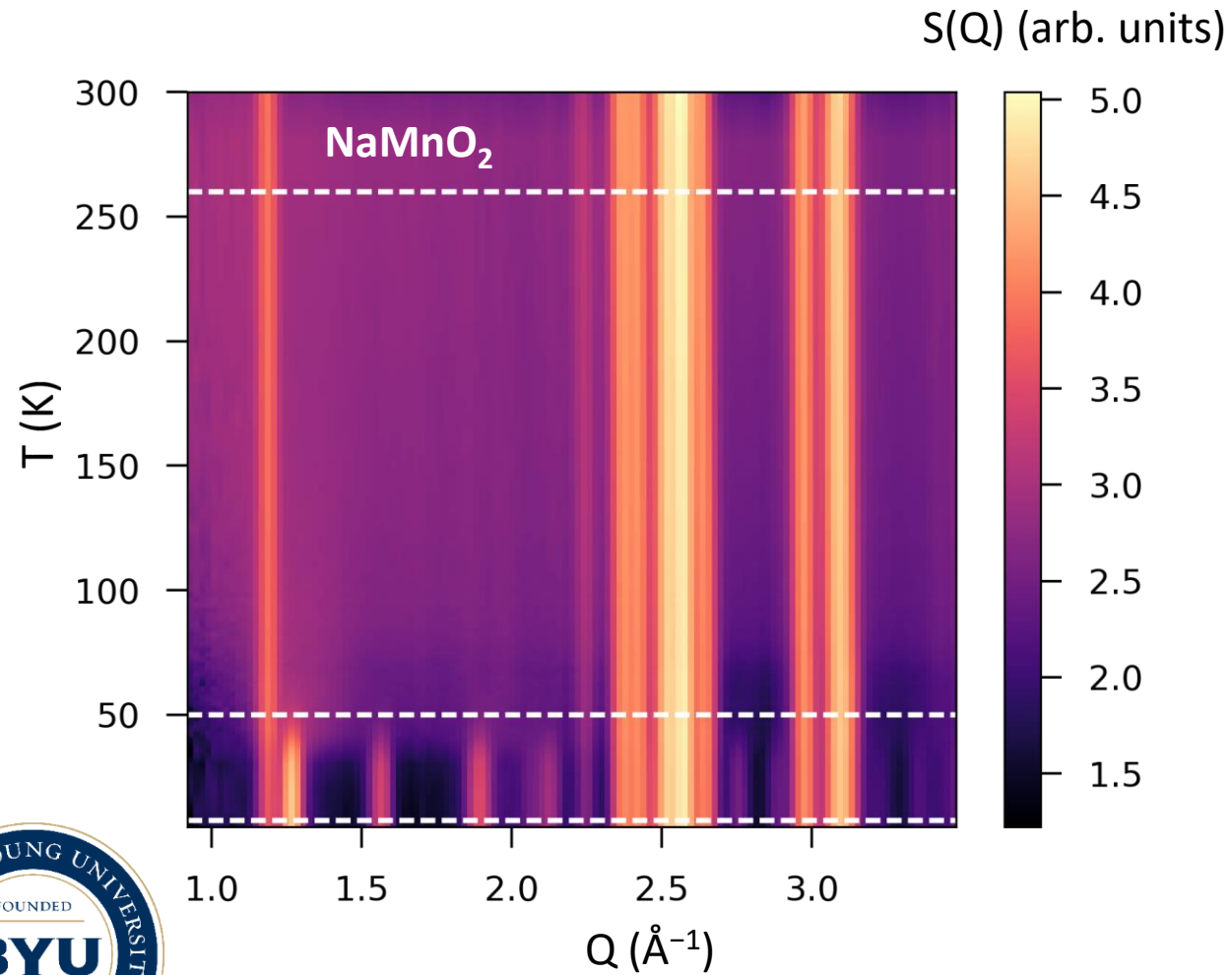
Short-range triclinic distortion on a ~ 2 nm length scale that grows at low T



Enhanced triclinic splitting at low r , weak local triclinicity above T_N



Investigating the local magnetic structure



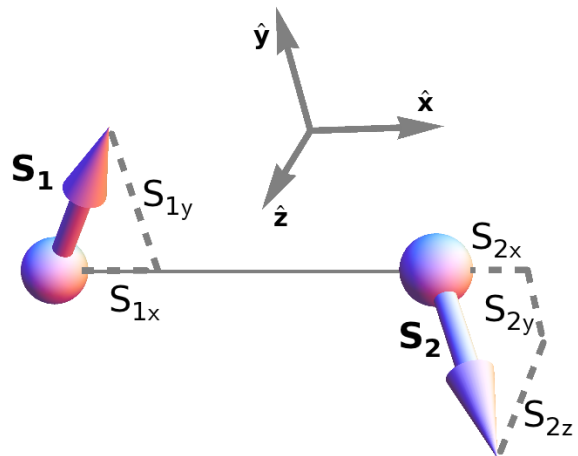
Magnetic PDF

ATOMIC
$$f(r) = \frac{1}{N \langle b \rangle^2} \sum_{i \neq j} \frac{b_i b_j}{r} \delta(r - r_{ij})$$

MAGNETIC
$$f(r) = \frac{1}{N} \frac{3}{2S(S+1)} \sum_{i \neq j} \left(\frac{A_{ij}}{r} \delta(r - r_{ij}) + B_{ij} \frac{r}{r_{ij}^3} \Theta(r_{ij} - r) \right)$$

