

UNIVERSITY OF
CAMBRIDGE

Spinvert: Magnetic structure refinement for correlated paramagnets

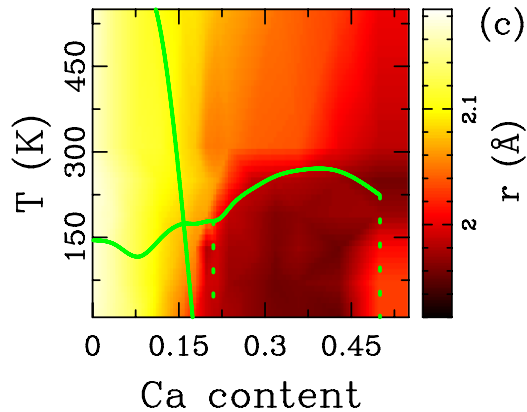
Joe Paddison
University of Cambridge

ADD2019 Grenoble
March 2019

Why magnetic disorder?

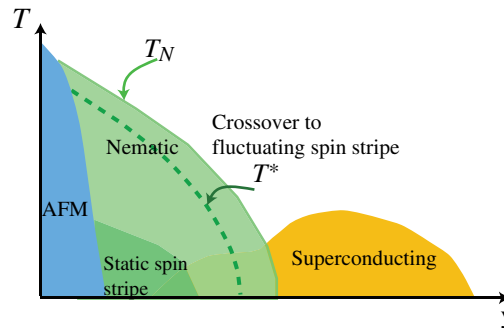
- ❑ Relevant to important magnetic materials
- ❑ Can generate new & exotic magnetic states

Colossal magnetoresistance

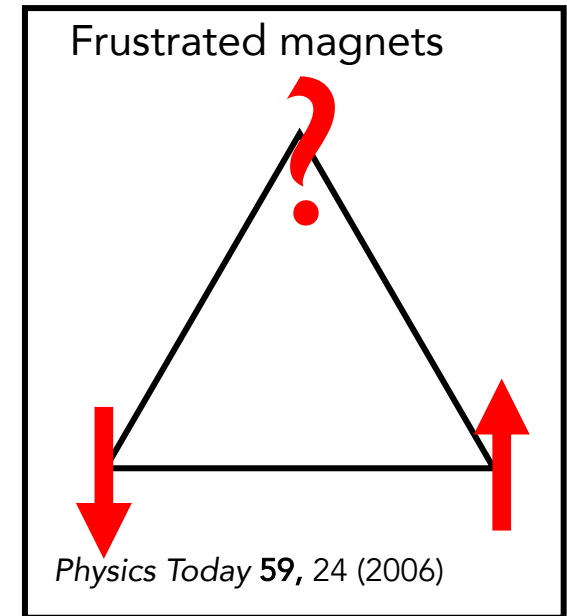


PRL **98**, 137203 (2007)

High- T_c superconductors



Rev. Mod. Phys. **75**, 1201 (2003)

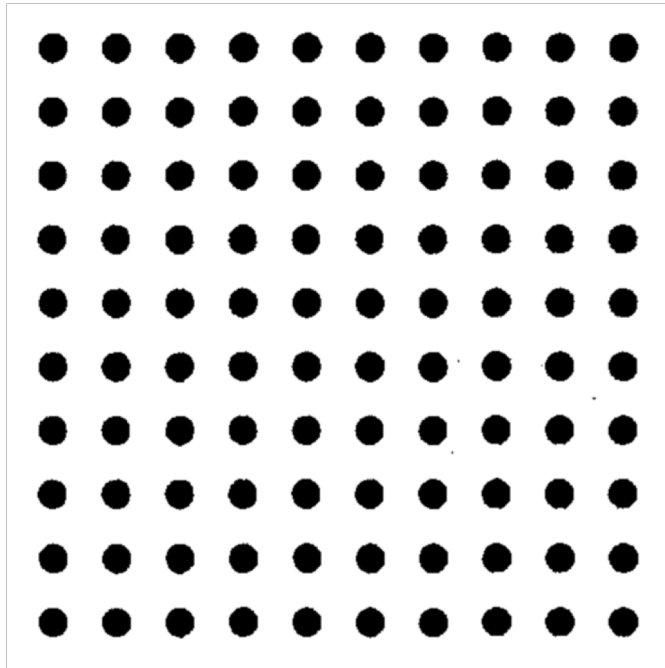


Physics Today **59**, 24 (2006)

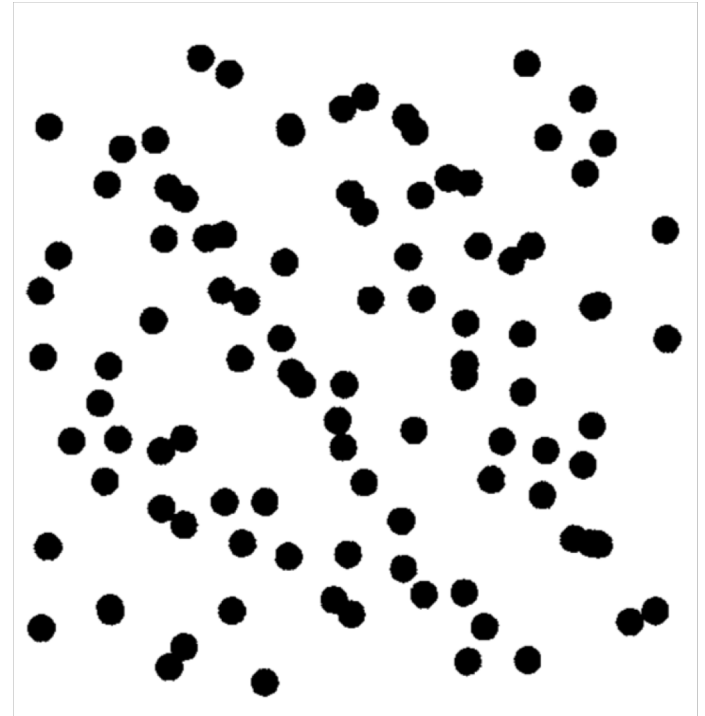
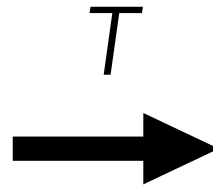
Plan

- **Introduction**
- Magnetic neutron scattering
- Reverse Monte Carlo & Spinvert
- Powder case study: $\text{Gd}_3\text{Ga}_5\text{O}_{12}$
- Single-crystal refinements

Disorder \neq randomness

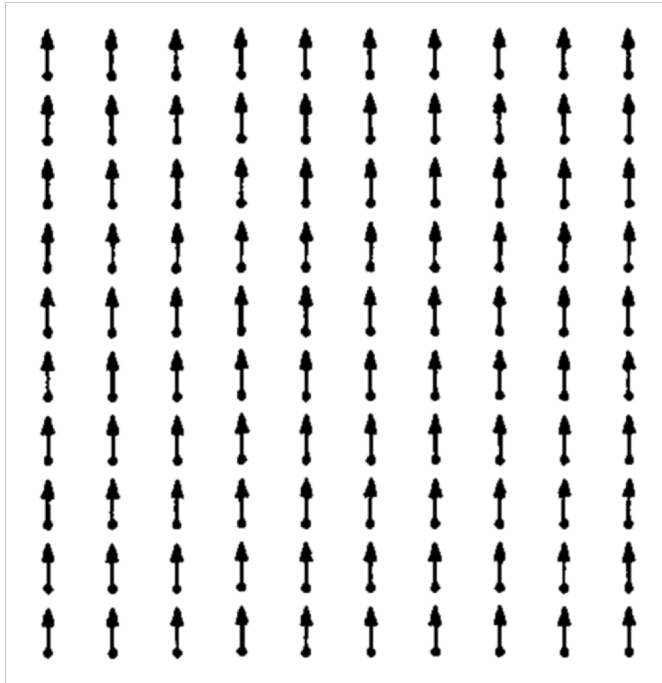


ordered

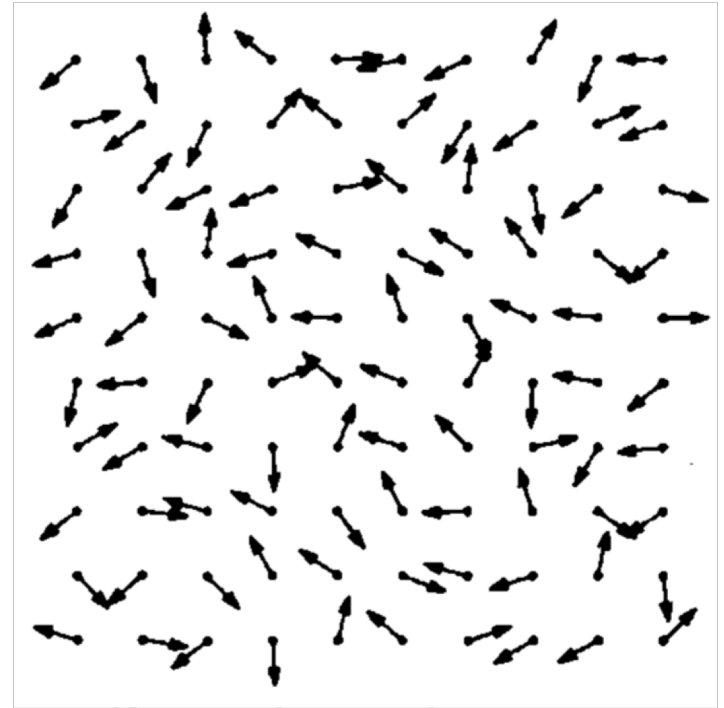
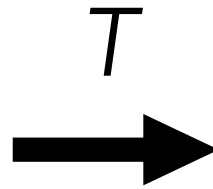


disordered

Disorder \neq randomness

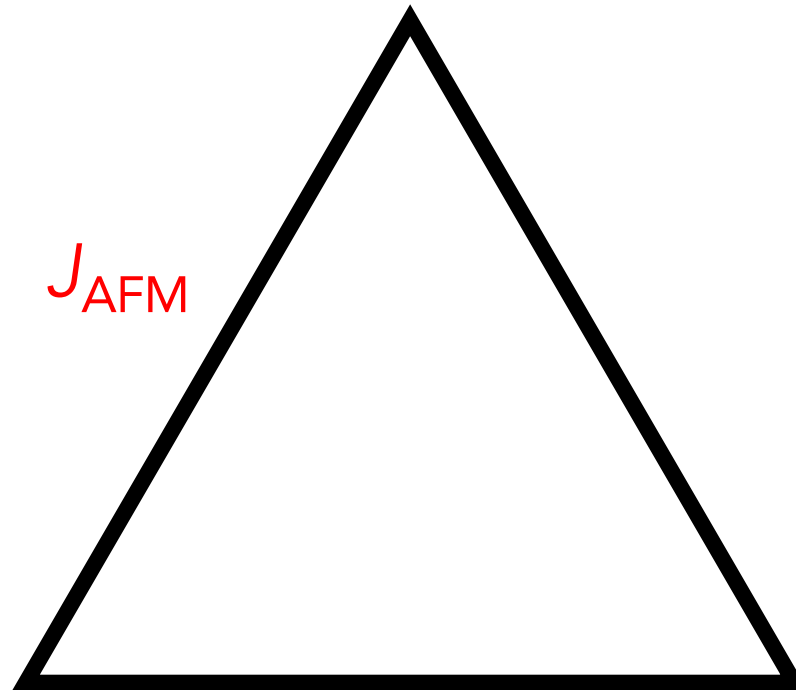


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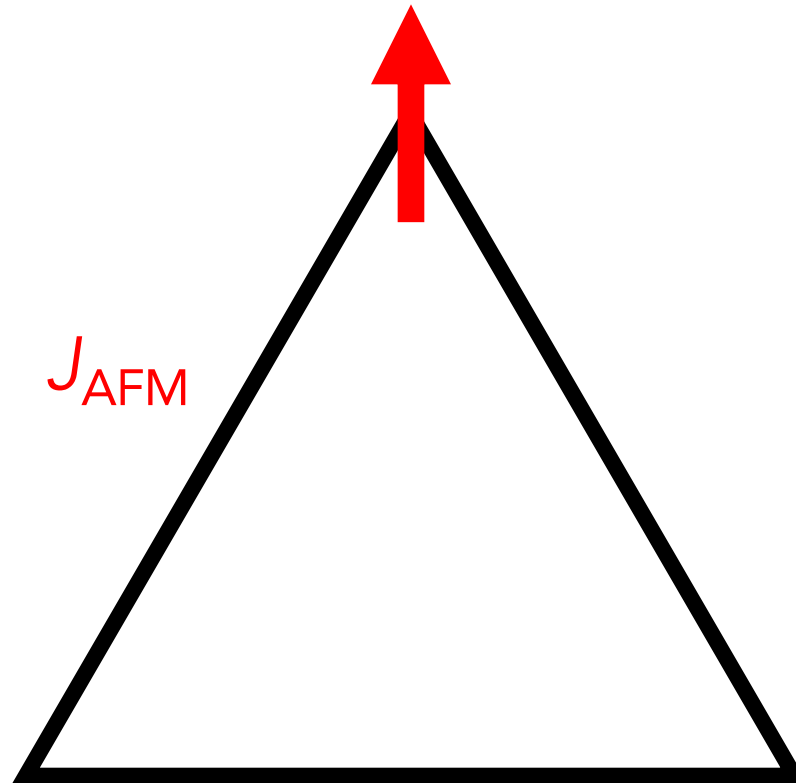
disordered

Magnetic frustration



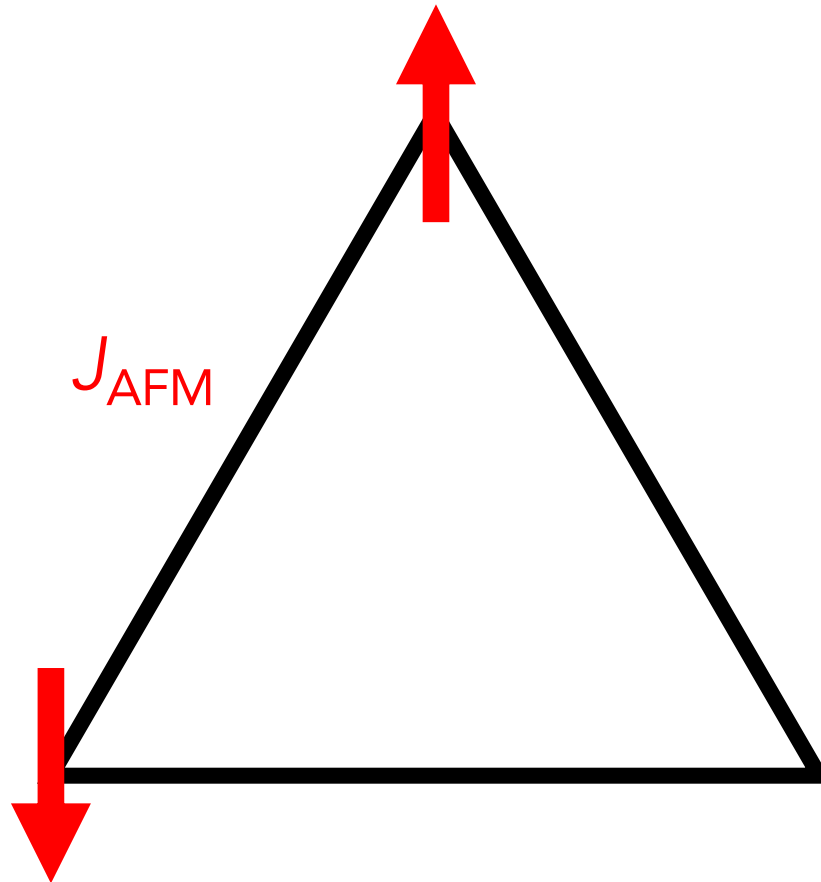
Wannier, *Phys Rev* **79**, 357 (1950)

Magnetic frustration



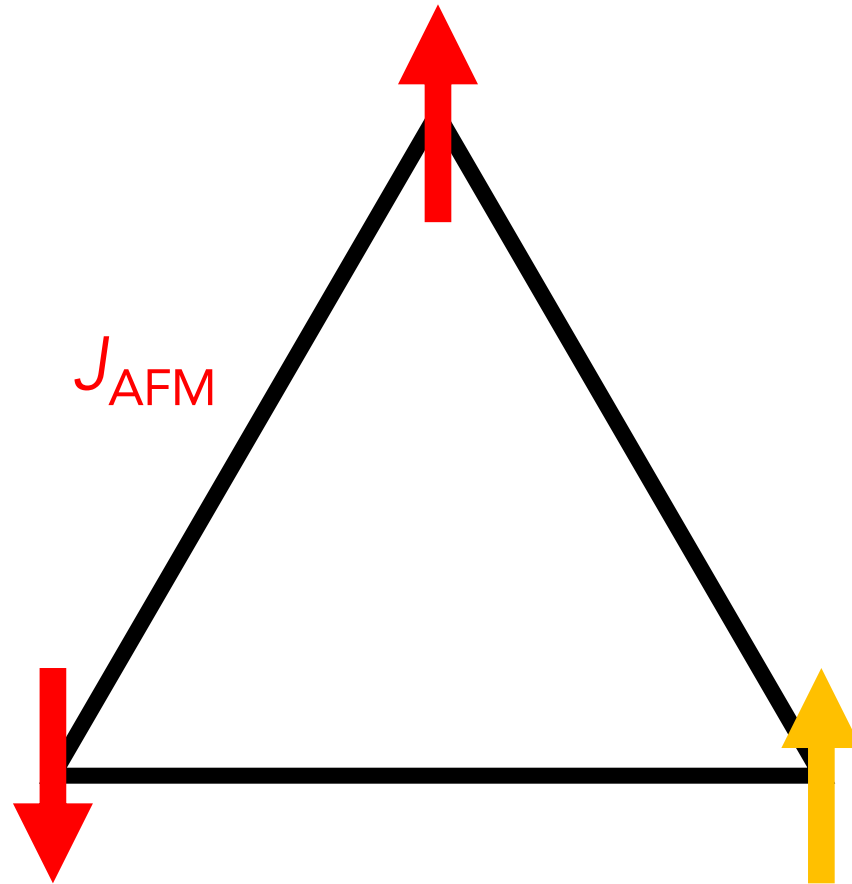
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Magnetic frustration



Wannier, *Phys Rev* **79**, 357 (1950)

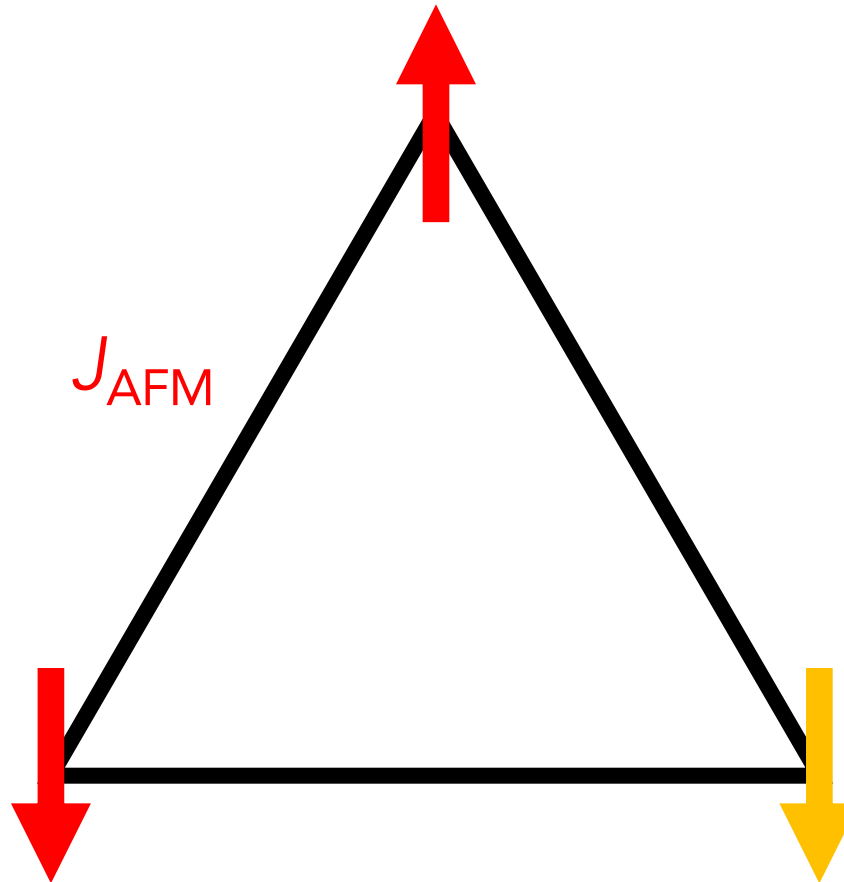
Magnetic frustration



(geometrical) frustration

Wannier, *Phys Rev* 79, 357 (1950)