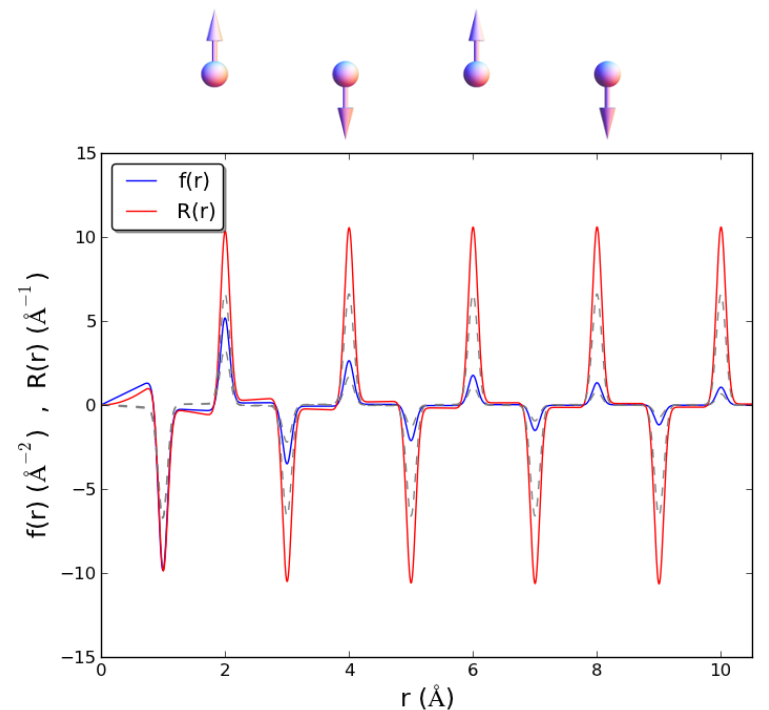
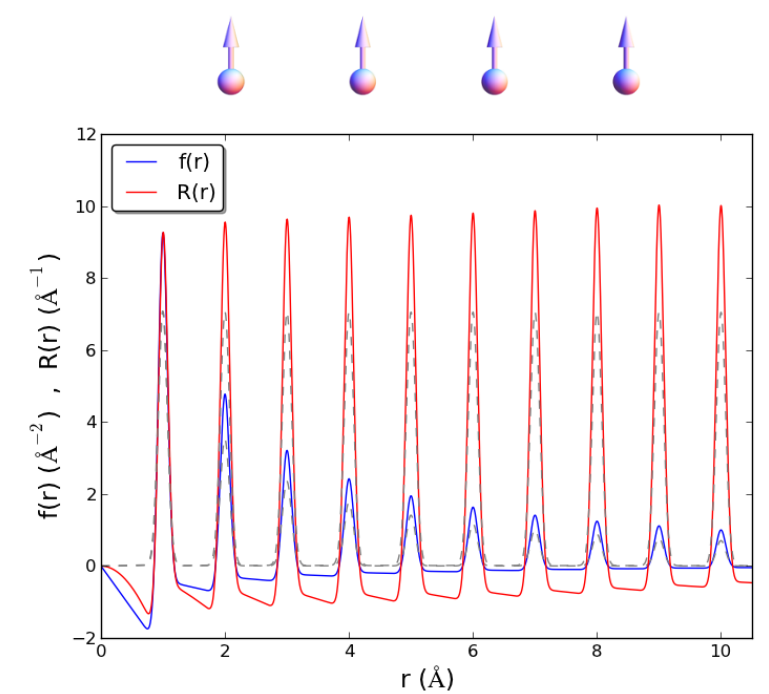
$$A_{ij} = S_i^y S_j^y$$