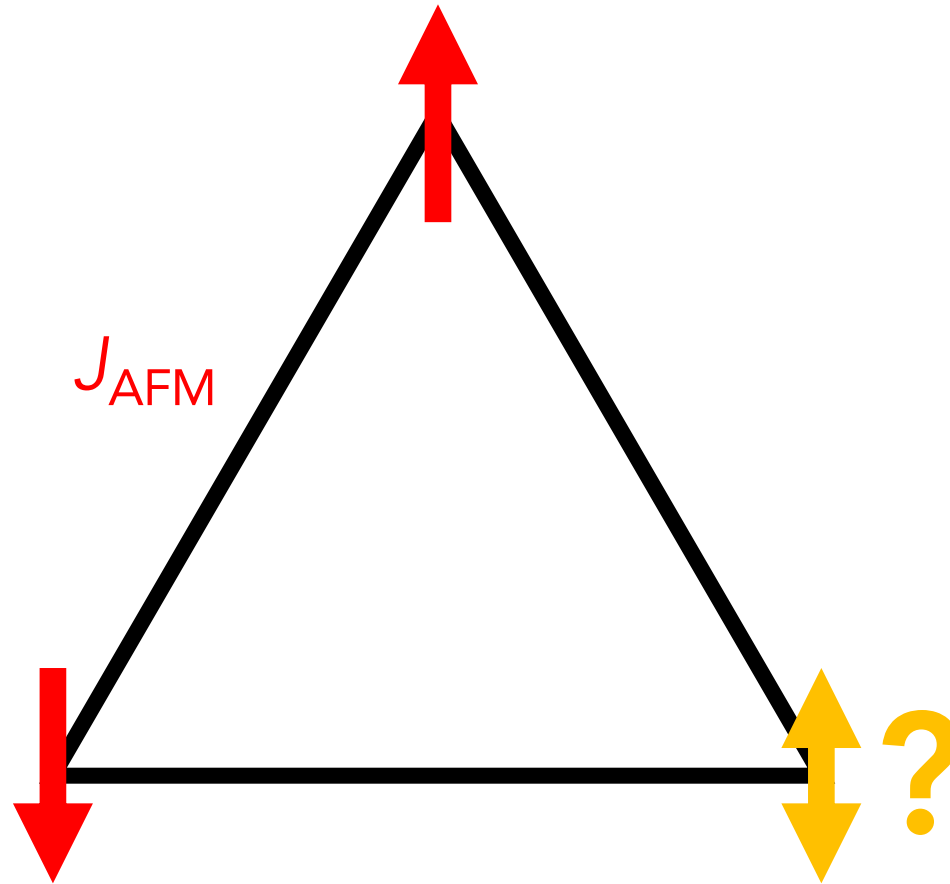
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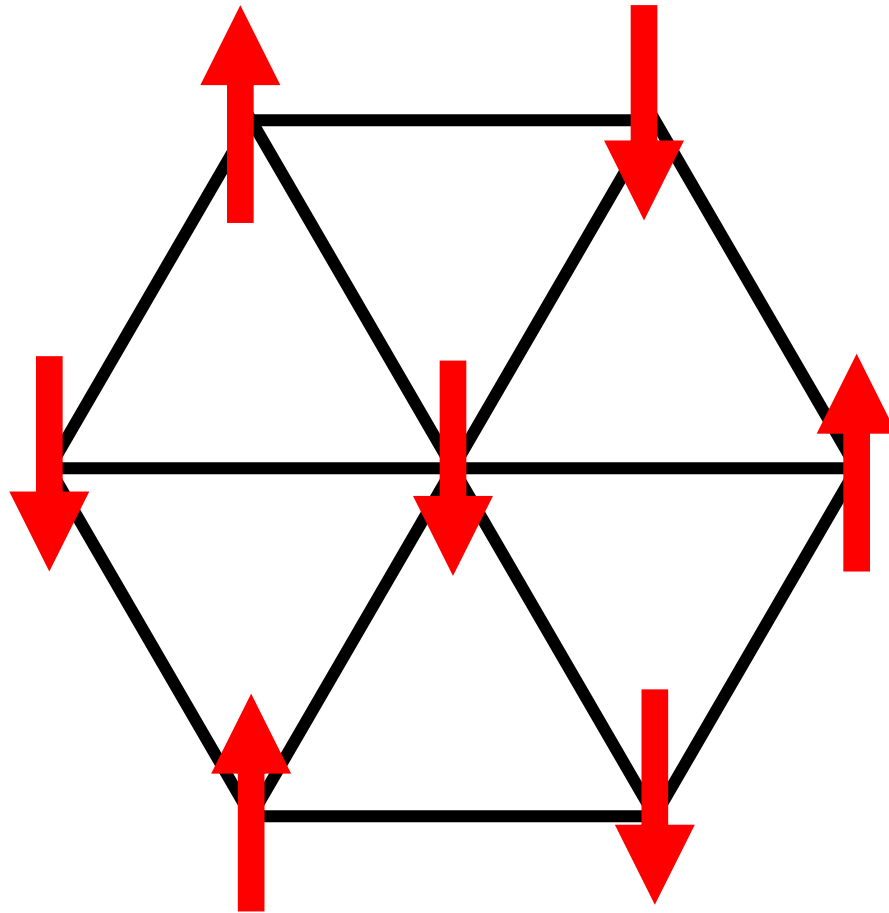
Magnetic frustration



frustration \rightarrow *degeneracy*

Wannier, *Phys Rev* 79, 357 (1950)

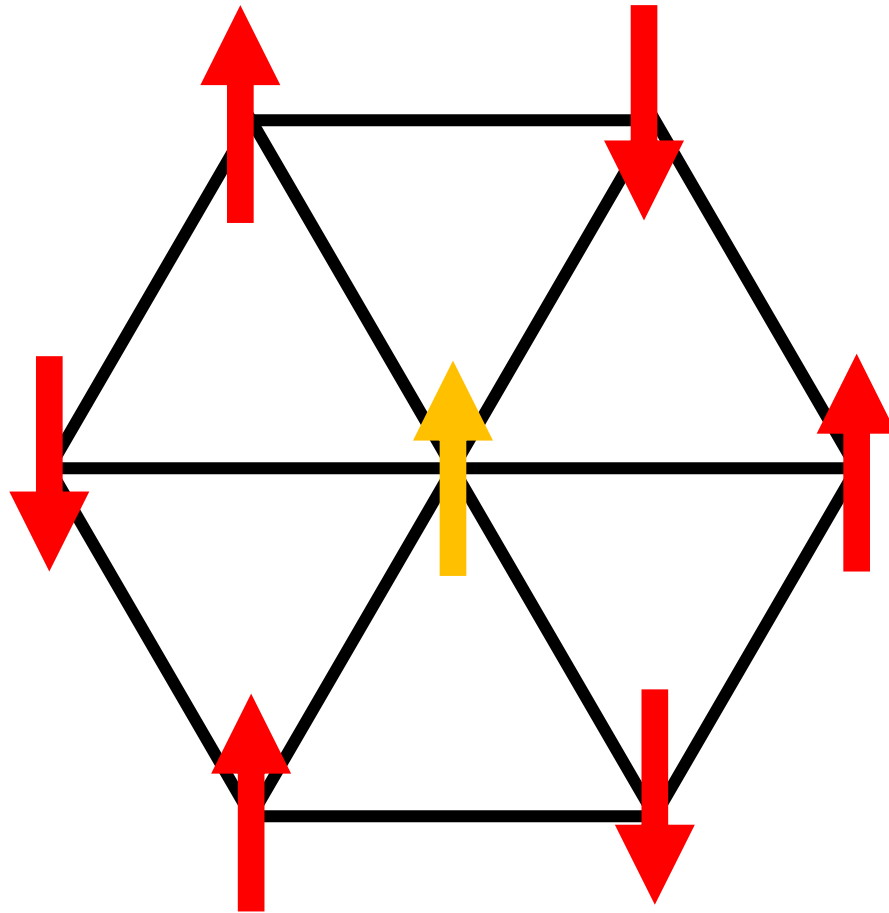
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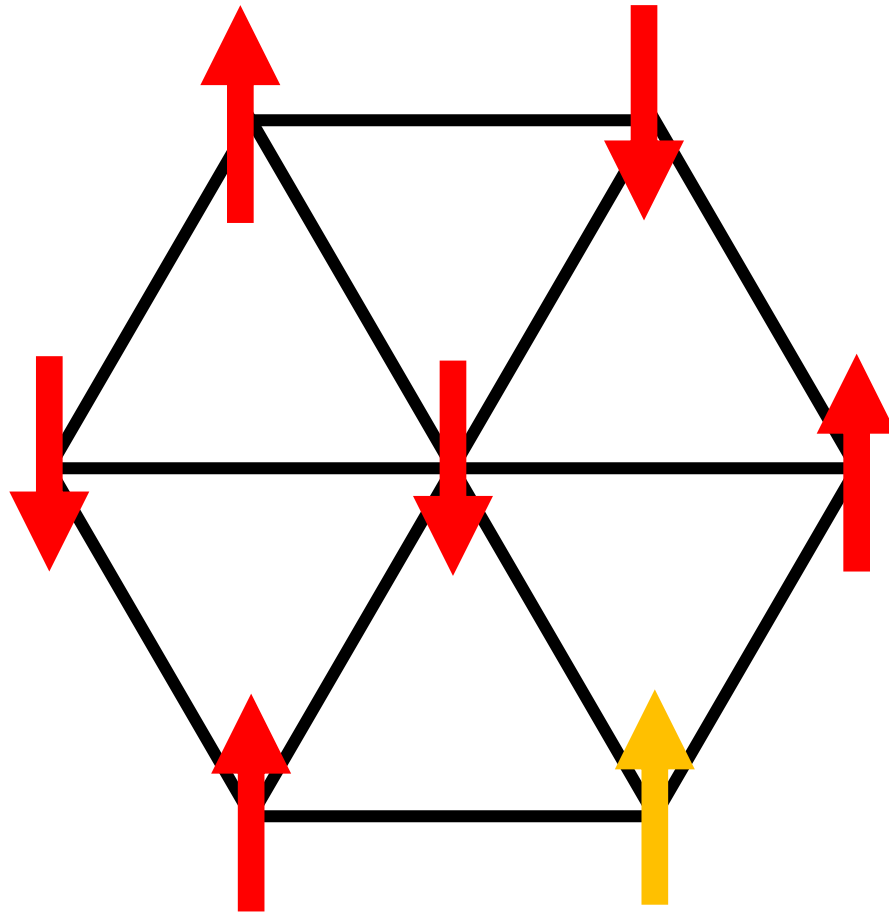
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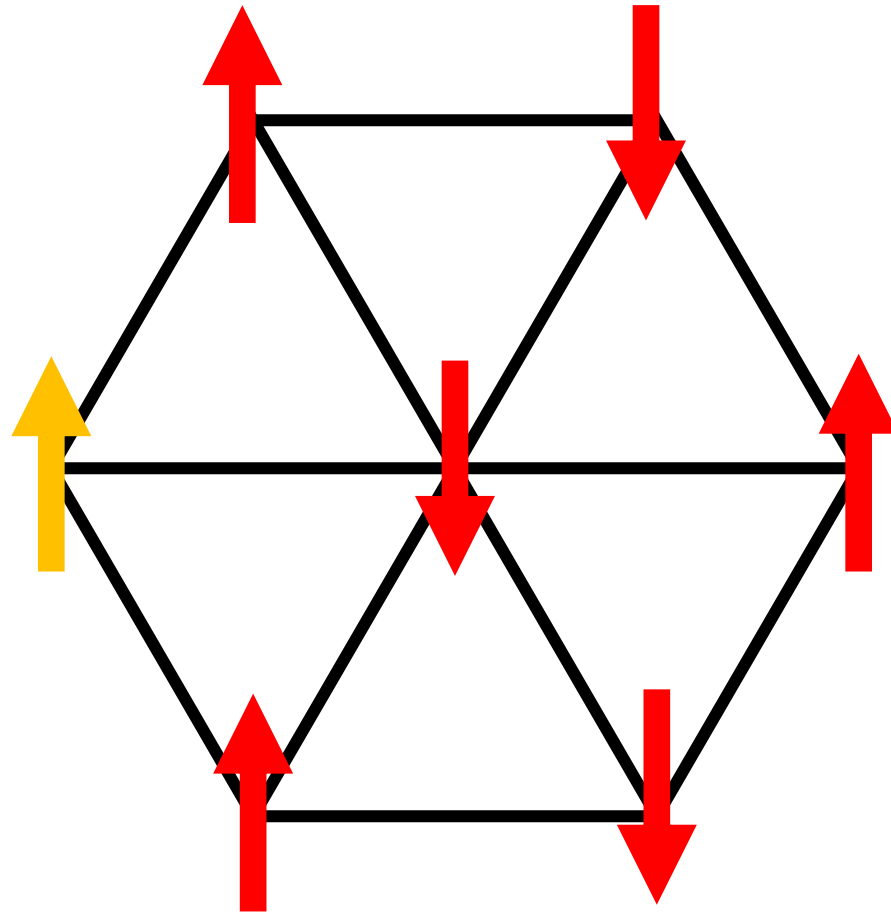
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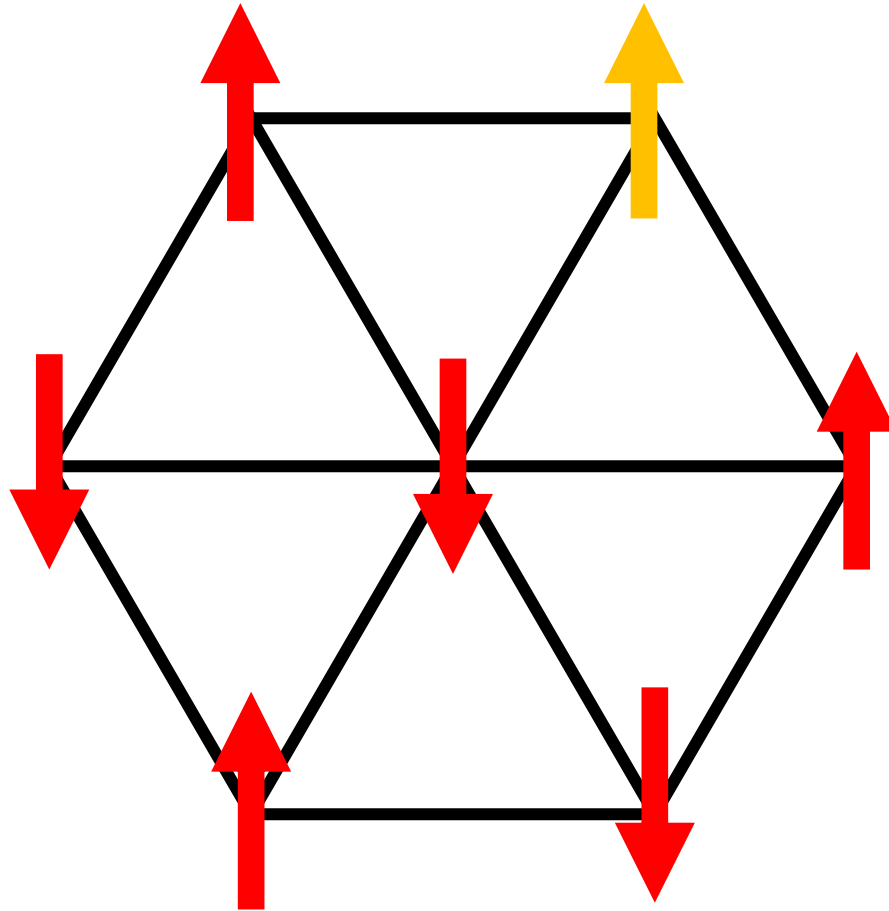
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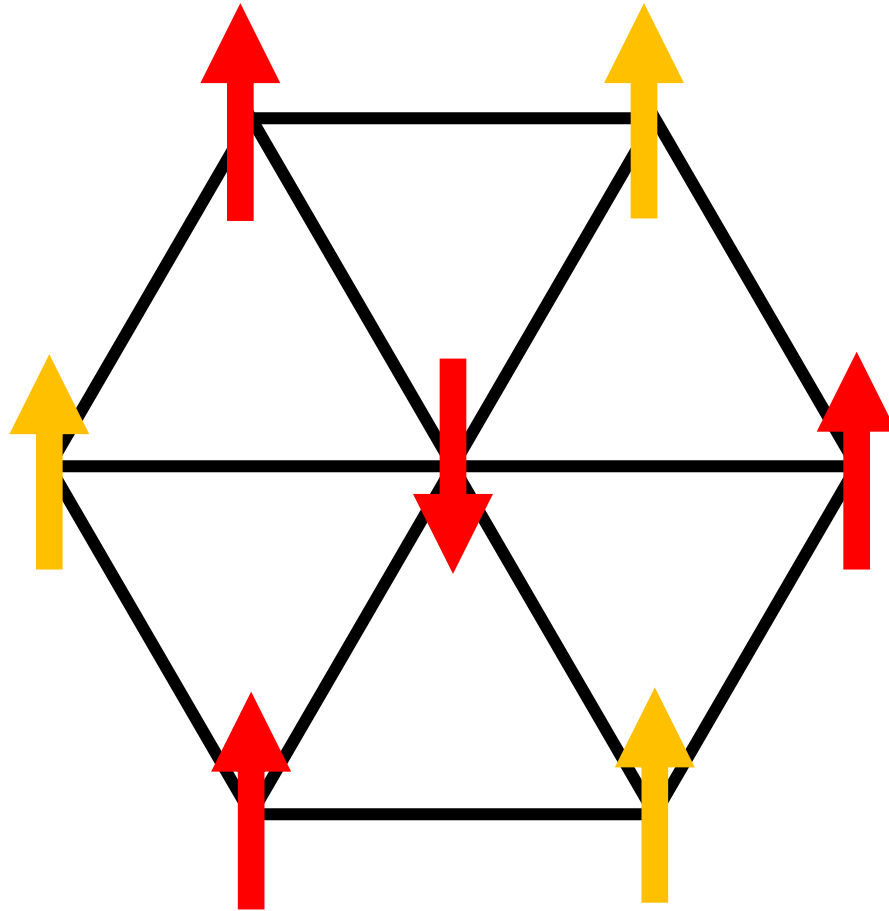
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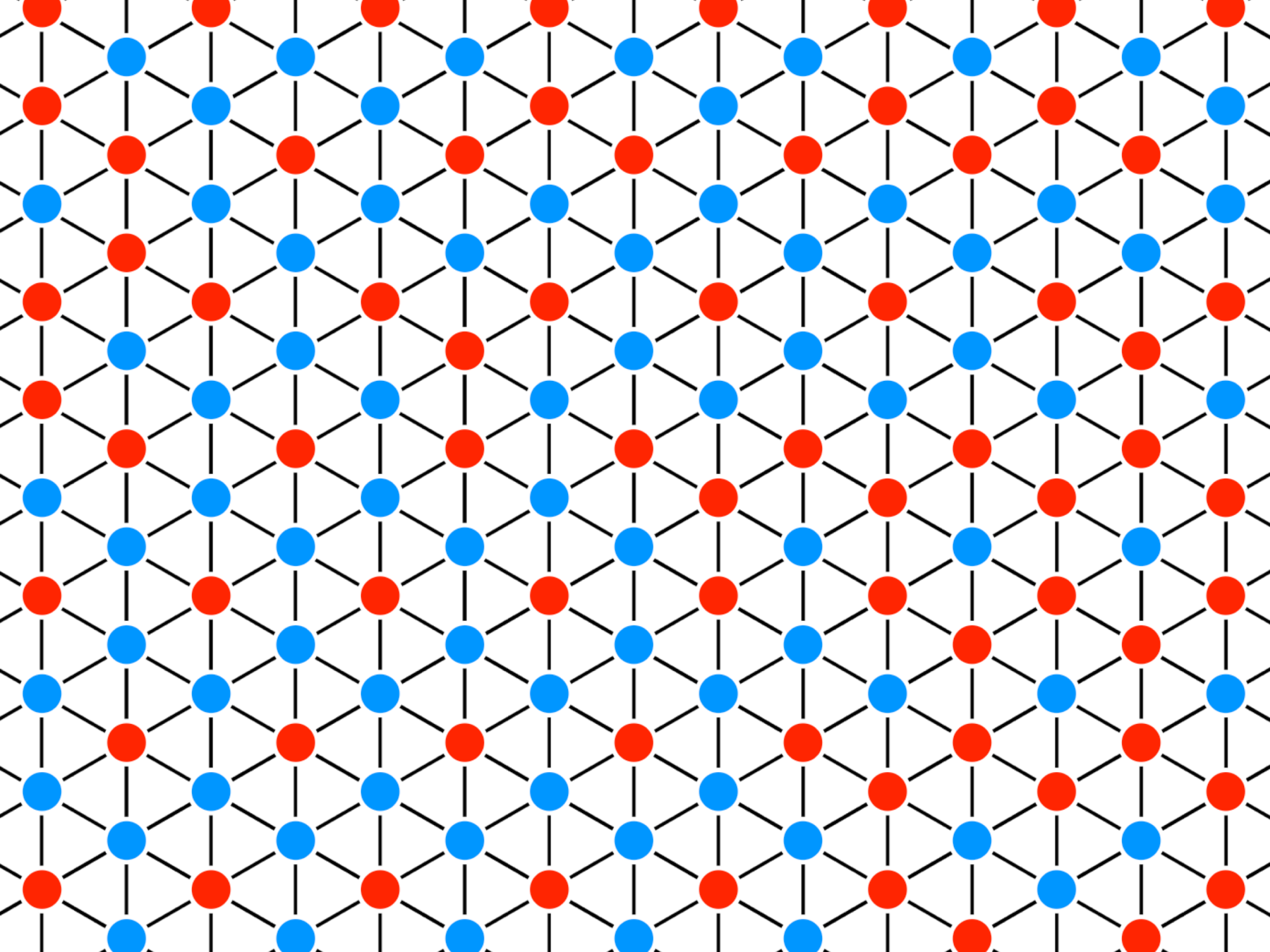
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Magnetic frustration