$$B_{ij} = 2S_i^x S_j^x - S_i^y S_j^y$$

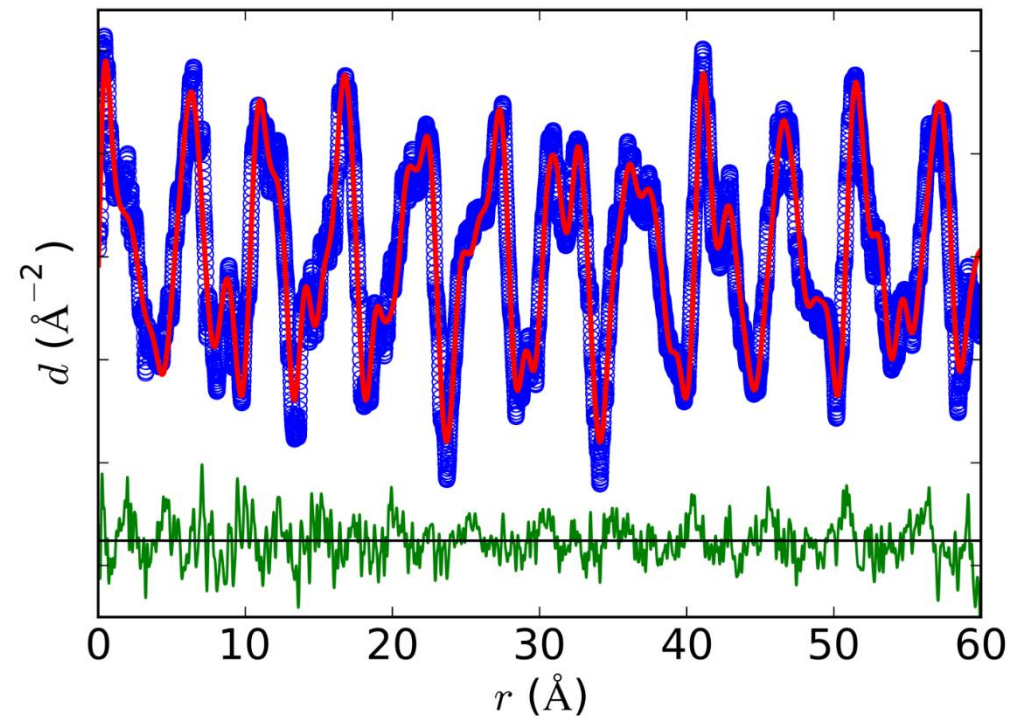
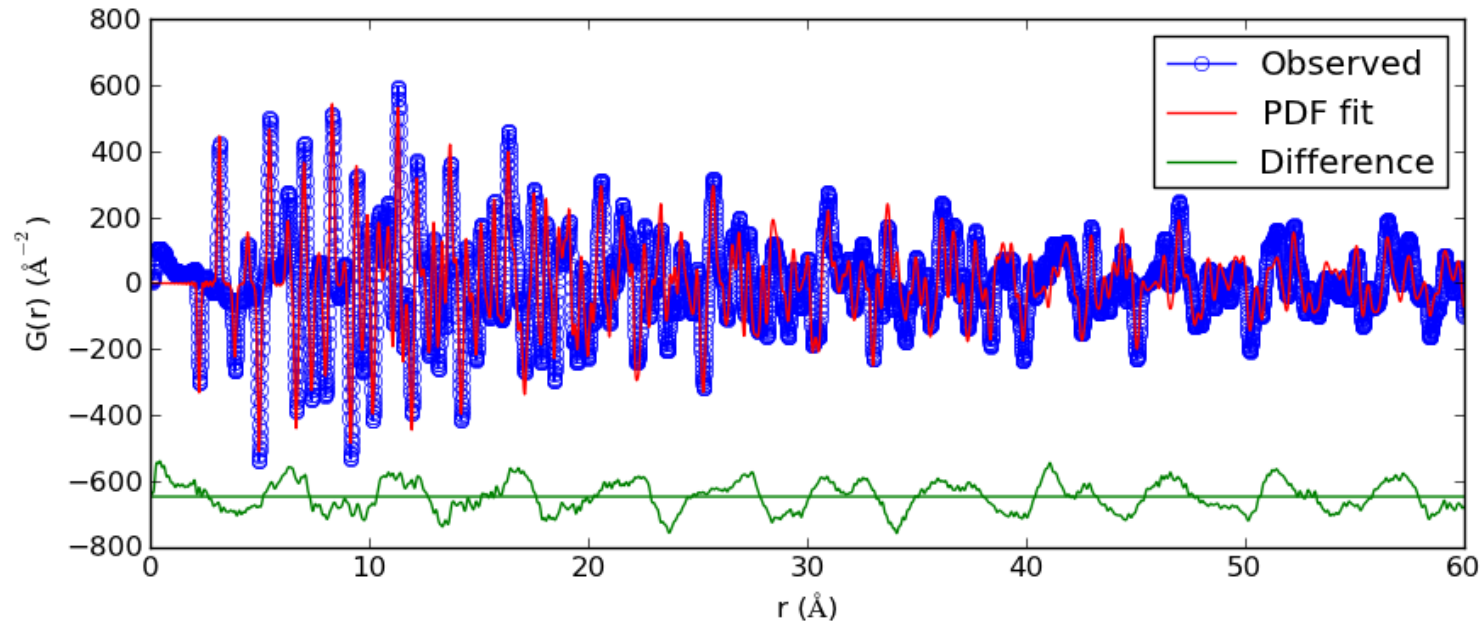


Positive peaks for
ferromagnetic correlations

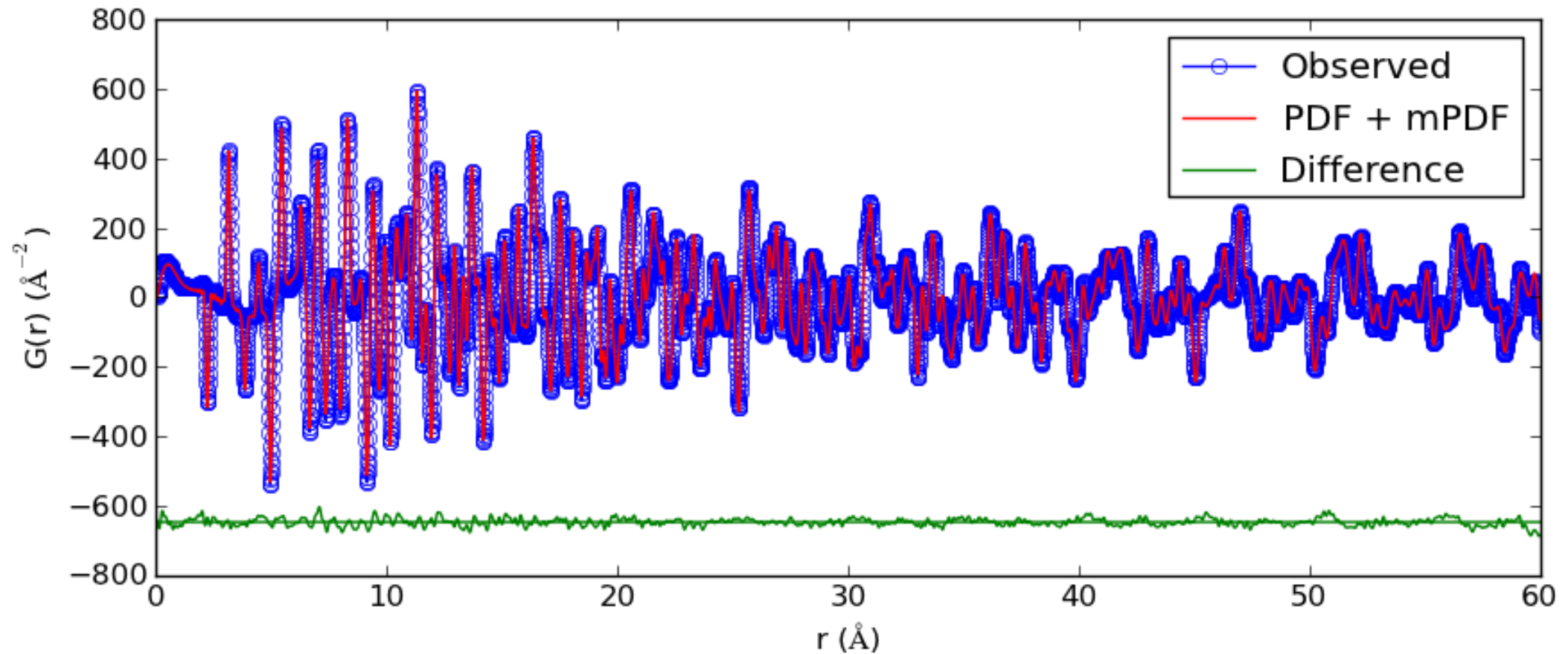
Negative peaks for
antiferromagnetic correlations



Example: Antiferromagnetic MnO



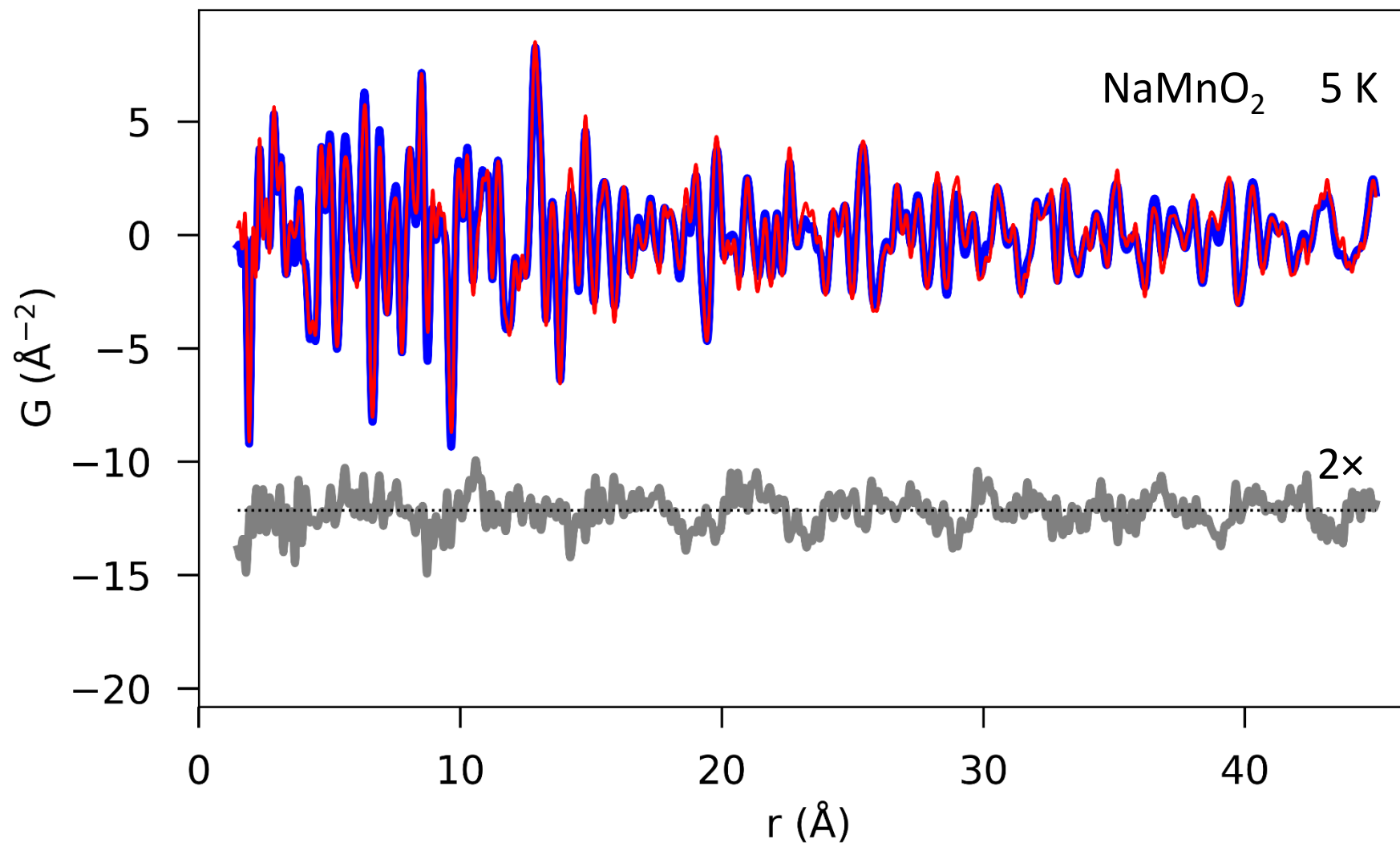
Example: Antiferromagnetic MnO



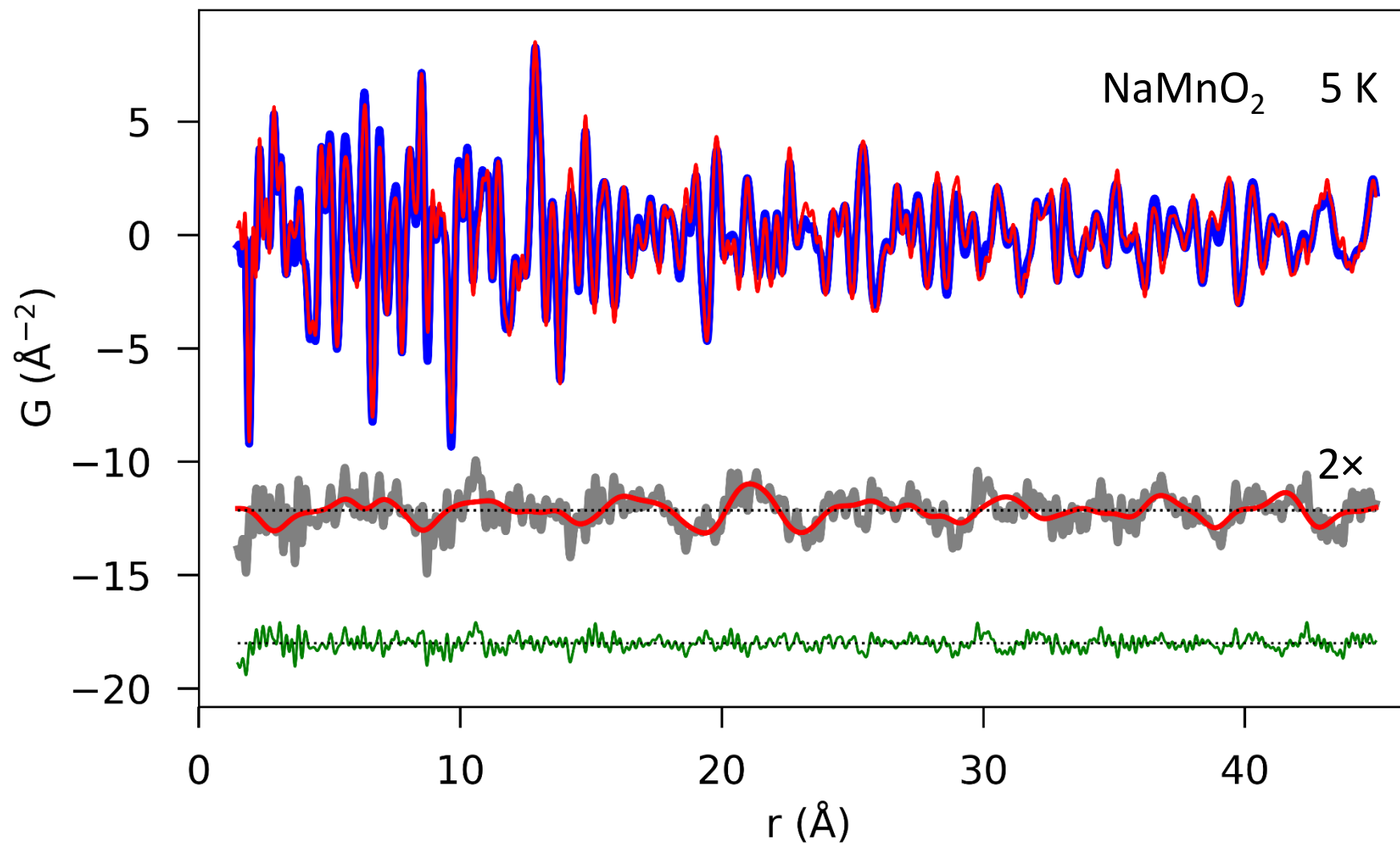
Total PDF fit (atomic + magnetic)