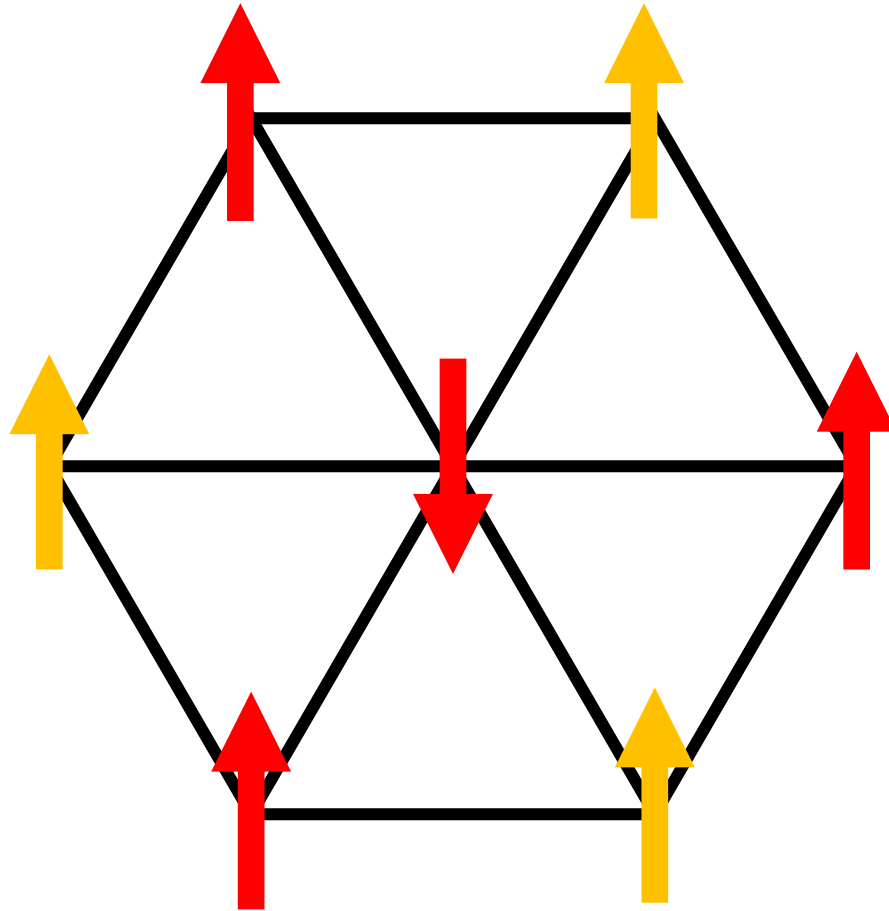


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Magnetic frustration

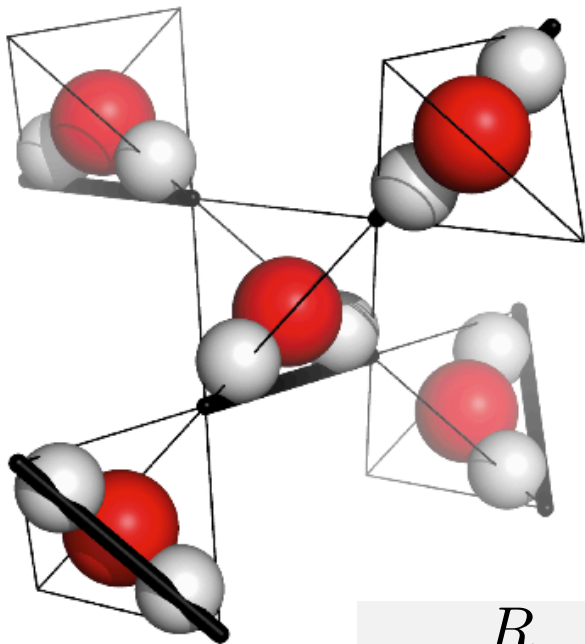


frustration \rightarrow *degeneracy* \rightarrow *correlated disorder*

Wannier, *Phys Rev* 79, 357 (1950)

"Ice rules"

(cubic) water ice



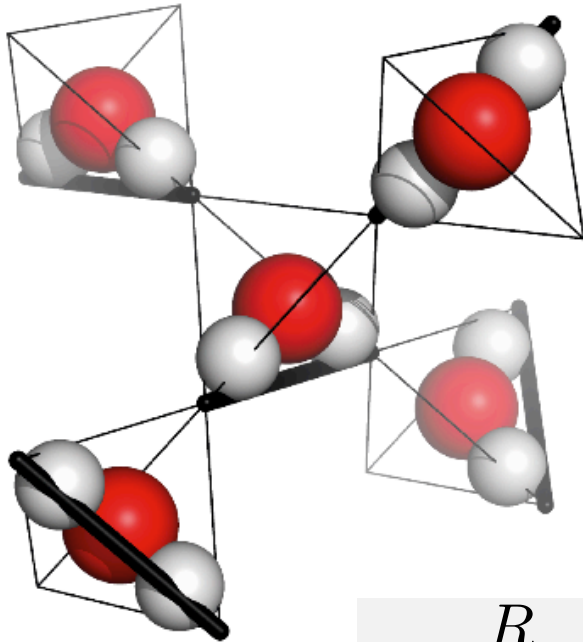
$$S = \frac{R}{2} \ln \left(\frac{3}{2} \right)$$

frustration → *degeneracy* → *correlated disorder*

Pauling, *J. Am. Chem. Soc.* 57, 2680 (1935)

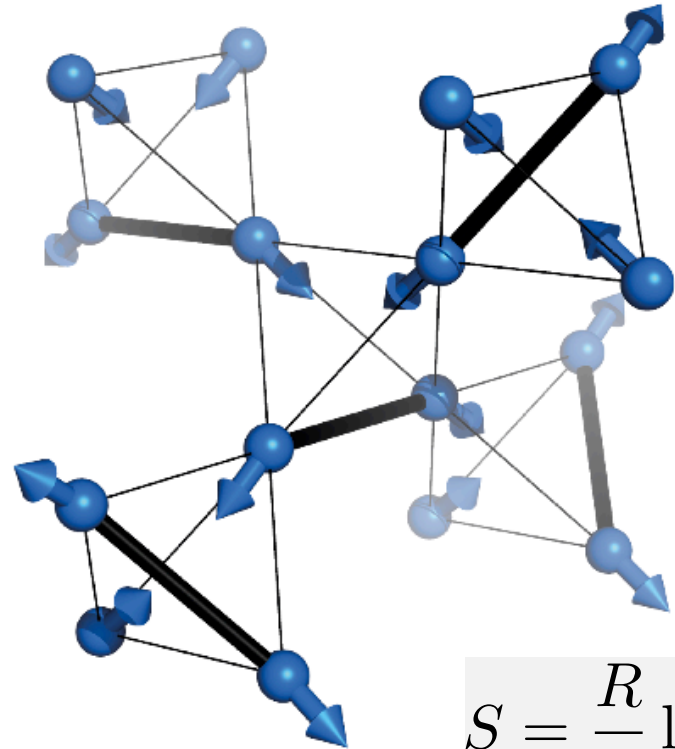
"Ice rules"

(cubic) water ice



$$S = \frac{R}{2} \ln \left(\frac{3}{2} \right)$$

spin ice



$$S = \frac{R}{2} \ln \left(\frac{3}{2} \right)$$

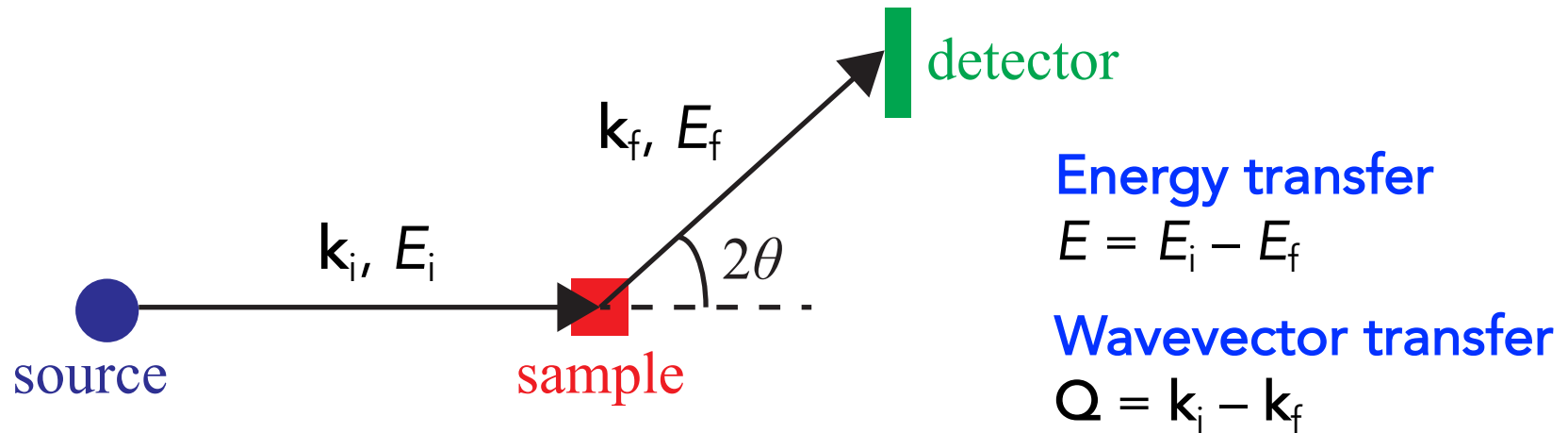
frustration \rightarrow degeneracy \rightarrow correlated disorder

Bramwell & Harris, *PRL* 79, 2554 (1997)
Pauling, *J. Am. Chem. Soc* 57, 2680 (1935)

Plan

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- **Magnetic neutron scattering**
- Reverse Monte Carlo & Spinvert
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Total scattering



- Total scattering: integral over energy transfer

$$I(\mathbf{Q}) = \int_{-\infty}^{\infty} I(\mathbf{Q}, E) dE$$

- Measures instantaneous correlations

- Quasi-static approximation: $\int dE \approx \int dE_f$ if $E \ll E_i$
diffraction (E_f not analysed)

- Total scattering = Bragg + diffuse

Nuclear neutron scattering – Equations

□ Assume elemental system (for simplicity)

➤ **Single crystal**

$$I_n(\mathbf{Q}) = b^2 \left(1 + \frac{1}{N} \sum_{i,j \neq i} \langle \exp(i\mathbf{Q} \cdot \mathbf{r}_{ij}) \rangle \right)$$

b = coherent scattering length

N = number of atoms

\mathbf{r}_{ij} = vector separation

$\langle \rangle$ = thermal average

Squires, *Introduction to Thermal Neutron Scattering*, CUP (1978)

Debye, *Ann. Phys. (Berlin)*, 351, 809 (1915)

Nuclear neutron scattering – Equations

□ Assume elemental system (for simplicity)

➤ **Single crystal**

$$I_n(\mathbf{Q}) = b^2 \left(1 + \frac{1}{N} \sum_{i,j \neq i} \langle \exp(i\mathbf{Q} \cdot \mathbf{r}_{ij}) \rangle \right)$$

↓ spherical
average

b = coherent scattering length
 N = number of atoms
 \mathbf{r}_{ij} = vector separation
 $\langle \rangle$ = thermal average

➤ **Powder**

$$I_n(Q) = b^2 \left(1 + \frac{1}{N} \sum_{i,j \neq i} \underbrace{\left\langle \frac{\sin Qr_{ij}}{Qr_{ij}} \right\rangle}_{\text{scattering from atom-pair correlations}} \right)$$

↑
single-atom
scattering
(ideal gas)

Debye formula
 r_{ij} = radial separation

Magnetic neutron scattering – Equations

□ Assume magnetic ions of a single type, with fixed locations

➤ **Single crystal**

$$I_m(\mathbf{Q}) = C [gf(Q)]^2 \left[\frac{2}{3} S(S+1) + \frac{1}{N} \sum_{i,j \neq i} \langle \mathbf{S}_i^\perp \cdot \mathbf{S}_j^\perp \rangle \exp(i\mathbf{Q} \cdot \mathbf{r}_{ij}) \right]$$

$C = 0.07265$ barn
 $f(Q) =$ form factor

$$\mathbf{S}^\perp = \mathbf{S} - (\mathbf{S} \cdot \hat{\mathbf{Q}})\hat{\mathbf{Q}} \quad \text{component of spin } \mathbf{S} \text{ perpendicular to } \mathbf{Q}$$

Magnetic neutron scattering – Equations

□ Assume magnetic ions of a single type, with fixed locations

➤ Single crystal

$$I_m(\mathbf{Q}) = C [gf(Q)]^2 \left[\frac{2}{3}S(S+1) + \frac{1}{N} \sum_{i,j \neq i} \langle \mathbf{S}_i^\perp \cdot \mathbf{S}_j^\perp \rangle \exp(i\mathbf{Q} \cdot \mathbf{r}_{ij}) \right] \quad \begin{array}{l} C = 0.07265 \text{ barn} \\ f(\mathbf{Q}) = \text{form factor} \end{array}$$

$$\mathbf{S}^\perp = \mathbf{S} - (\mathbf{S} \cdot \hat{\mathbf{Q}})\hat{\mathbf{Q}} \quad \text{component of spin } \mathbf{S} \text{ perpendicular to } \mathbf{Q}$$

➤ Powder

$$I_m(Q) = C [gf(Q)]^2 \left\{ \frac{2}{3}S(S+1) + \frac{1}{N} \sum_{i,j \neq i} \left[\langle A_{ij} \rangle \frac{\sin Qr_{ij}}{Qr_{ij}} + \langle B_{ij} \rangle \left(\frac{\sin Qr_{ij}}{(Qr_{ij})^3} - \frac{\cos Qr_{ij}}{(Qr_{ij})^2} \right) \right] \right\}$$

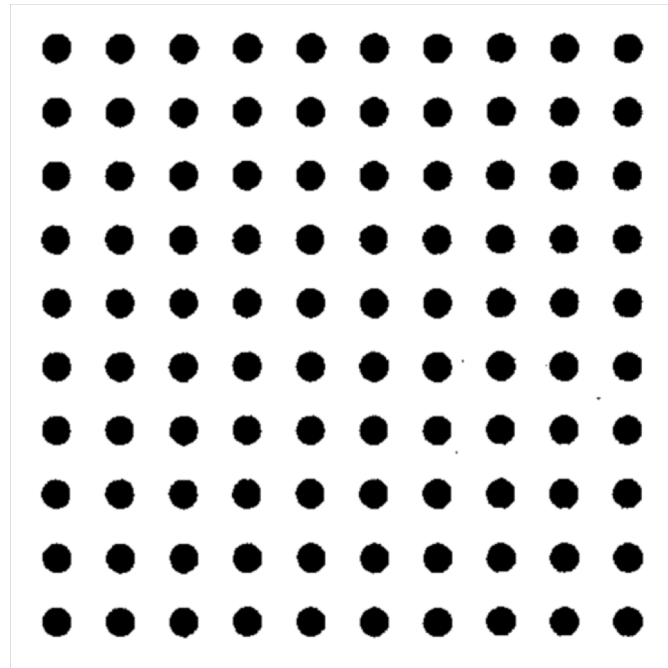
↑
single-spin scattering (ideal paramagnet)

scattering from spin-pair correlations

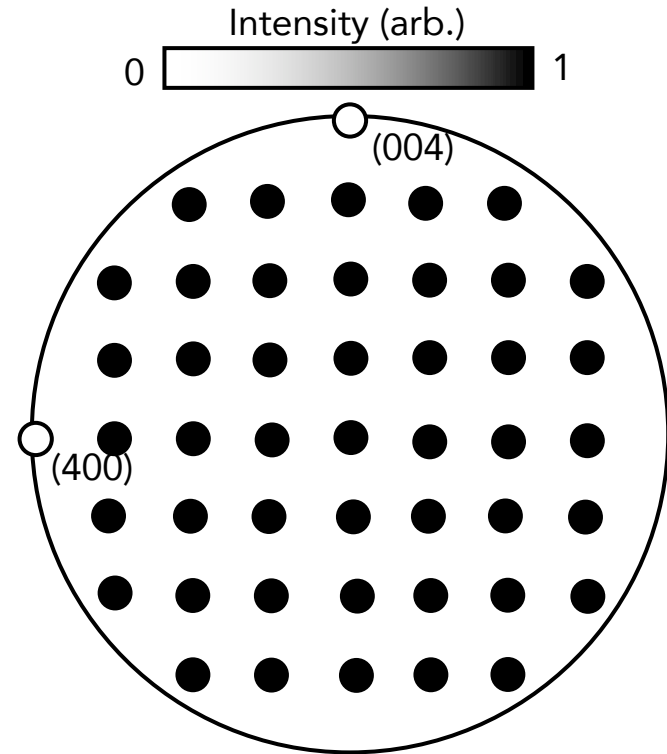
$$\left. \begin{array}{l} A_{ij} = \mathbf{S}_i \cdot \mathbf{S}_j - (\mathbf{S}_i \cdot \hat{\mathbf{r}}_{ij})(\mathbf{S}_j \cdot \hat{\mathbf{r}}_{ij}) \\ B_{ij} = 3(\mathbf{S}_i \cdot \hat{\mathbf{r}}_{ij})(\mathbf{S}_j \cdot \hat{\mathbf{r}}_{ij}) - \mathbf{S}_i \cdot \mathbf{S}_j \end{array} \right\} \begin{array}{l} \text{spin correlation} \\ \text{coefficients} \end{array}$$

Neutron scattering – Order vs disorder

- Long-range order \rightarrow Bragg scattering



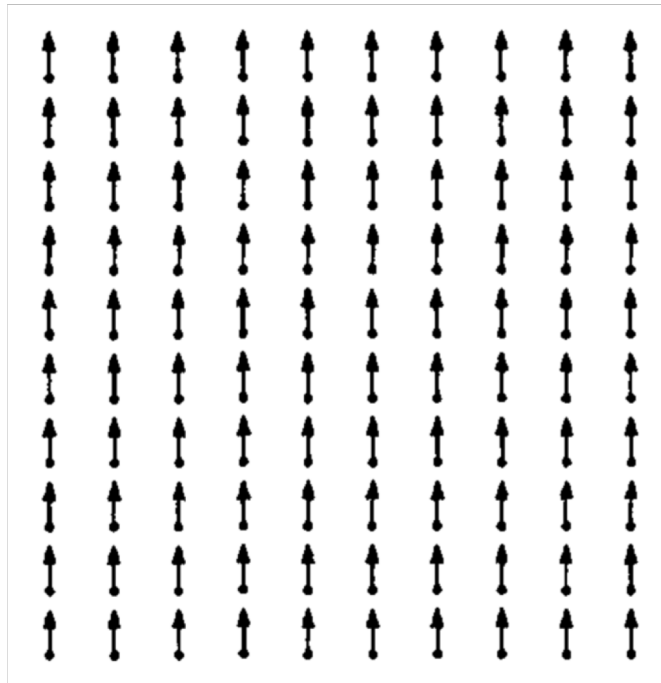
Real space, r



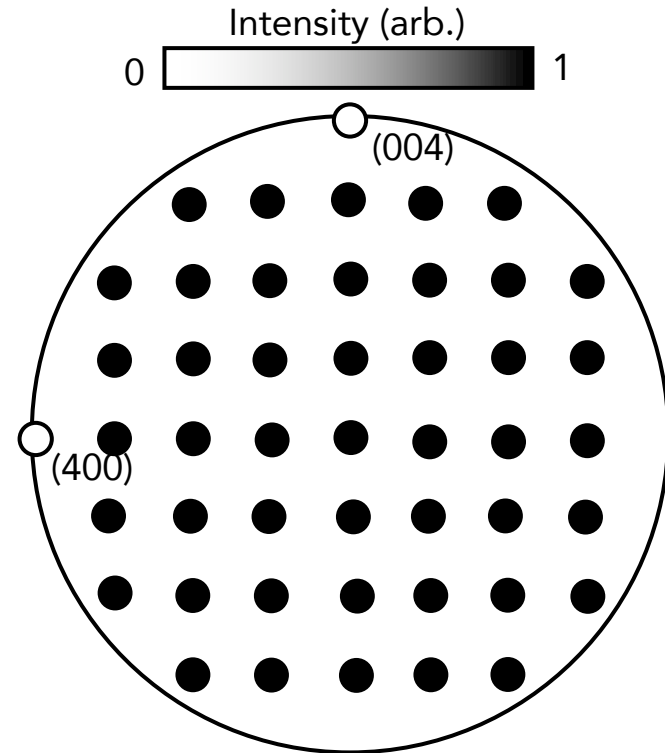
Reciprocal space, Q

Neutron scattering – Order vs disorder

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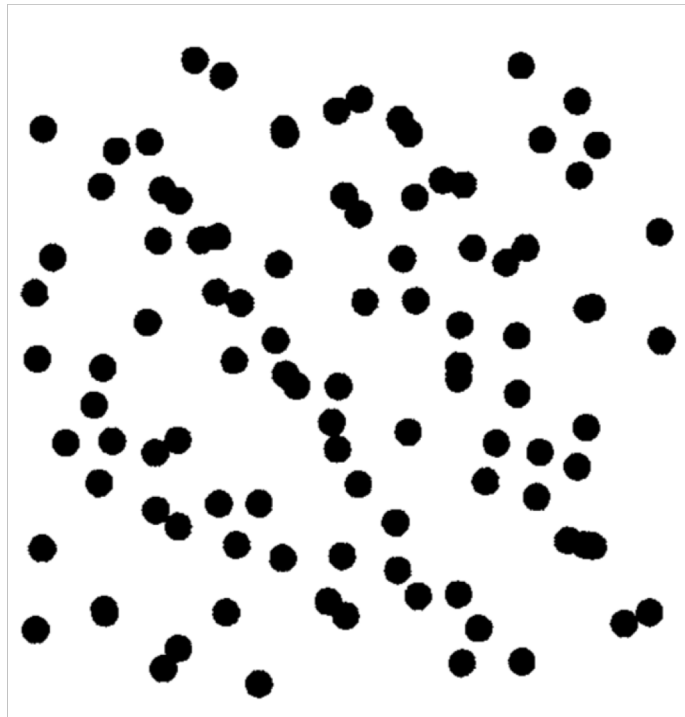
Real space, r