Magnetic PDF refinements for NaMnO₂



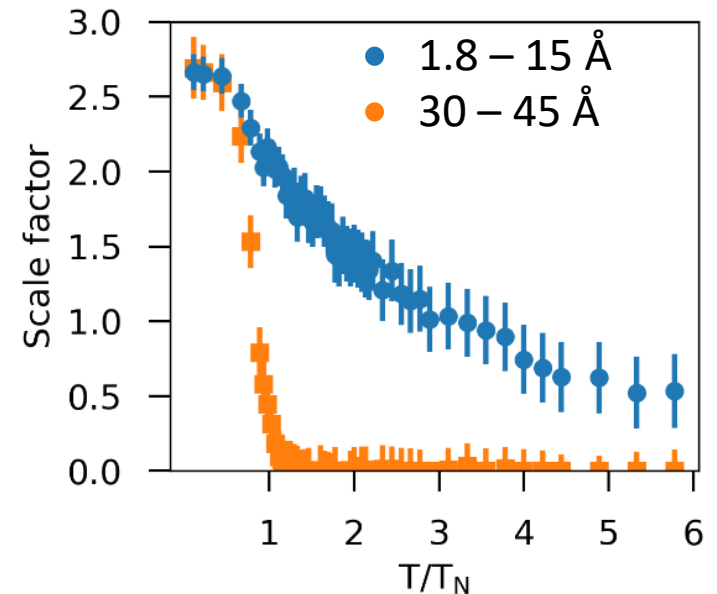
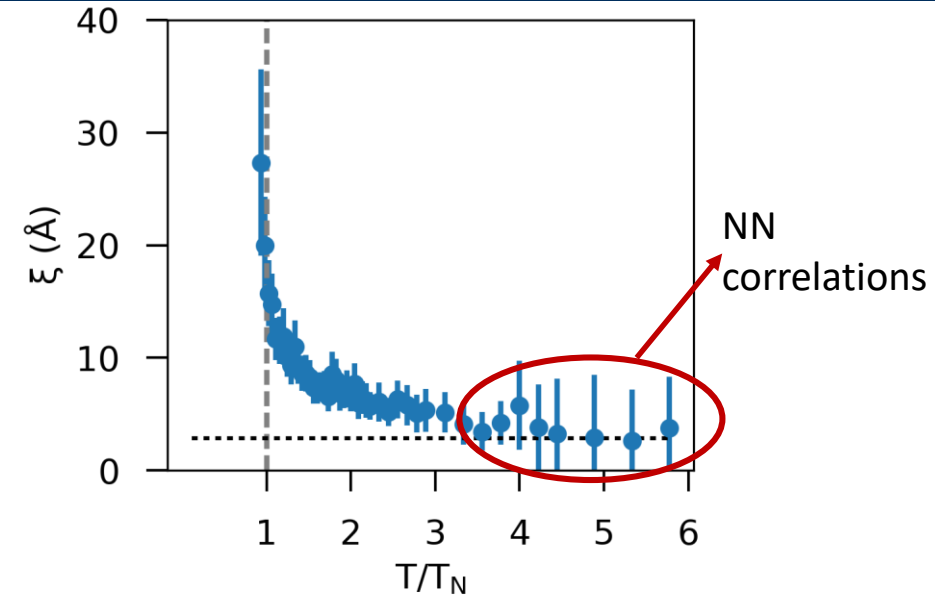
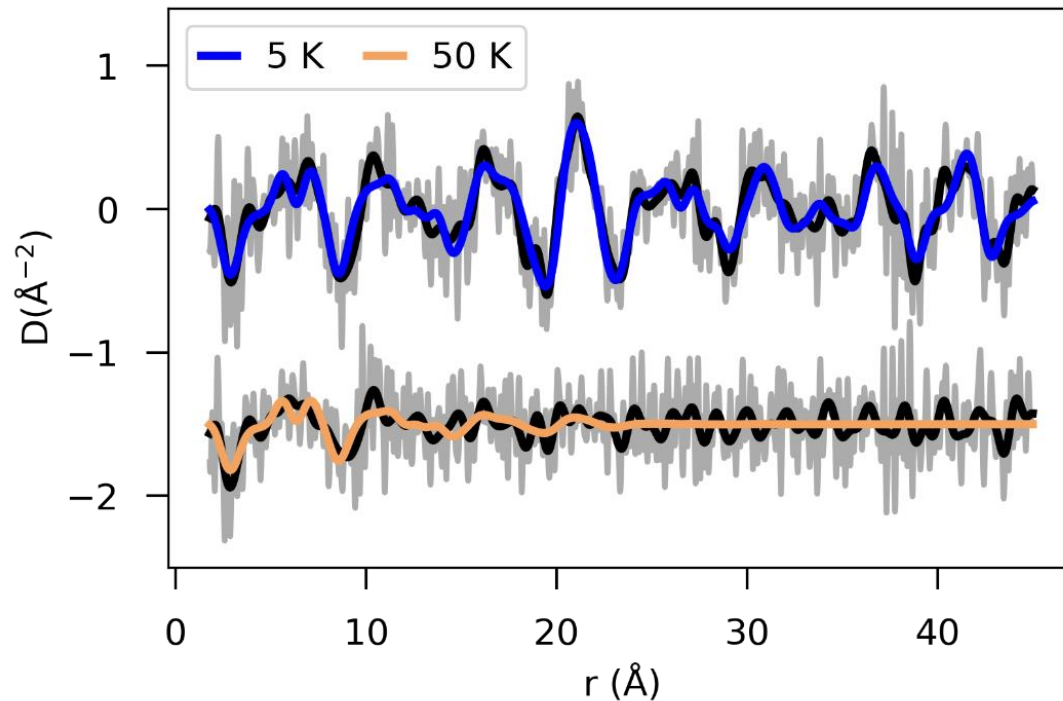
Magnetic PDF refinements for NaMnO_2



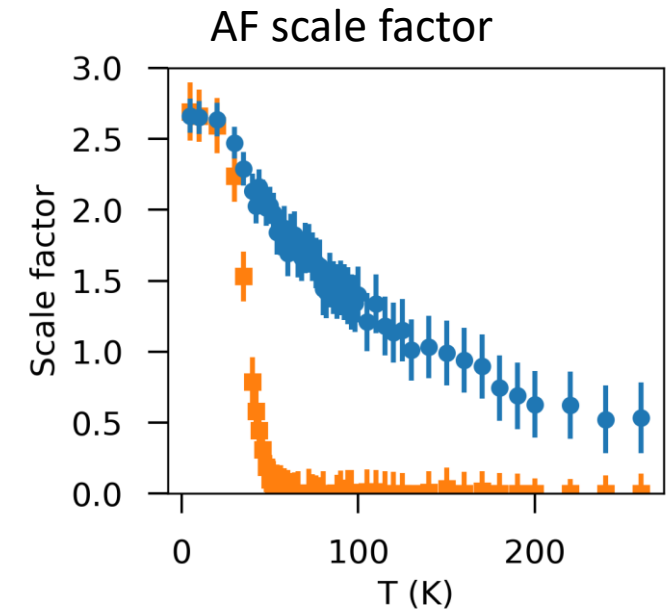
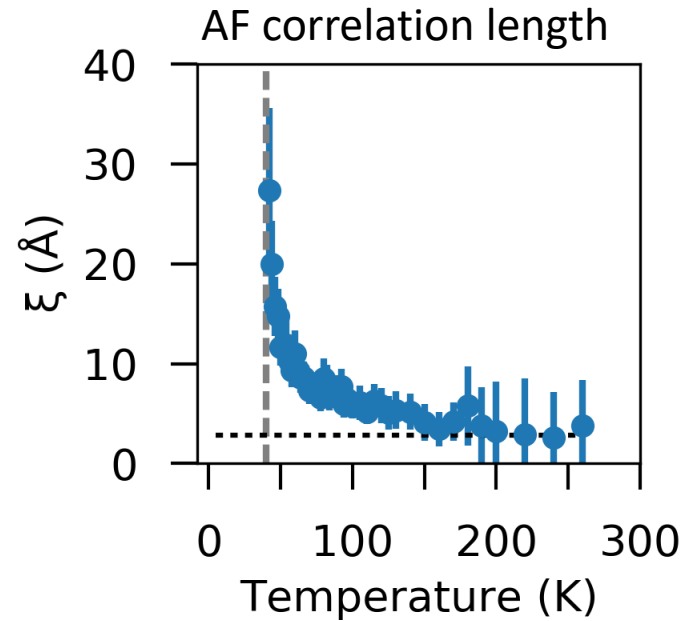
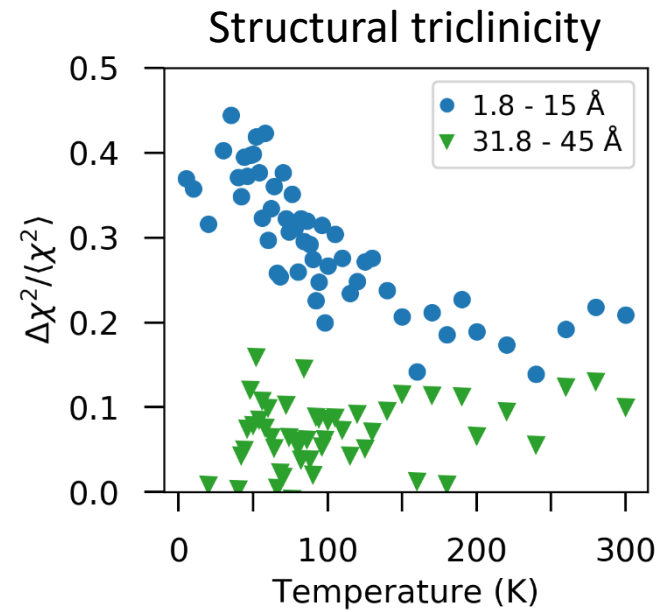
Magnetic PDF refinements