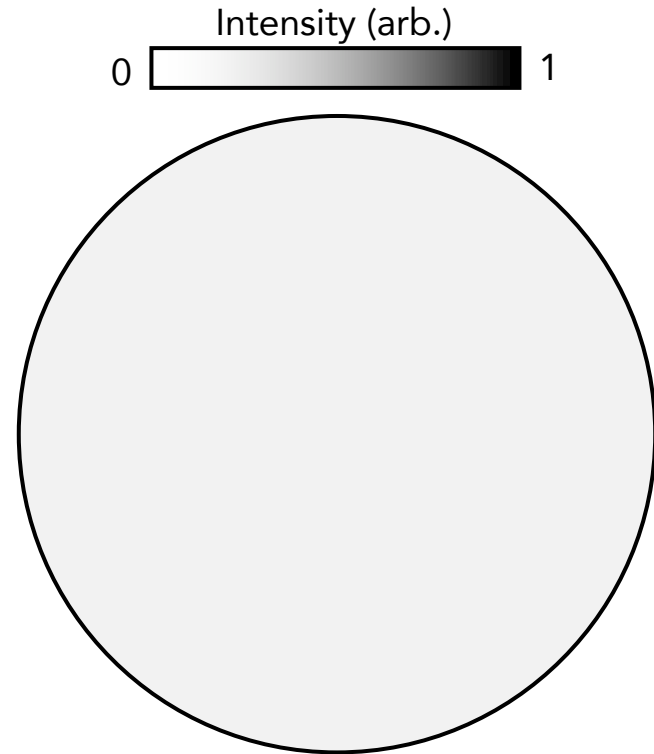
Reciprocal space, Q

Neutron scattering – Order vs disorder

□ Random disorder \rightarrow flat scattering



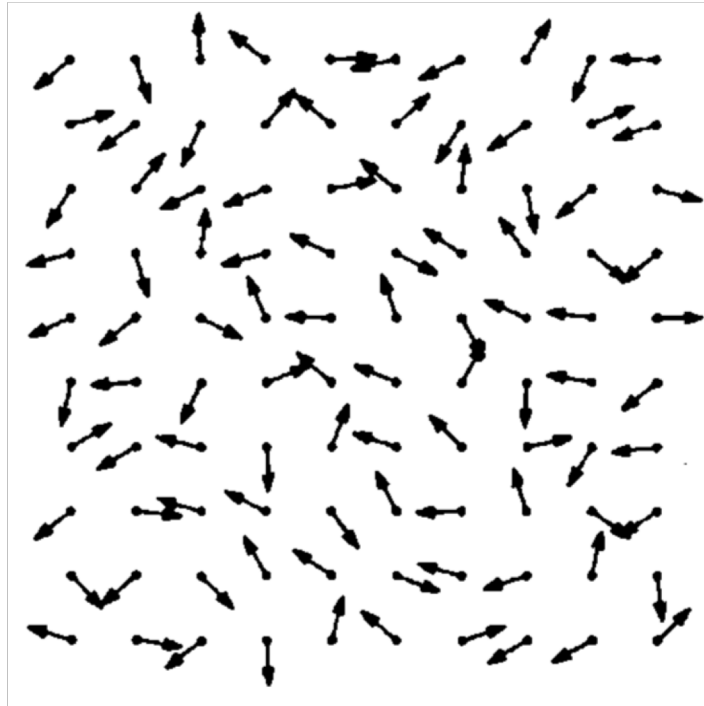
Real space, r



Reciprocal space, Q

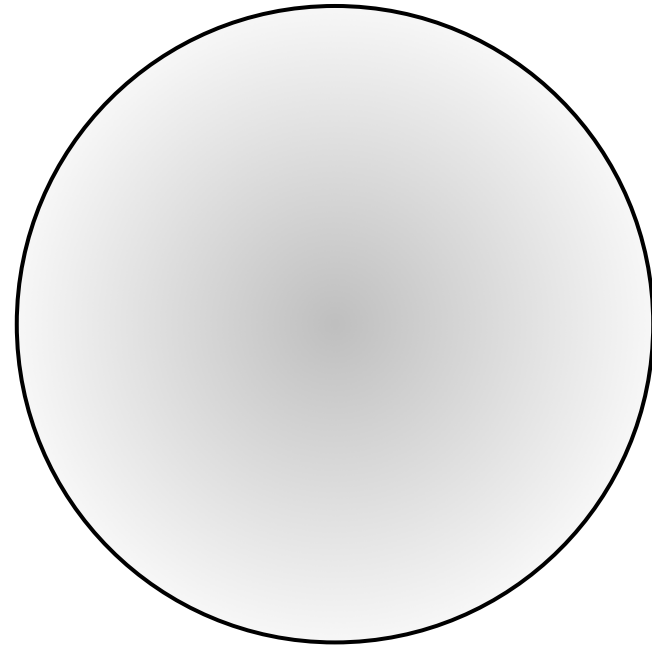
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Real space, r

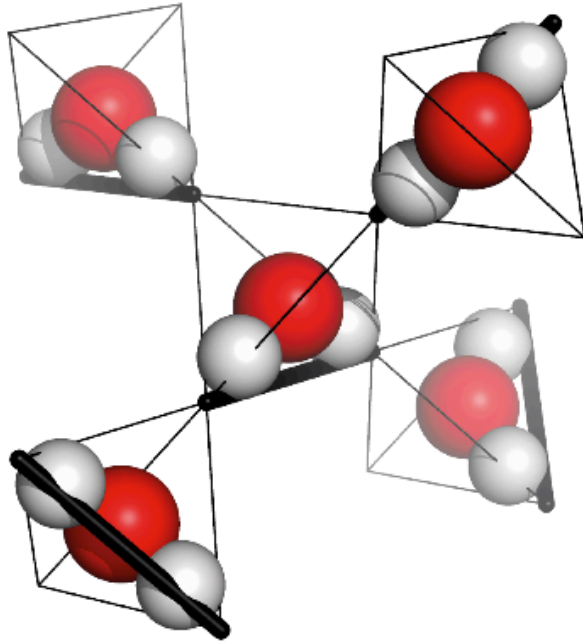
Intensity (arb.)
0  1



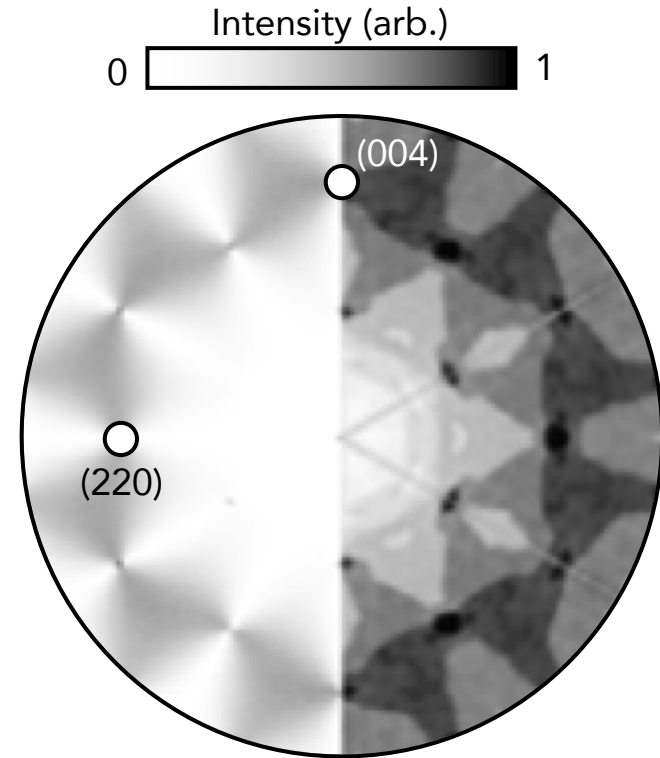
Reciprocal space, Q

Neutron scattering – Order vs disorder

- Correlated disorder \rightarrow structured diffuse scattering



Real space, r

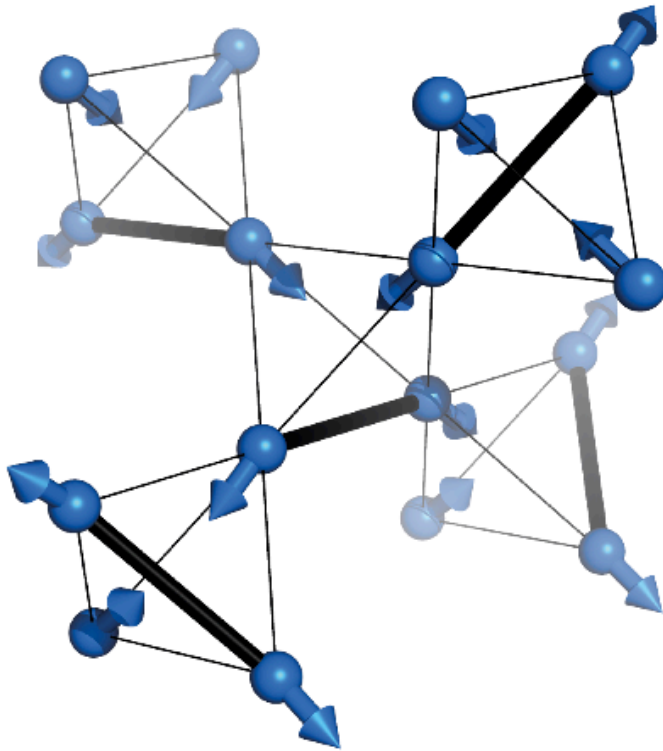


Reciprocal space, Q
Neutron scattering

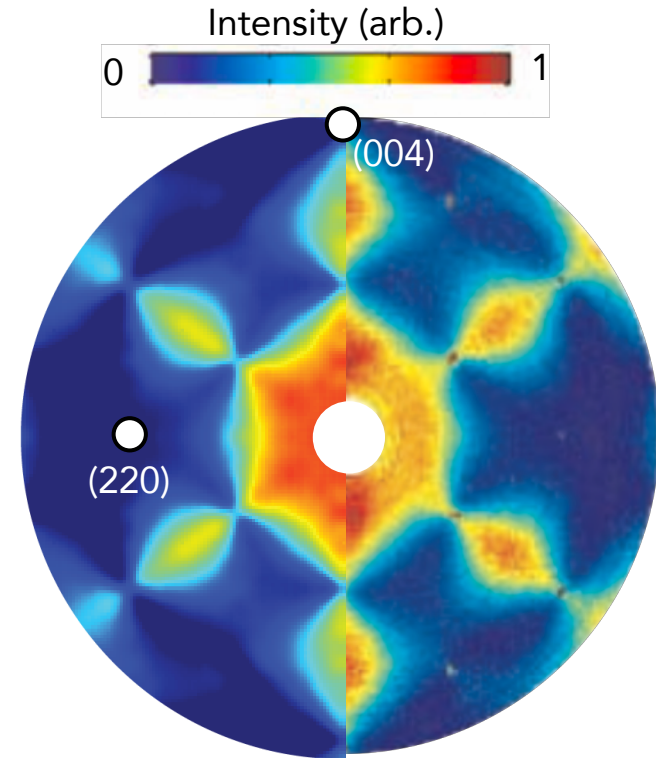
Wehinger *et al.*, *JPCM* 26, 265401 (2014)

Neutron scattering – Order vs disorder

- Correlated disorder \rightarrow structured diffuse scattering



Real space, r

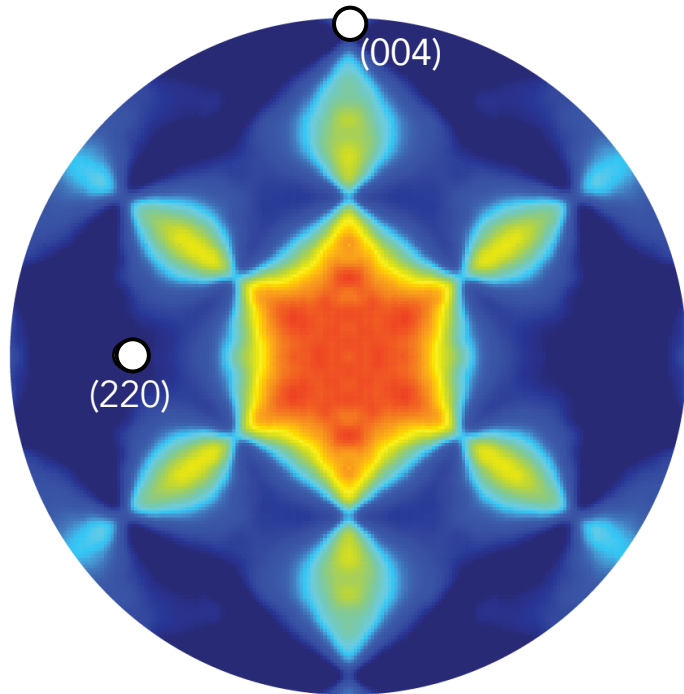


Reciprocal space, Q
Spin-polarised neutron scattering

Fennell *et al.*, *Science* 326, 415 (2009)

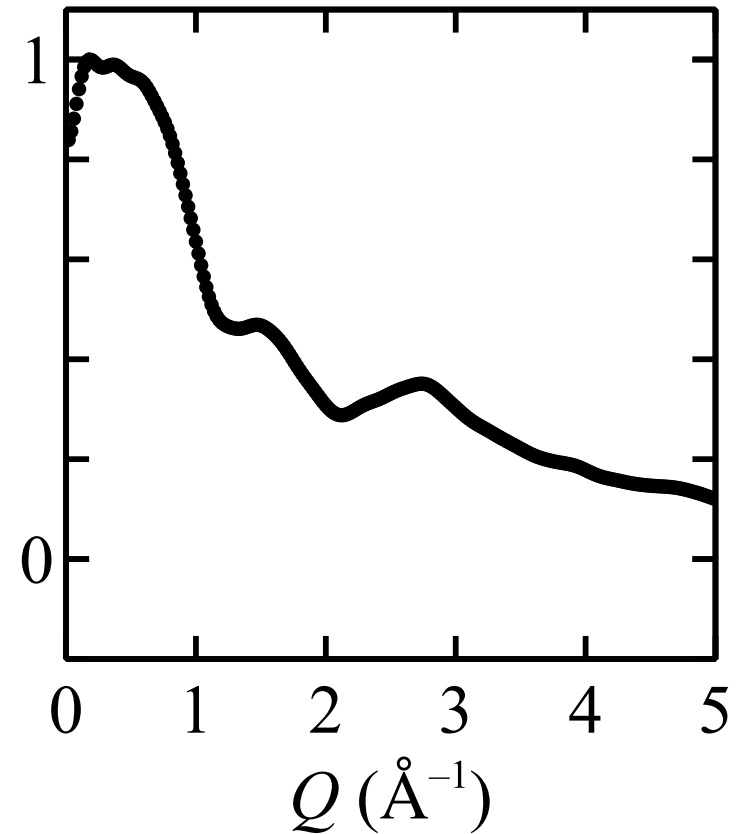
Neutron scattering – Powder vs crystal

single crystal



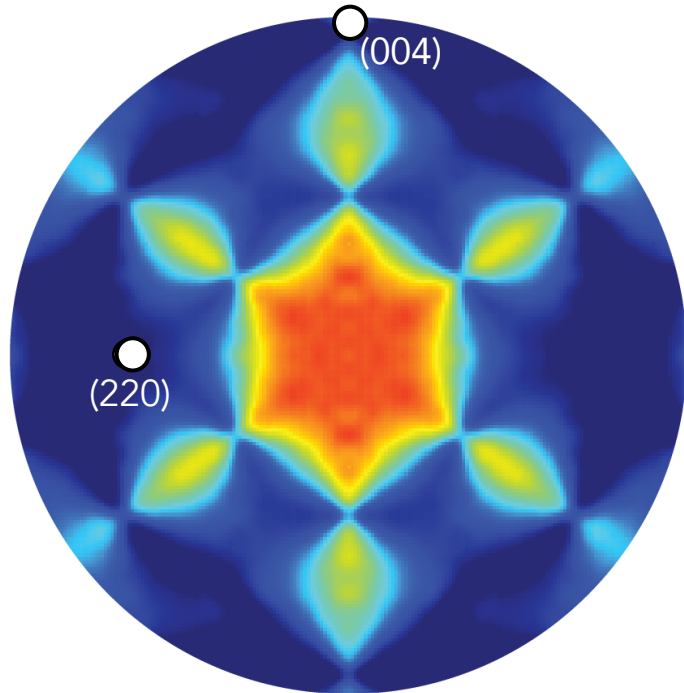
$I(Q)$

powder



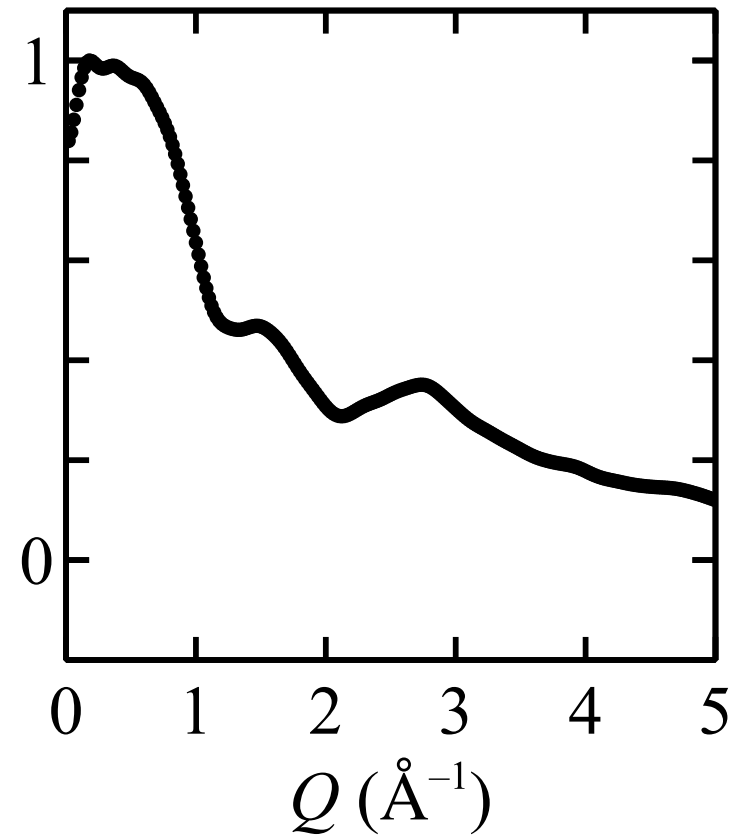
Neutron scattering – Powder vs crystal

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$I(Q)$

powder



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- **Reverse Monte Carlo & Spinvert**
- Powder case study: $\text{Gd}_3\text{Ga}_5\text{O}_{12}$
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Reverse Monte Carlo (RMC) refinement

□ Goodness-of-fit metric:

$$\chi^2 = W \sum_Q \left[\frac{I_{\text{calc}}(Q) - I_{\text{expt}}(Q)}{\sigma(Q)} \right]^2$$

1. Big box: $\sim 10^4$ spin vectors, initially randomised
2. **Rotate** a spin at random

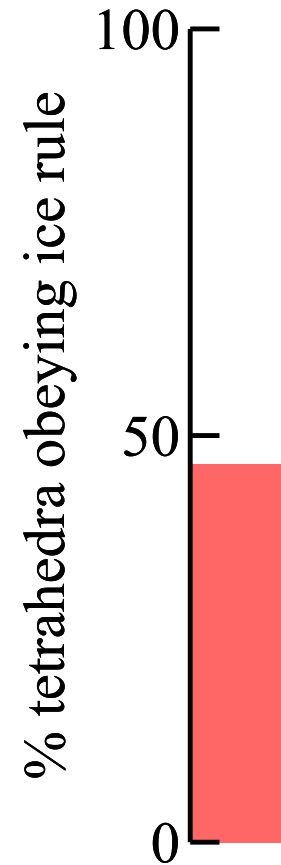
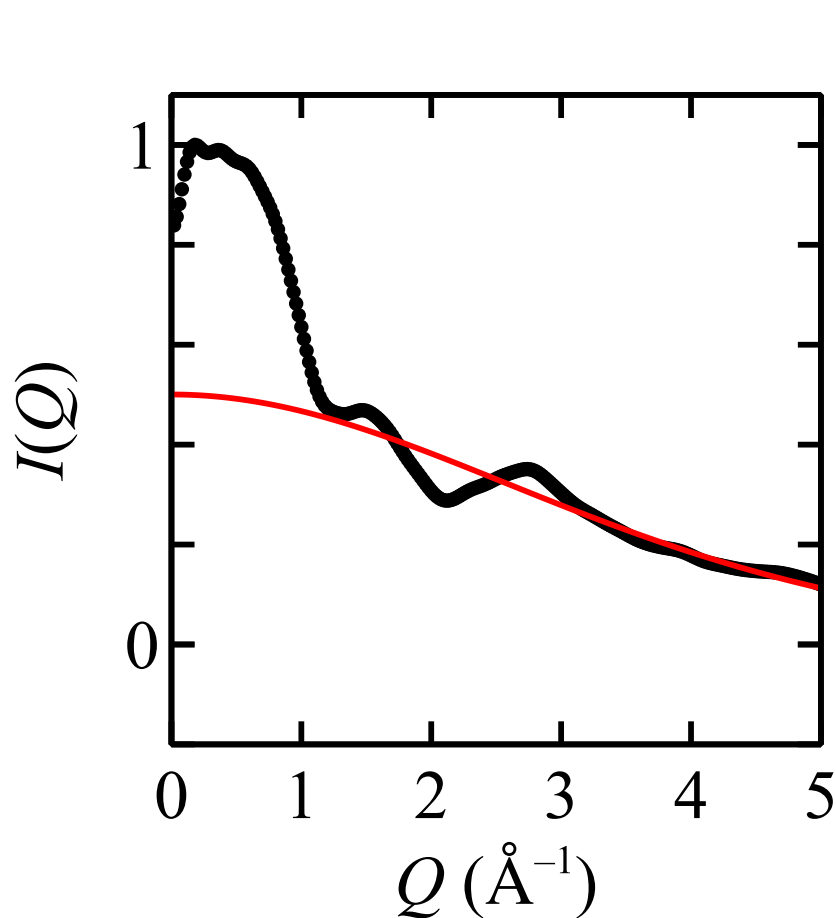
Accept move if $\Delta\chi^2 \leq 0$

Otherwise, accept with probability $\exp(-\Delta\chi^2/2)$

3. **Repeat step 2** until fit achieved
4. **Calculate** diffuse scattering, correlation functions, etc..