Magnetic model parameters:

- Scale factor
- Exponential damping envelope
- Two polar angles to define spin direction



Connection to atomic PDF results: Pinning down the transition mechanism



- Local triclinicity and AF correlations share identical temperature dependence
- Long-range AF order triggered once AF correlations reach length scale of local triclinic distortion (~ 2 nm)
- **Novel transition mechanism:** *Short-range* triclinic distortion lifts triangular degeneracy on the nanoscale, enabling *long-range* antiferromagnetic order



Comparison to CuMnO_2 : Whence the difference?

CuMnO_2 achieves magnetic LRO through a *global* degeneracy-lifting structural distortion; NaMnO_2 does the same through a *local* distortion

Key Difference: NaMnO_2 has significantly more structural disorder

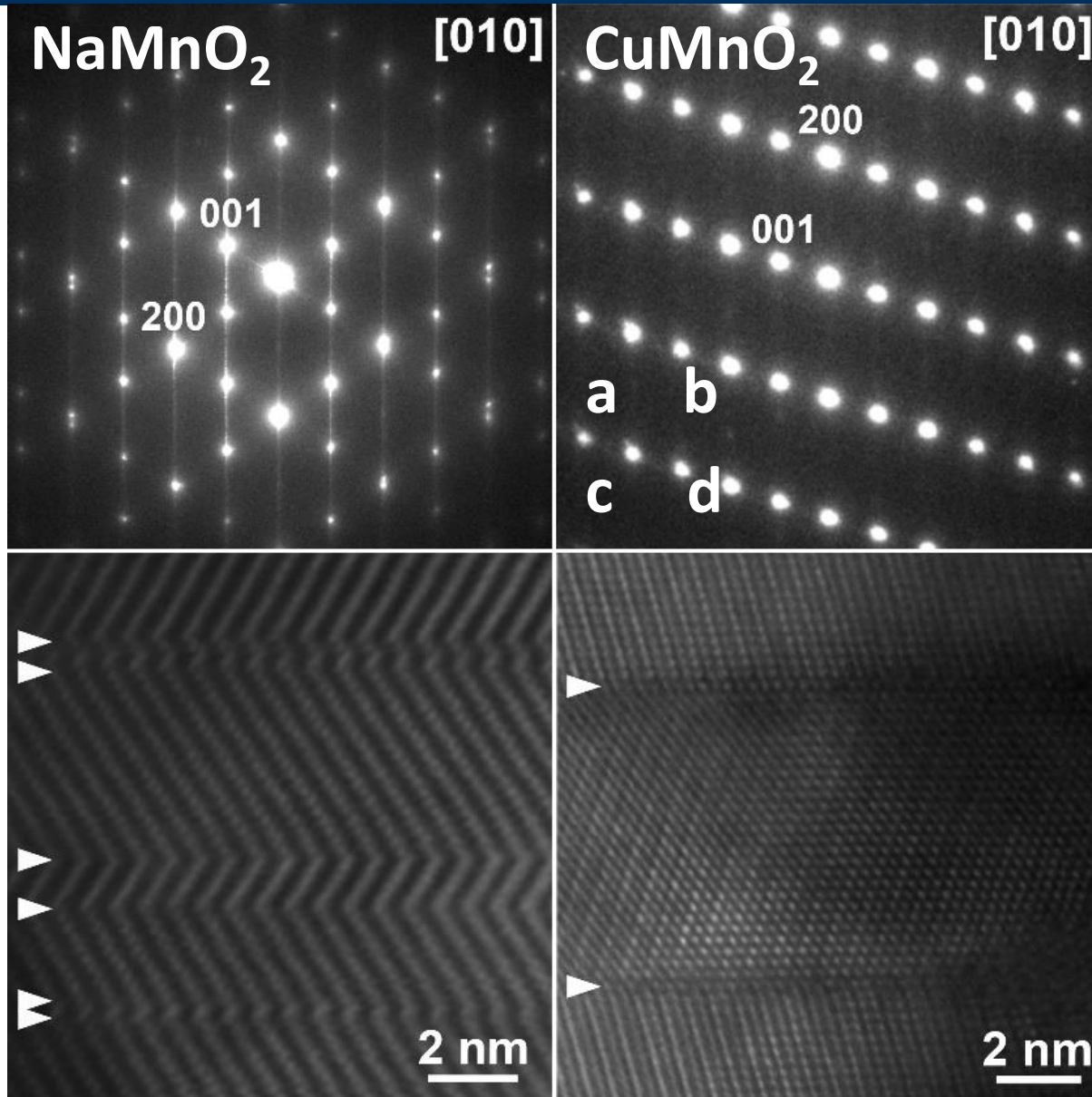
Na vacancies (8%)
 $\text{Mn}^{3+} (S=2) \rightarrow \text{Mn}^{4+} (S=3/2)$

Stacking faults



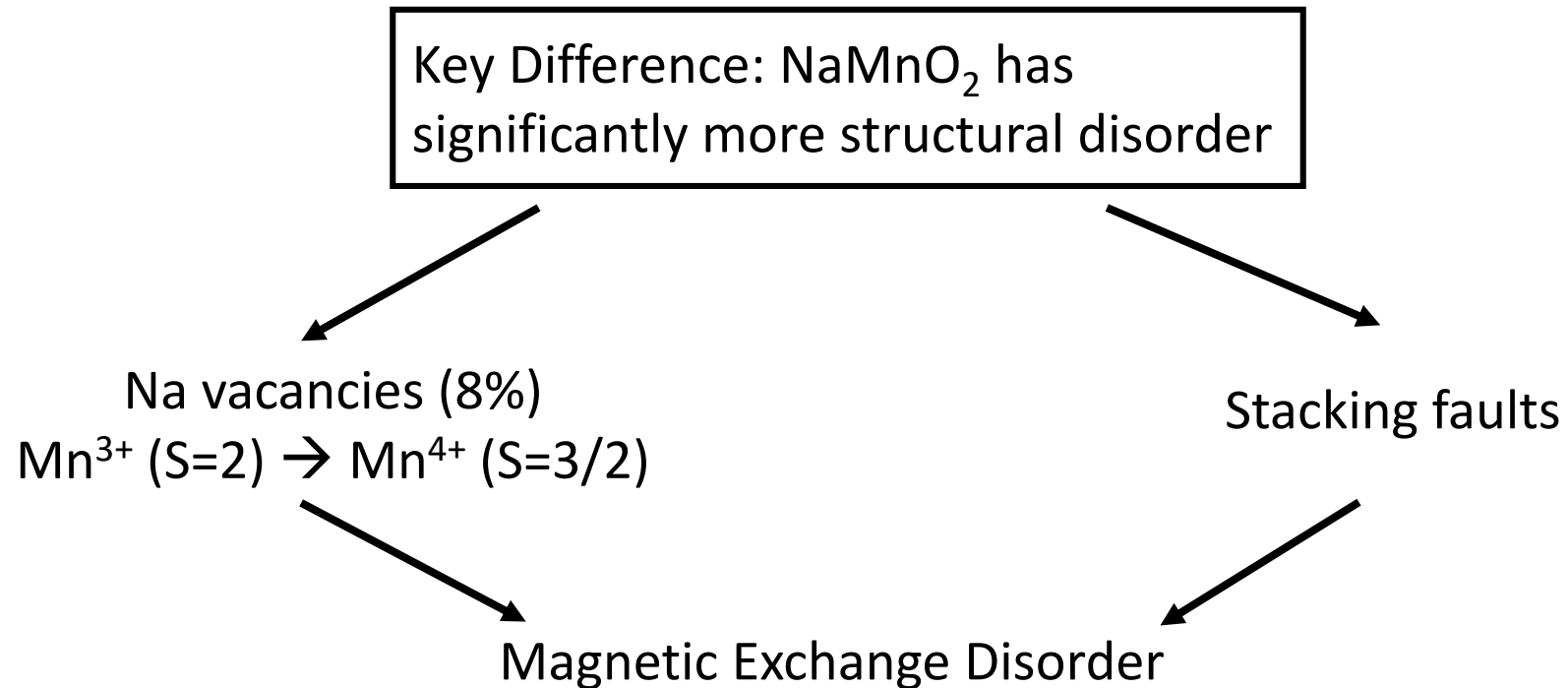
Stacking faults in NaMnO_2 and CuMnO_2

TEM data

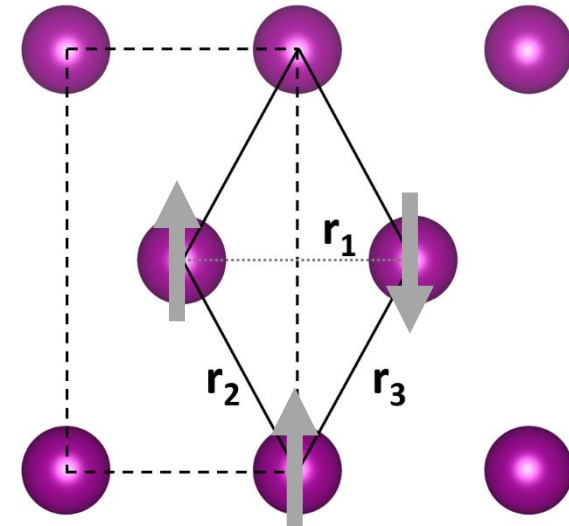


Comparison to CuMnO_2 : Whence the difference?

CuMnO_2 achieves magnetic LRO through a *global* degeneracy-lifting structural distortion; NaMnO_2 does the same through a *local* distortion



Theoretical prediction of NN Heisenberg model with magnetoelastic coupling: Beyond a critical level of exchange disorder, a global structural transition will NOT occur



Conclusions

- NaMnO_2 displays a well-defined local triclinic distortion correlated over a 2 nm length scale that increases at low temperature
- Short-range AF correlations persist above T_N and track with the local triclinic distortion
- Local triclinic distortion lifts the magnetic degeneracy on the nanoscale, enabling long-range AF order below 45 K
- Rare example of short-range structural distortion coupling to long-range AF order
- Combined atomic and magnetic PDF analysis was key to understanding this system