Spin ice – Local structure solution

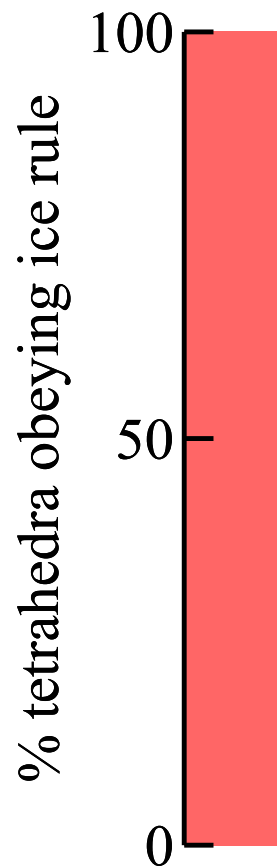
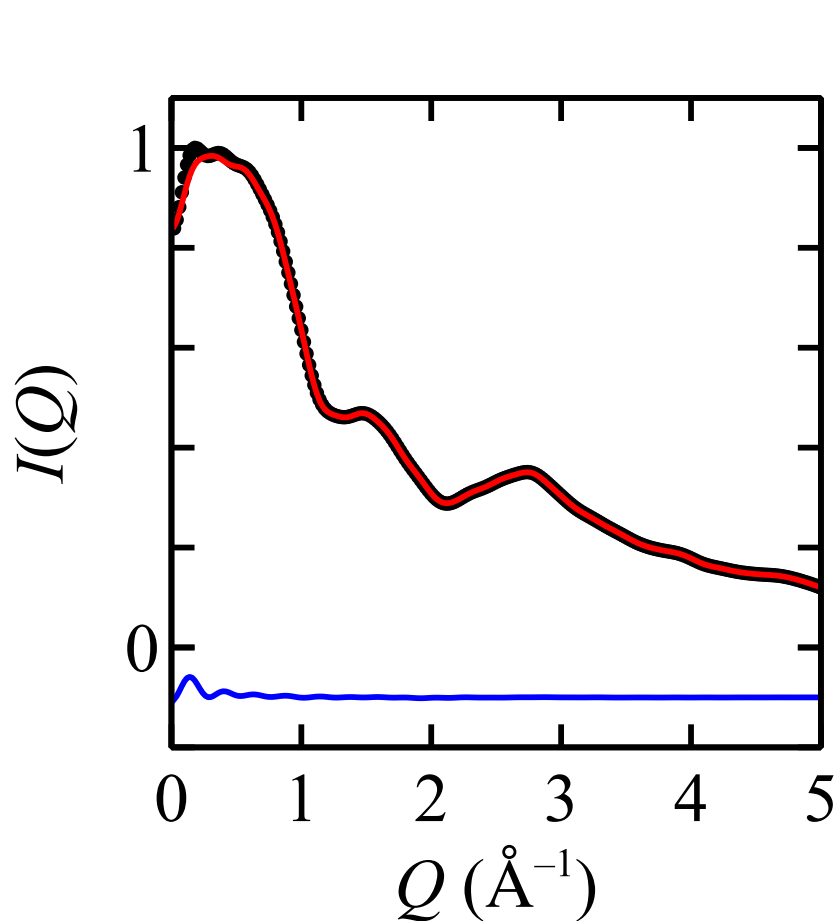
- Reverse Monte Carlo refinement from random initial configurations



Andrew Goodwin
Oxford

Spin ice – Local structure solution

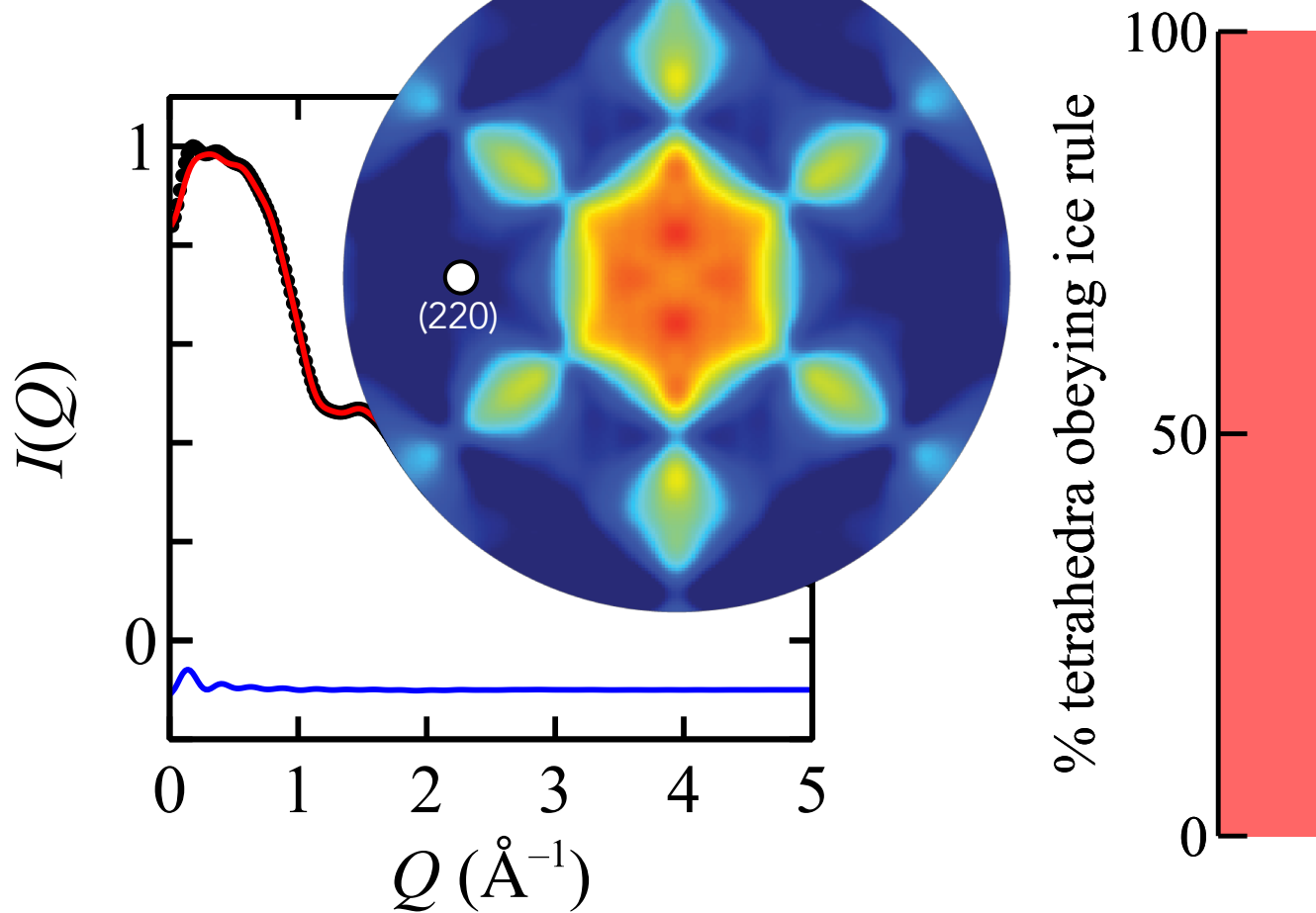
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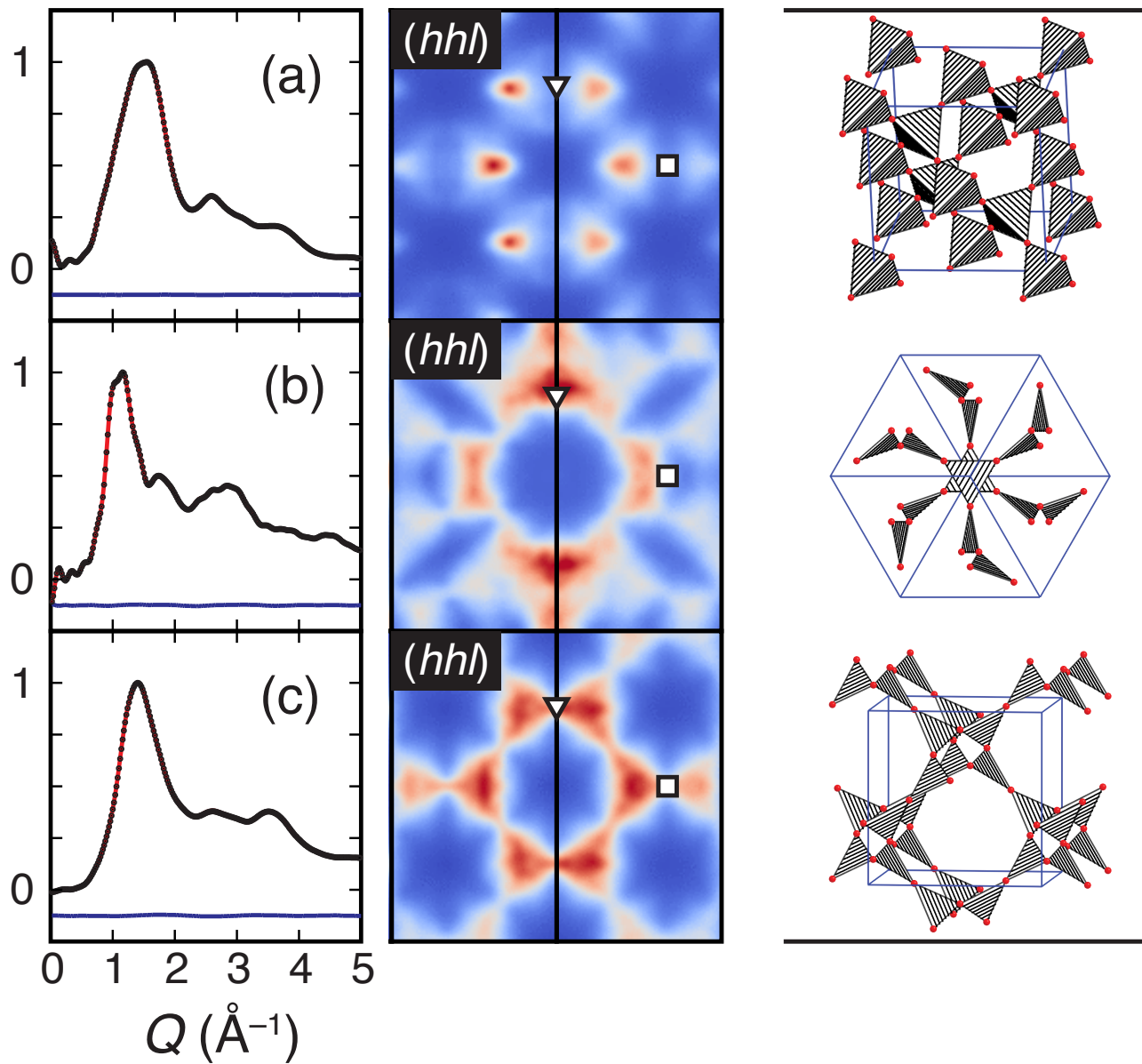
□ Reverse Monte Carlo  Moment from random initial configurations



Andrew Goodwin
Oxford

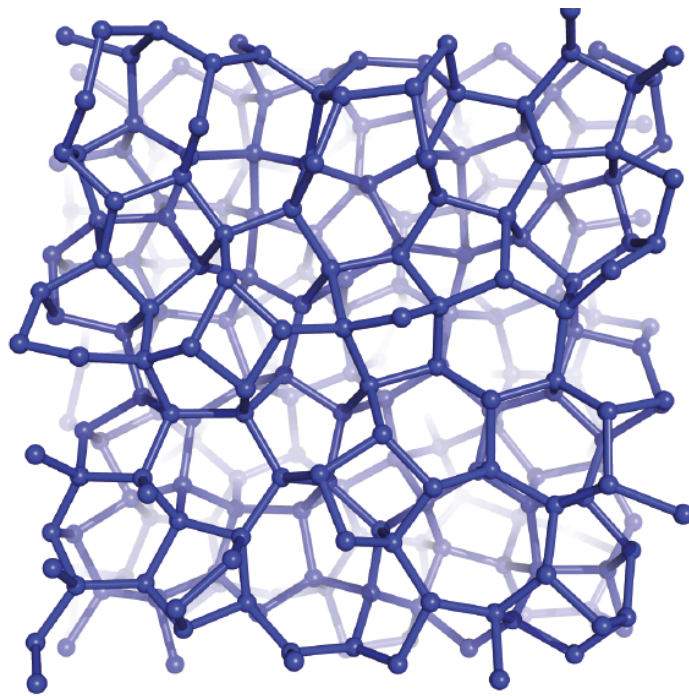
Paddison & Goodwin, *PRL* 108, 017204 (2012)

Exact RMC

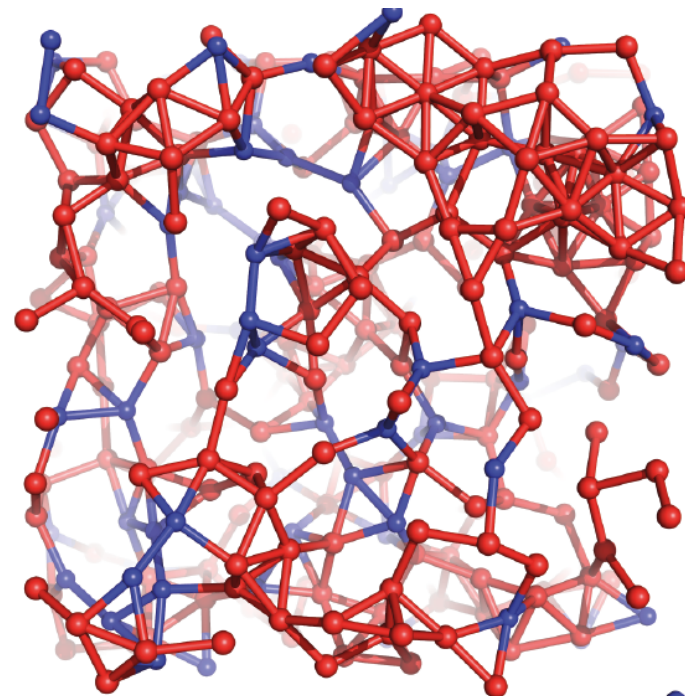


A note of caution

- ❑ RMC produces most disordered configuration consistent with input data and constraints (crystal structure, spin length)
- ❑ Spin liquids more strongly constrained than actual liquids & amorphous systems



a-Si



Spinvert – What does it do?

IOP PUBLISHING

JOURNAL OF PHYSICS: CONDENSED MATTER

J. Phys.: Condens. Matter **25** (2013) 454220 (15pp)

doi:10.1088/0953-8984/25/45/454220

SPINVERT: a program for refinement of paramagnetic diffuse scattering data

Joseph A M Paddison^{1,2}, J Ross Stewart² and Andrew L Goodwin¹

- ❑ Refinement of *atomistic model* to *magnetic diffuse scattering* data
- ❑ “Model independent” – no spin Hamiltonian
- ❑ **Design principles:**
 - Easy to use
 - Fast to run
 - Straightforward to customise

Paddison, Stewart & Goodwin, *J. Phys.: Condens. Matter* **25**, 454220 (2013)

Spinvert – What doesn't it do?

IOP PUBLISHING

JOURNAL OF PHYSICS: CONDENSED MATTER

J. Phys.: Condens. Matter **25** (2013) 454220 (15pp)

[doi:10.1088/0953-8984/25/45/454220](https://doi.org/10.1088/0953-8984/25/45/454220)

SPINVERT: a program for refinement of paramagnetic diffuse scattering data

Joseph A M Paddison^{1,2}, J Ross Stewart² and Andrew L Goodwin¹

- Magnetic diffuse scattering *only*
- No positional disorder, no magneto-elastic coupling
- Single type of magnetic ion

Paddison, Stewart & Goodwin, *J. Phys.: Condens. Matter* **25**, 454220 (2013)

Spinvert – How to get it?

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JOURNAL OF PHYSICS: CONDENSED MATTER

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SPINVERT: a program for refinement of paramagnetic diffuse scattering data

Joseph A M Paddison^{1,2}, J Ross Stewart² and Andrew L Goodwin¹

paddisongroup.wordpress.com/software

- ❑ Program, instructions, examples

- ❑ Distributed as Fortran90 source code
 - Needs to be compiled on your system
 - Download compiler from gcc.gnu.org/wiki/GFortranBinaries
 - `gfortran spinvert.f90 -o spinvert -O3`

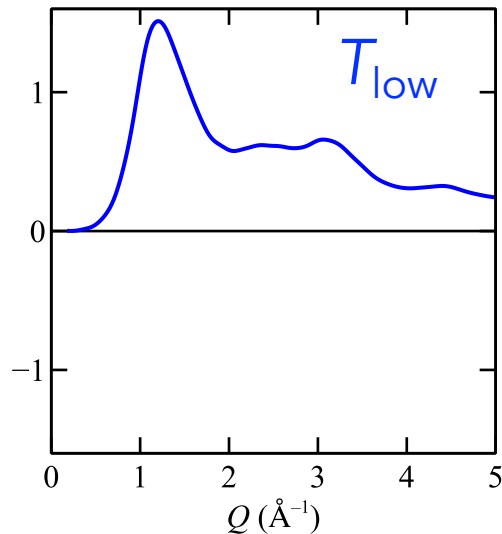
Paddison, Stewart & Goodwin, *J. Phys.: Condens. Matter* **25**, 454220 (2013)

Spinvert – How to get suitable data?

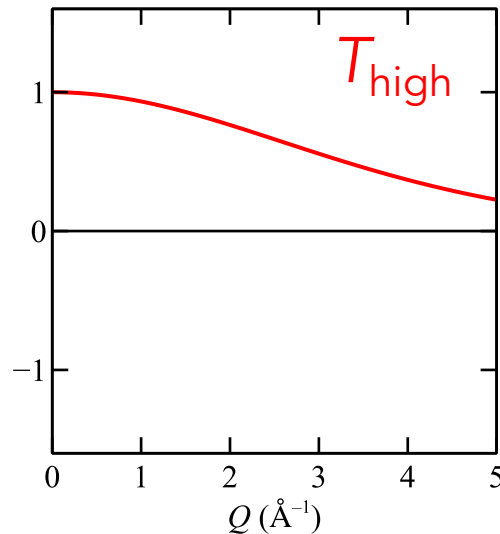
□ **Key challenge:** isolating magnetic diffuse scattering

□ **Three main methods:**

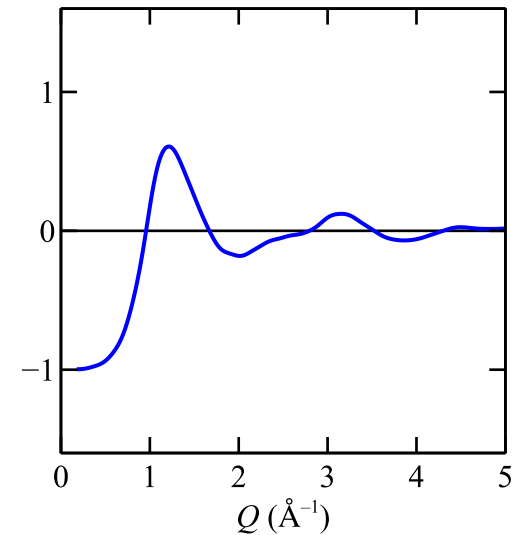
1. Polarised neutrons → e.g. D7 at ILL
2. “Total scattering” → Matt Tucker & Helen Playford’s talk
3. Temperature subtractions → **special requirements for Spinvert:**



—



=



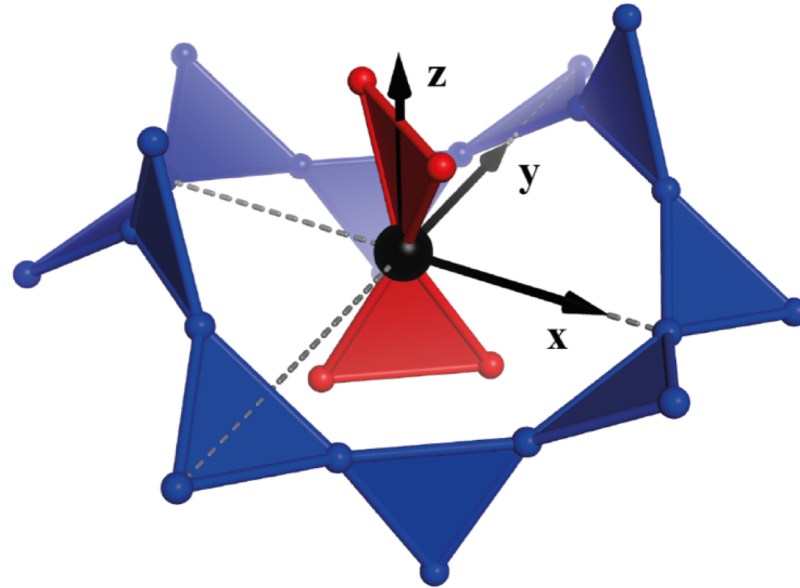
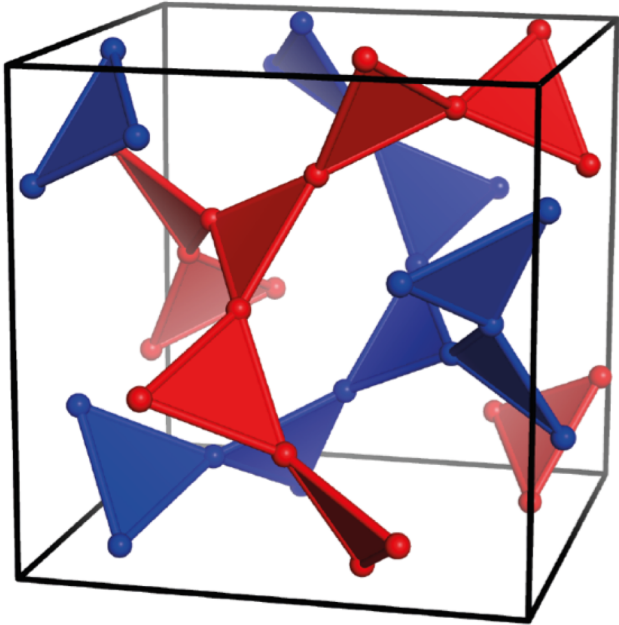
- place data on absolute intensity scale ($\text{barn sr}^{-1} \text{spin}^{-1}$)
- measure magnetic moment length

Plan

- Introduction
- Magnetic neutron scattering
- Reverse Monte Carlo & Spinvert
- **Powder case study: $\text{Gd}_3\text{Ga}_5\text{O}_{12}$**
- Single-crystal refinements

Gd₃Ga₅O₁₂ – Structure

- Interpenetrating networks of corner-sharing triangles in 3D
- Antiferromagnetic interactions of strength ~2 K



Pascale Deen
(ESS/Lund)

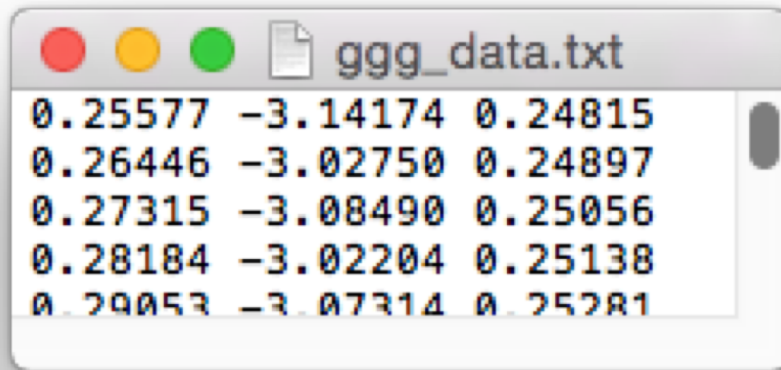


Henrik Jacobsen
(Copenhagen)

Kinney & Wolf, *J. Appl. Phys.* 50, 2115 (1979)
Yavors'kii, Enjalran & Gingras, *PRL* 97, 267203 (2006)

Gd₃Ga₅O₁₂ – Experimental data

Input file: "name_data.txt"



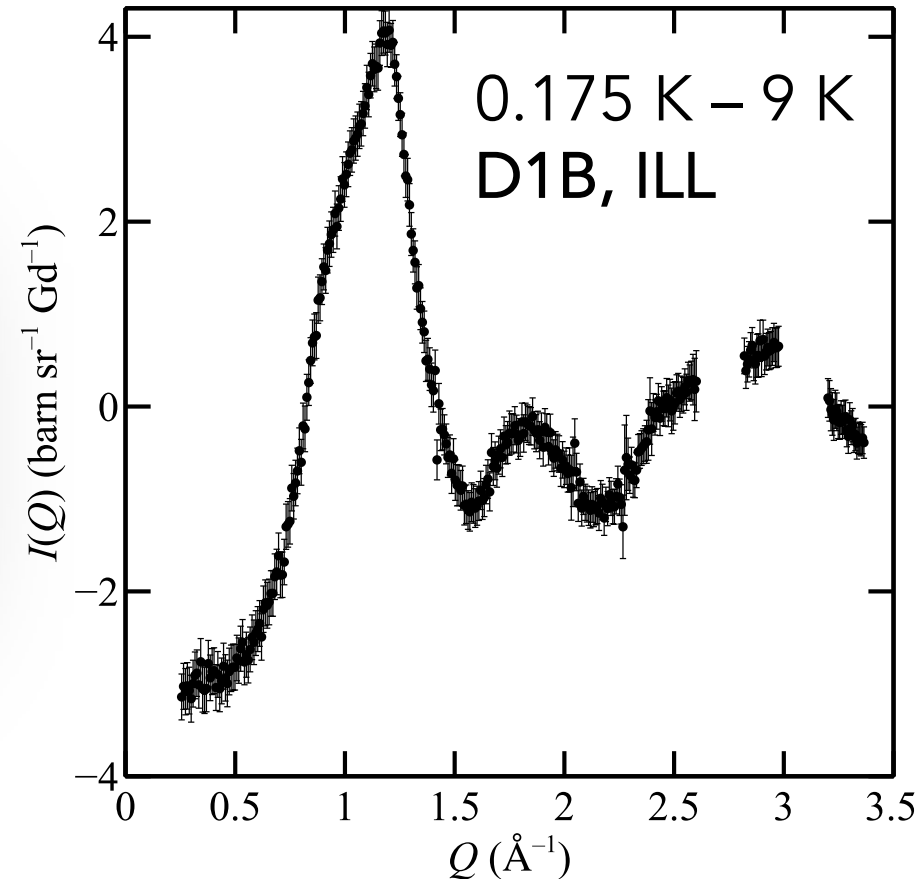
A screenshot of a text editor window titled "ggg_data.txt". The window contains five lines of data, each with three columns of numbers. The data is as follows:

Q (Å ⁻¹)	Intensity (bn sr ⁻¹ spin ⁻¹)	Error
0.25577	-3.14174	0.24815
0.26446	-3.02750	0.24897
0.27315	-3.08490	0.25056
0.28184	-3.02204	0.25138
0.29053	-3.07314	0.25281

Q
(Å⁻¹)

Intensity
(bn sr⁻¹ spin⁻¹)

Error



Gd₃Ga₅O₁₂ – Config file

```
gfg_config.txt – Edited v
TITLE gfg
CELL 12.349 12.349 12.349 90.0 90.0 90.0
SITE 0.1250 0.0000 0.2500
SITE 0.6250 0.5000 0.7500
SITE 0.2500 0.1250 0.0000
SITE 0.7500 0.6250 0.5000
SITE 0.0000 0.2500 0.1250
SITE 0.5000 0.7500 0.6250
SITE 0.6250 0.0000 0.2500
SITE 0.1250 0.5000 0.7500
SITE 0.7500 0.1250 0.5000
SITE 0.2500 0.6250 0.0000
SITE 0.5000 0.2500 0.3750
SITE 0.0000 0.7500 0.8750
SITE 0.3750 0.5000 0.2500
SITE 0.8750 0.0000 0.7500
SITE 0.5000 0.7500 0.1250
SITE 0.0000 0.2500 0.6250
SITE 0.8750 0.5000 0.2500
SITE 0.3750 0.0000 0.7500
SITE 0.0000 0.7500 0.3750
SITE 0.5000 0.2500 0.8750
SITE 0.2500 0.3750 0.5000
SITE 0.7500 0.8750 0.0000
SITE 0.2500 0.8750 0.5000
SITE 0.7500 0.3750 0.0000
FORM_FACTOR_J0 0.0186 25.3867 0.2895 11.1421 0.7135 3.7520 -0.0217
SPIN_DIMENSION 3
TEMP_SUBTRACT
SCALE 63.0
WEIGHT 500.0
BOX 6 6 6
MOVES 300
```

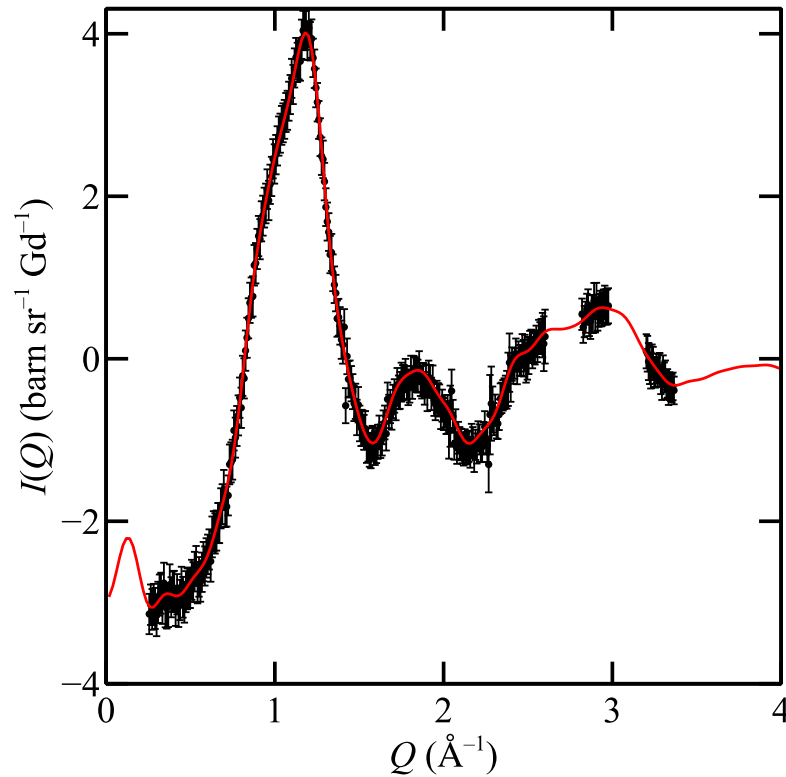
- ❑ “name_config.txt”
- ❑ List of **keywords** followed by **values**
- ❑ Keywords can be in any order

$$\text{Scale} = g^2 S(S + 1)$$

$$\chi^2 = W \sum_Q \left[\frac{I_{\text{calc}}(Q) - I_{\text{expt}}(Q)}{\sigma(Q)} \right]^2$$

Gd₃Ga₅O₁₂ – Fit

- ❑ Output file: "name_fit_01.txt"
- ❑ Calculate powder pattern over extended Q -range to check results "make sense"



Gd₃Ga₅O₁₂ – Spins file

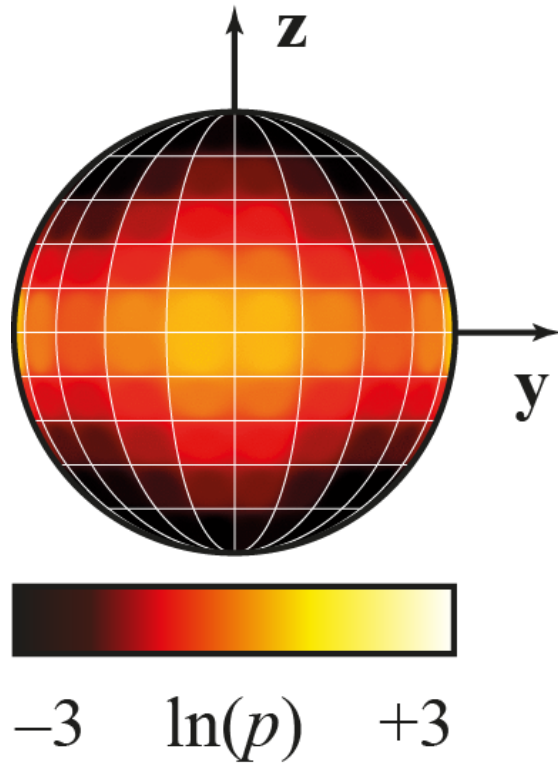
- ❑ Output file: "name_spins_01.txt"
- ❑ Spin orientations and metadata

```
ggg_spins_01.txt
TITLE ggg
CELL 12.349000000000000 12.349000000000000 12.349000000000000 90.0000000 90.0000000 90.0000000
SITE 0.12500000000000000 0.00000000000000000 0.25000000000000000
SITE 0.62500000000000000 0.50000000000000000 0.75000000000000000
SITE 0.25000000000000000 0.12500000000000000 0.00000000000000000
SITE 0.75000000000000000 0.62500000000000000 0.50000000000000000
SITE 0.00000000000000000 0.25000000000000000 0.12500000000000000
SITE 0.50000000000000000 0.75000000000000000 0.62500000000000000
SITE 0.62500000000000000 0.00000000000000000 0.25000000000000000
SITE 0.12500000000000000 0.50000000000000000 0.75000000000000000
SITE 0.75000000000000000 0.12500000000000000 0.50000000000000000
SITE 0.25000000000000000 0.62500000000000000 0.00000000000000000
SITE 0.50000000000000000 0.25000000000000000 0.37500000000000000
SITE 0.00000000000000000 0.75000000000000000 0.87500000000000000
SITE 0.37500000000000000 0.50000000000000000 0.25000000000000000
SITE 0.87500000000000000 0.00000000000000000 0.75000000000000000
SITE 0.50000000000000000 0.75000000000000000 0.12500000000000000
SITE 0.00000000000000000 0.25000000000000000 0.62500000000000000
SITE 0.87500000000000000 0.50000000000000000 0.25000000000000000
SITE 0.37500000000000000 0.00000000000000000 0.75000000000000000
SITE 0.00000000000000000 0.75000000000000000 0.37500000000000000
SITE 0.50000000000000000 0.25000000000000000 0.87500000000000000
SITE 0.25000000000000000 0.37500000000000000 0.50000000000000000
SITE 0.75000000000000000 0.87500000000000000 0.00000000000000000
SITE 0.25000000000000000 0.87500000000000000 0.50000000000000000
SITE 0.75000000000000000 0.37500000000000000 0.00000000000000000
BOX 6 6 6
FORM_FACTOR_J0 1.8599999999999998E-002 25.3867000000000001 0.28949999999999999 11.142099999999999 0.71350000000000002
3.7519999999999998 -2.17000000000000001E-002
PROPOSED_MOVES 886464
ACCEPTED_MOVES 398957
WEIGHT 500.000000000000000
TEMP_SUBTRACT
CHI_SQUARED 69.073821040774575
R_FACTOR 6.4884619747326413
SCALE 63.000000000000000
FLAT_BACKGROUND 0.00000000000000000
LINEAR_BACKGROUND 0.00000000000000000
SPIN 1 0 0 0 0.82264674345196132 -0.56685015688850382 -4.3968569721580822E-002
SPIN 2 0 0 0 0.95521777682432363 -8.8001464444131025E-002 0.28251502808609136
SPIN 3 0 0 0 -0.73250525848391879 0.18794069290076534 -0.65430447212699649
SPIN 4 0 0 0 -0.52705374016138040 0.84962067581191258 1.8948937036386431E-002
```

$\text{Gd}_3\text{Ga}_5\text{O}_{12}$ – Analysing the results

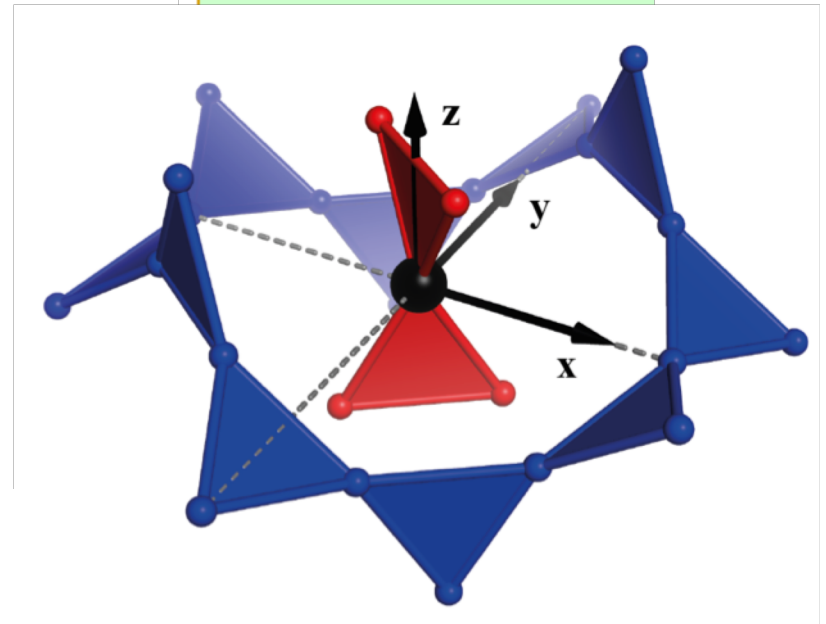
Single spins

□ “Spinplot” program



Gd^{3+} site symmetry
from International Tables:

24	<i>c</i>	2.22
----	----------	------



$Gd_3Ga_5O_{12}$ – Analysing the results

Single spins

VOLUME 92, NUMBER 16

PHYSICAL REVIEW LETTERS

week ending
23 APRIL 2004

Planar Spin Fluctuations with a Quadratic Thermal Dependence Rate in Spin Liquid $Gd_3Ga_5O_{12}$

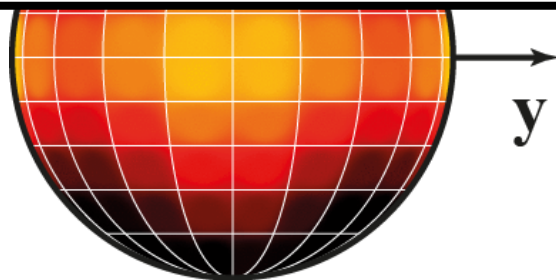
P. Bonville and J. A. Hodges

C.E.A., Centre d'Etudes de Saclay, Service de Physique de l'Etat Condensé, 91191 Gif-sur-Yvette, France

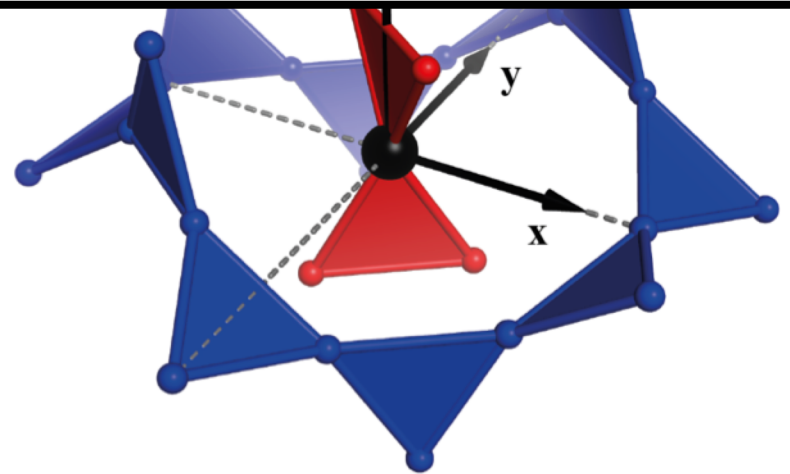
J. P. Sanchez and P. Vulliet

C.E.A., Centre d'Etudes de Grenoble, Service de Physique Statistique, Magnétisme et Supraconductivité, 38054 Grenoble, France

(Received 10 November 2003; published 23 April 2004)



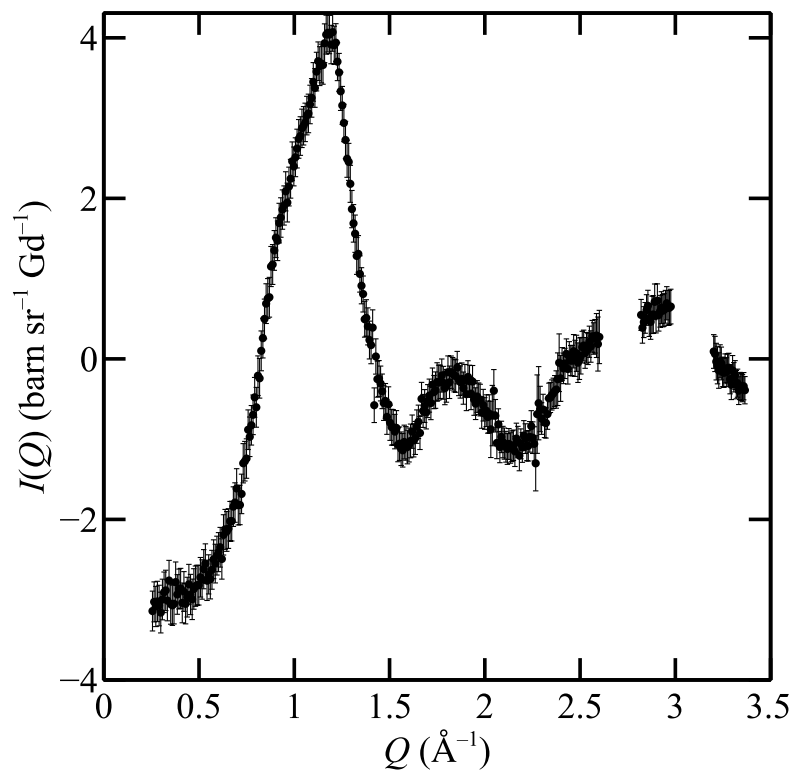
-3 $\ln(p)$ $+3$



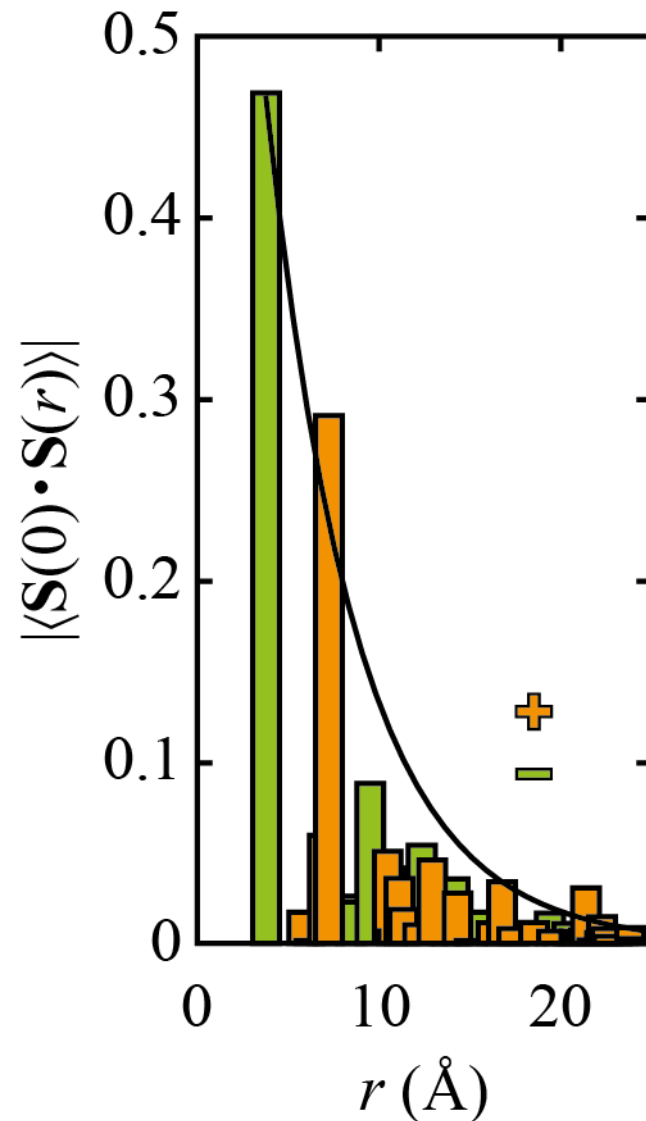
Gd₃Ga₅O₁₂ – Analysing the results

Spin correlations

□ “Spincorrel” program



“Fourier transform”



Gd₃Ga₅O₁₂ – Analysing the results

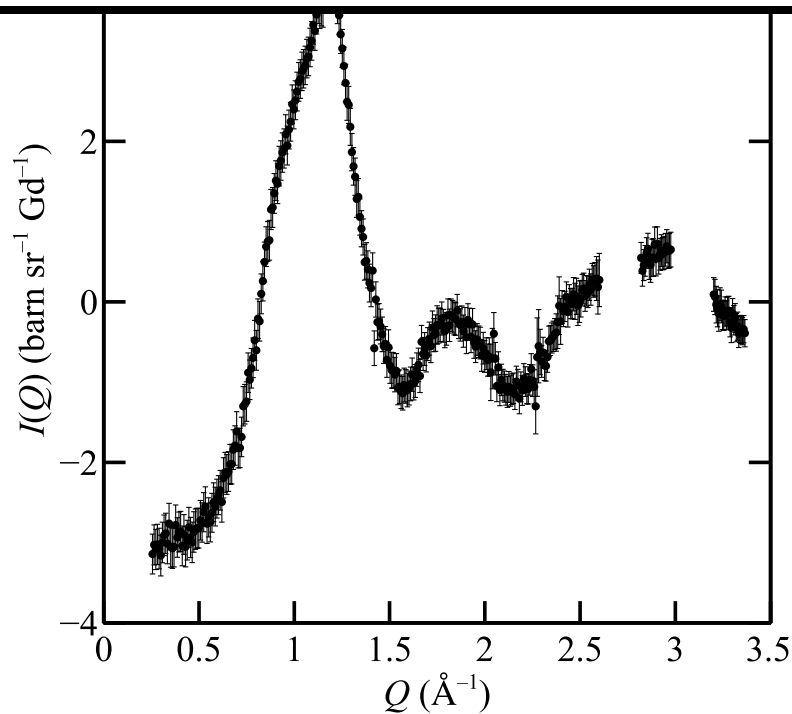
Spin correlations

Acta Crystallographica Section A
**Foundations and
Advances**

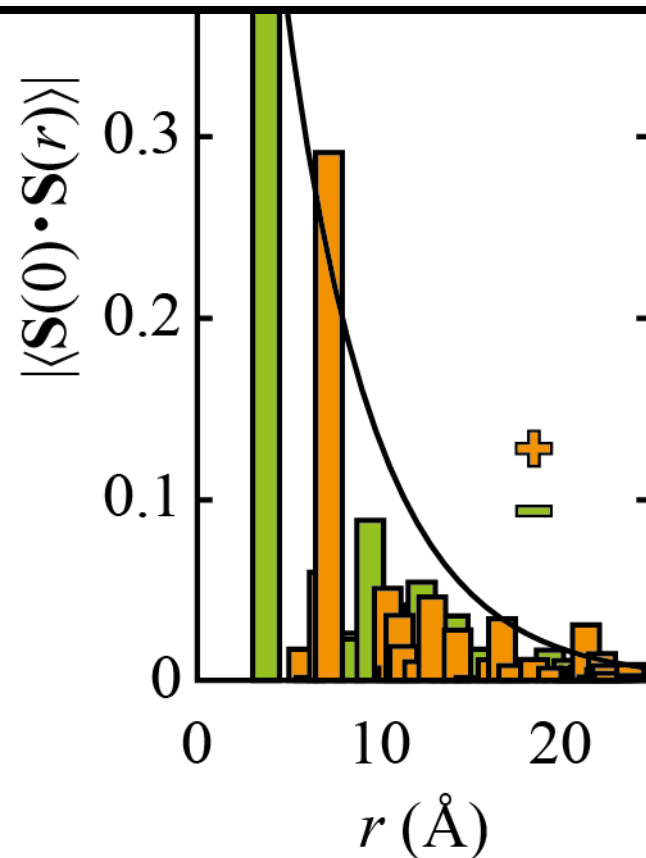
ISSN 2053-2733

Magnetic pair distribution function analysis of local magnetic correlations

Benjamin A. Frandsen,^a Xiaohao Yang^b and Simon J. L. Billinge^{b,c*}

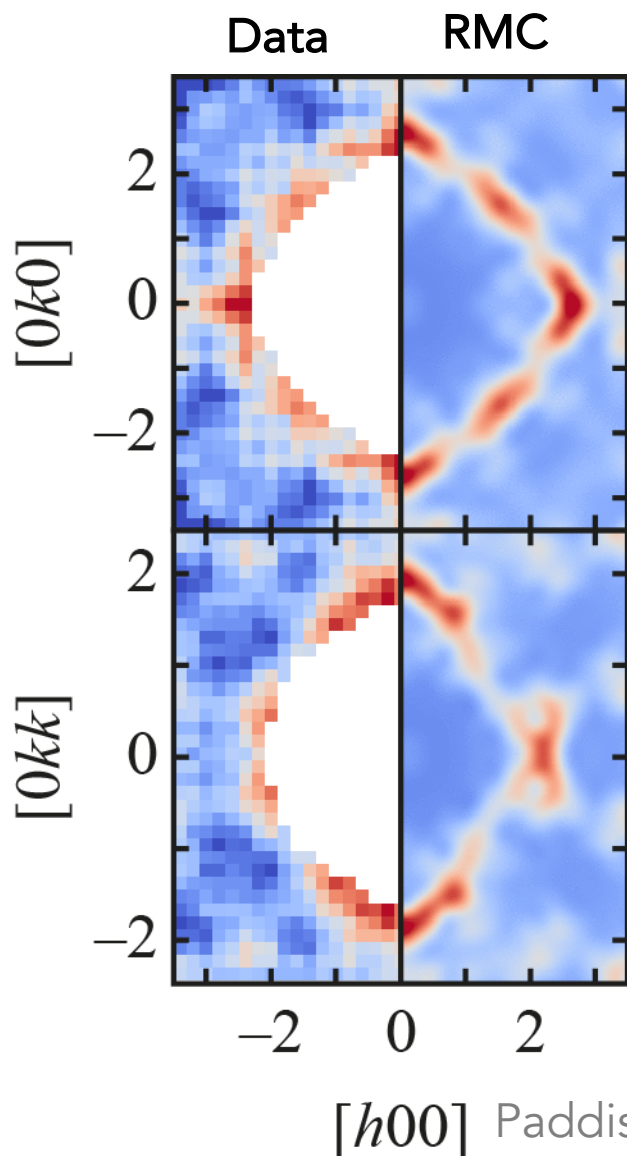


“Fourier
transform”



Gd₃Ga₅O₁₂ – Analysing the results

Single-crystal scattering



- "Scatty" program
- Average single-crystal calculation over >10 boxes
- Input file: scatty_config.txt

```
NAME hh1
X_AXIS 3 3 0 50
Y_AXIS 0 0 4 50
Z_AXIS 0 0 0 1

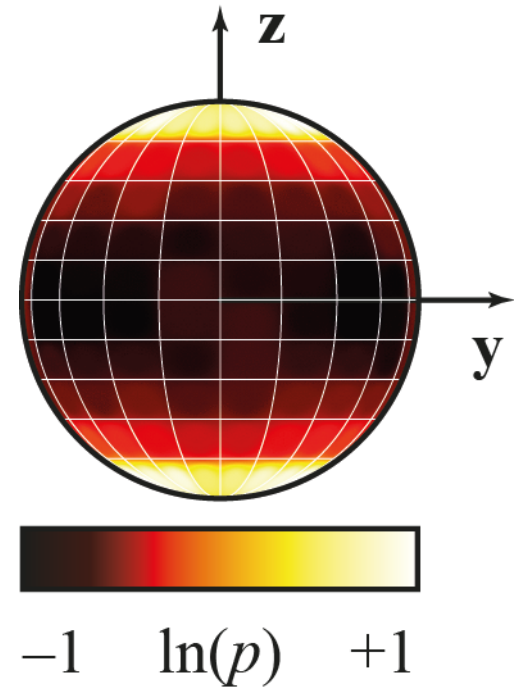
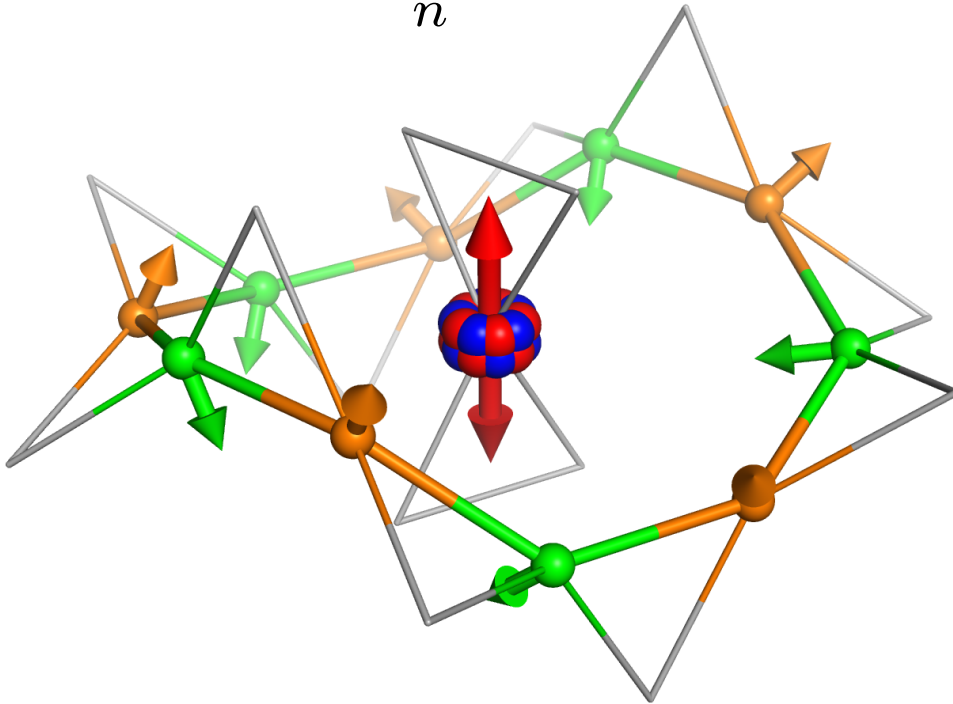
SYMMETRY m-3m
RADIATION N|
```

- Data at $T = 0.175$ K (D9, ILL)

Gd₃Ga₅O₁₂ – Going further

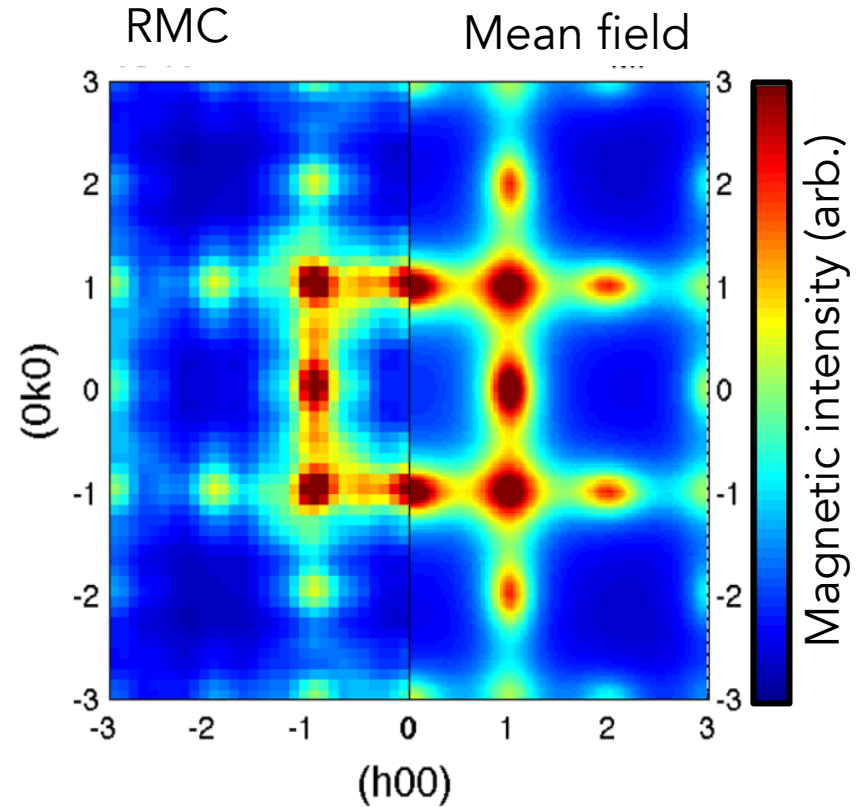
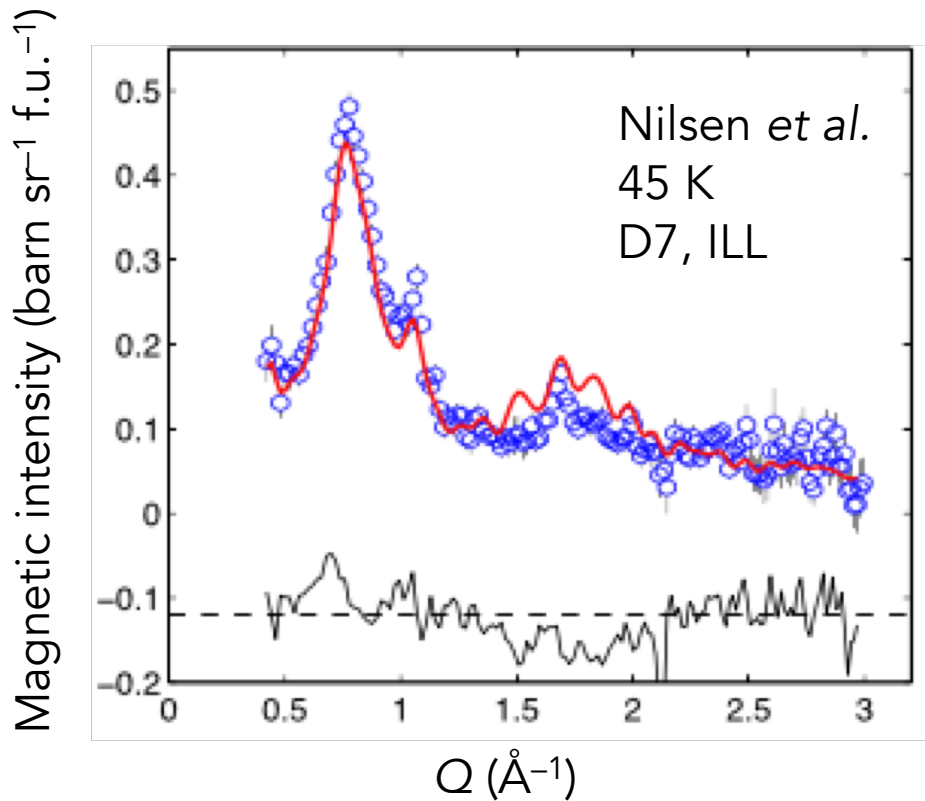
Collective effects

$$\mathbf{L}(\mathbf{r}) = \frac{1}{10} \sum_n \cos(n\pi) \mathbf{S}_n(\mathbf{r})$$



Ba₂YRuO₆ – Another example

- ❑ Double perovskite structure (FCC magnetic lattice)
- ❑ Compare RMC results with J_1 - J_2 spin Hamiltonian



Plan

- Introduction
- Magnetic neutron scattering
- Reverse Monte Carlo & Spinvert
- Powder case study: $\text{Gd}_3\text{Ga}_5\text{O}_{12}$
- **Single-crystal refinements**

Spinvert-3D – Single-crystal refinements

- ❑ “Spinvert-3D” for 3D refinements is available
- ❑ Beta version – please let me know any bugs!

PHYSICAL REVIEW B **97**, 014429 (2018)

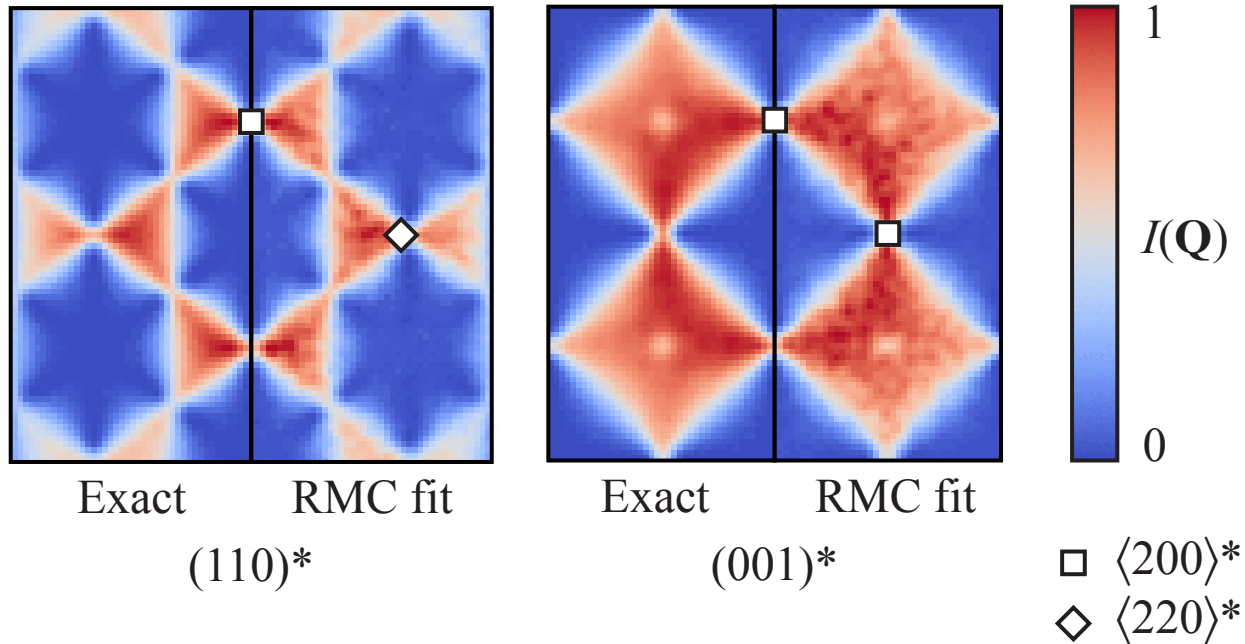
Magnetic structure of paramagnetic MnO

Joseph A. M. Paddison,^{1,2,3,4} Matthias J. Gutmann,² J. Ross Stewart,² Matthew G. Tucker,^{2,5,6} Martin T. Dove,⁷
David A. Keen,² and Andrew L. Goodwin^{1,*}

Paddison *et al.*, *PRB* **97**, 014429 (2018)

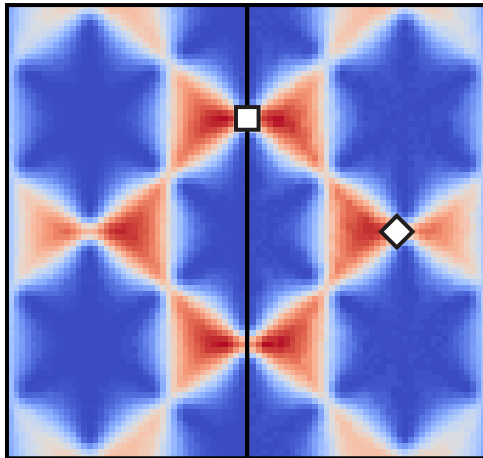
Spinvert-3D – Proof of principle

- Fit to simulated single-crystal data for a model frustrated magnet (Heisenberg spins on pyrochlore lattice with AF interactions)
- First**, fit to **volume** of reciprocal space (~500,000 data points)



Spinvert-3D – Proof of principle

- Fit to simulated single-crystal data for a model frustrated magnet
(Heisenberg spins on pyrochlore lattice with AF interactions)
- Second**, fit to **only (110)* plane** of reciprocal space



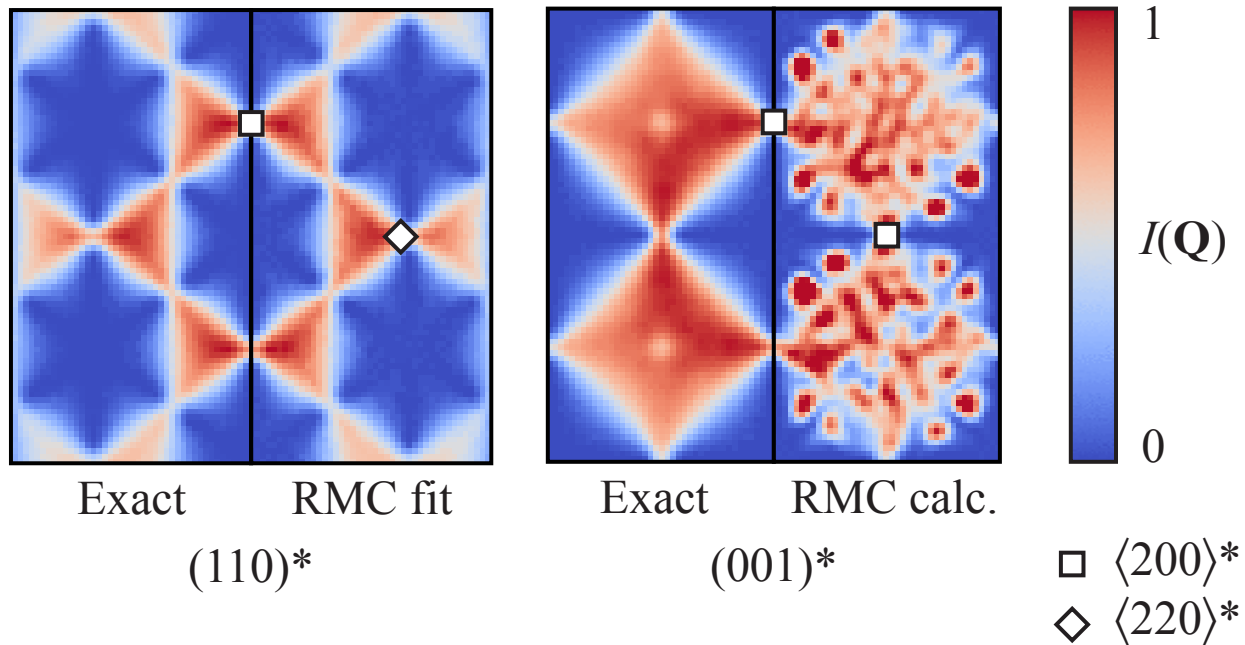
Exact

RMC fit

$(110)^*$

Spinvert-3D – Proof of principle

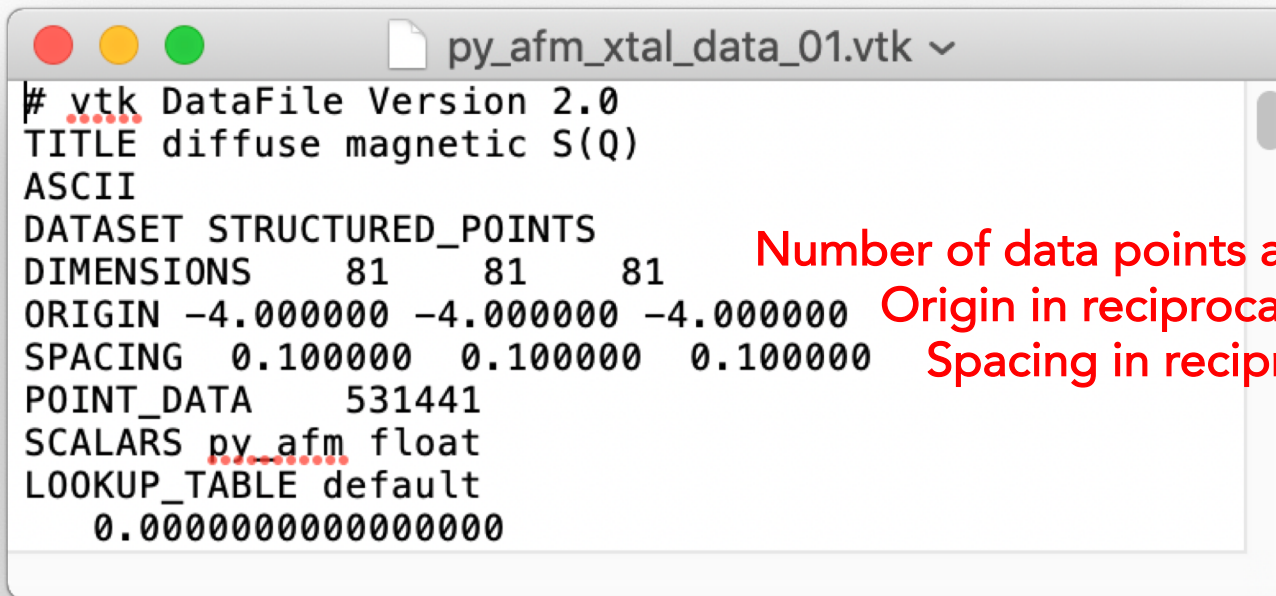
- Fit to simulated single-crystal data for a model frustrated magnet (Heisenberg spins on pyrochlore lattice with AF interactions)
- Second**, fit to **only (110)* plane** of reciprocal space



- Conclusion:** Spinvert-3D works best with a large volume of data!

Spinvert-3D – Data file

- ❑ Input file: “*name_xtal_data.vtk*”
- ❑ Visualization Toolkit (.vtk) format
 - Readable in 3D display software, e.g. **ParaView**



```
# vtk DataFile Version 2.0
TITLE diffuse magnetic S(Q)
ASCII
DATASET STRUCTURED_POINTS
DIMENSIONS 81 81 81
ORIGIN -4.000000 -4.000000 -4.000000
SPACING 0.100000 0.100000 0.100000
POINT_DATA 531441
SCALARS py_afm float
LOOKUP_TABLE default
0.000000000000000000
```

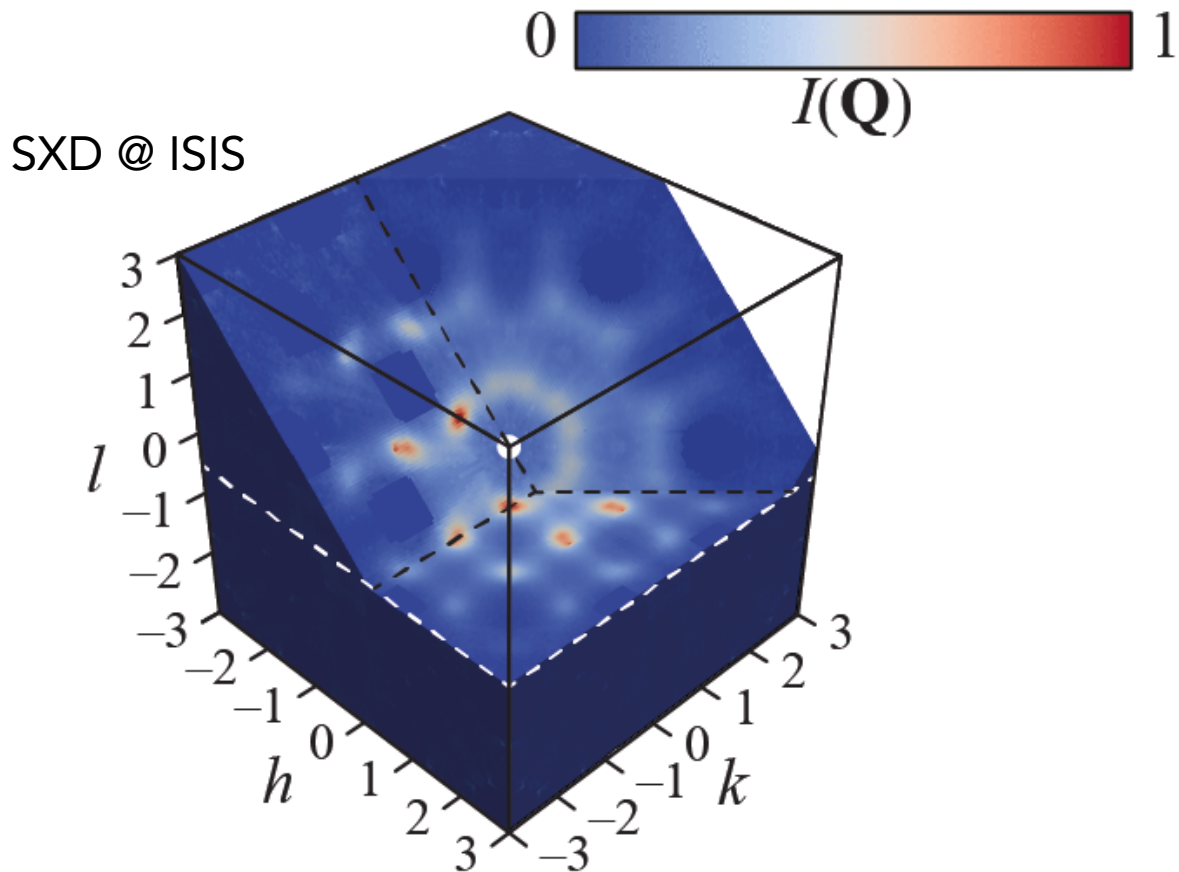
Number of data points along each axis

Origin in reciprocal-lattice (*hkl*) units

Spacing in reciprocal-lattice (*hkl*) units

Spinvert-3D – Paramagnetic MnO

- Rock-salt structure, antiferromagnetic $T_N = 118$ K

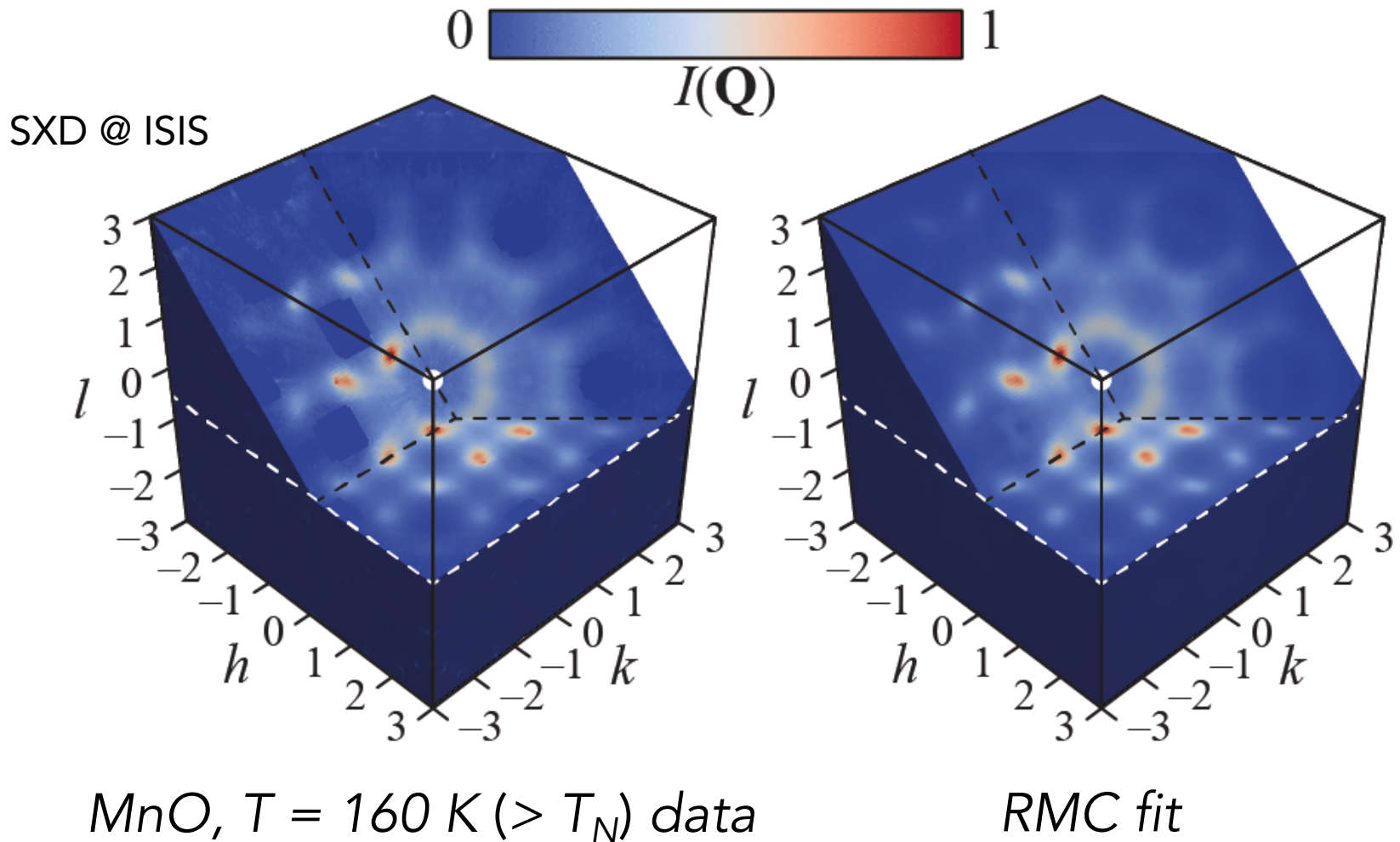


MnO, $T = 160$ K ($> T_N$) data

Paddison *et al.*, *PRB* **97**, 014429 (2018)

Spinvert-3D – Paramagnetic MnO

- Exploit information content of 3D scattering data

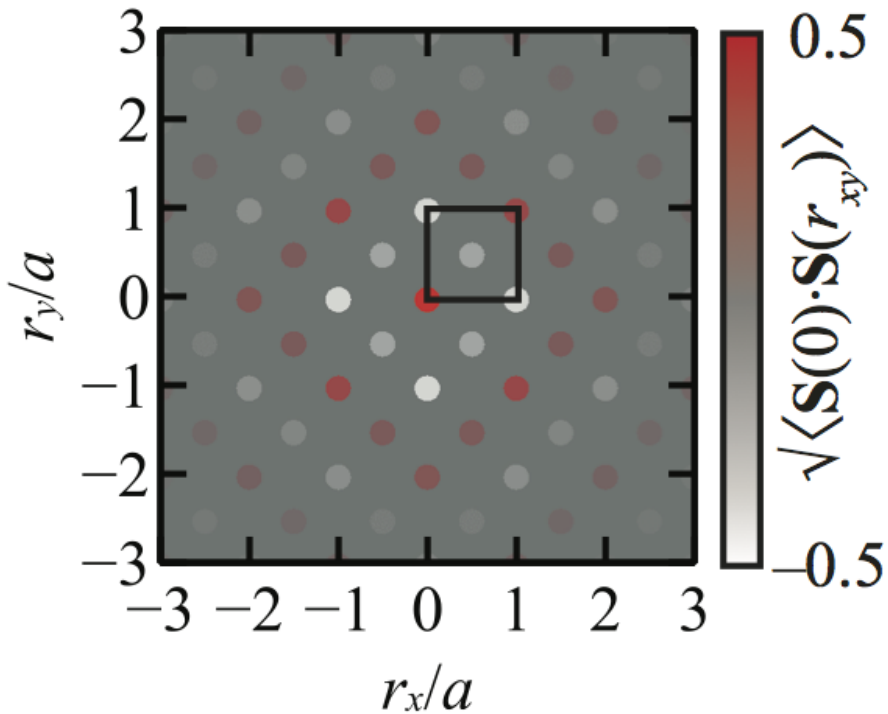


Paddison *et al.*, *PRB* **97**, 014429 (2018)

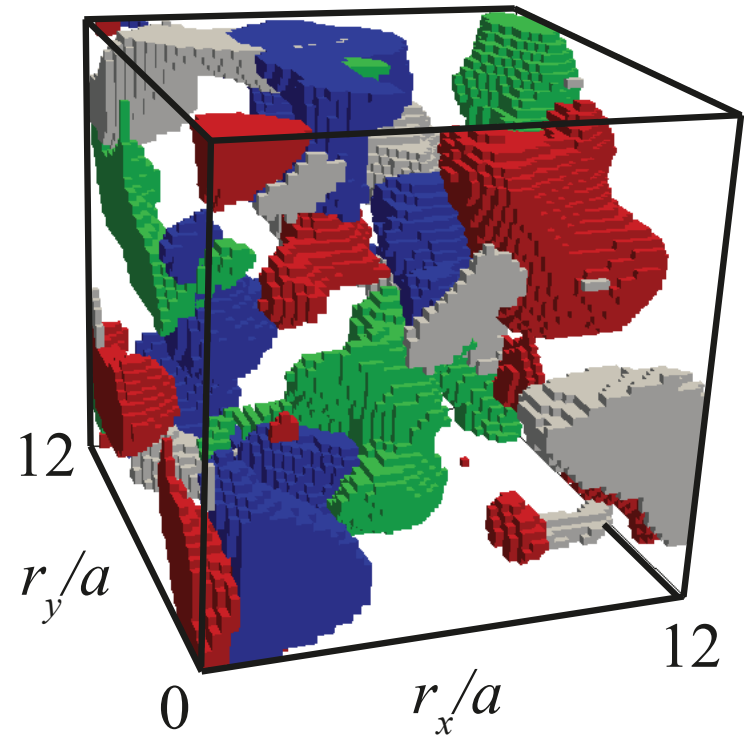
Spininvert-3D – Paramagnetic MnO

- Extract 3D model of domain structure in paramagnetic phase

$$S_{\mathbf{k}}(\mathbf{r}) = \left| \sum_i w(|\mathbf{r} - \mathbf{r}_i|) \mathbf{S}_i \exp\left(i\frac{2\pi}{a}\mathbf{k} \cdot \mathbf{r}_i\right) \right|^2$$



spin correlations



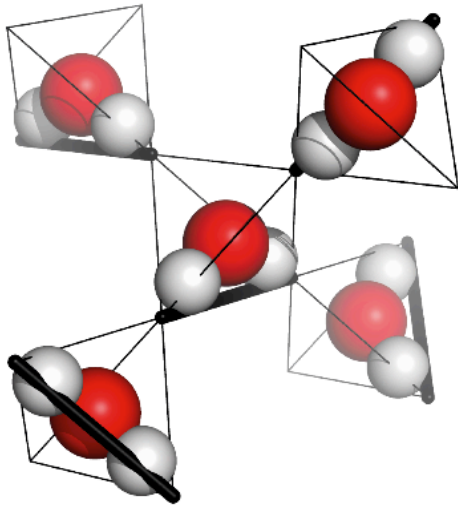
paramagnetic domains

Paddison *et al.*, *PRB* **97**, 014429 (2018)

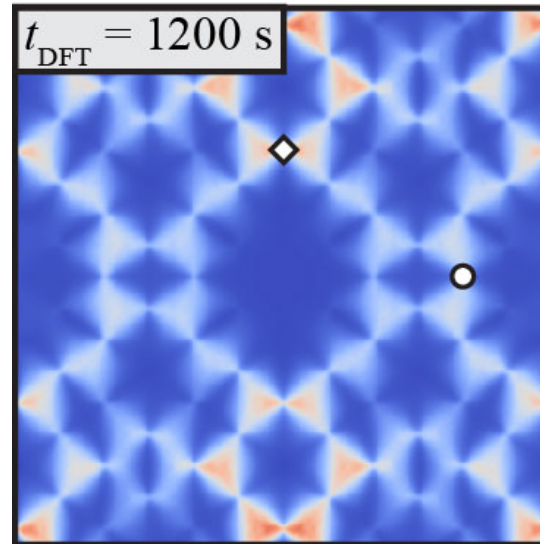
See also mPDF: Frandsen *et al.*, *Phys. Rev. Lett.* **116**, 197204 (2016)

Ultrafast calculation of 3D diffuse scattering

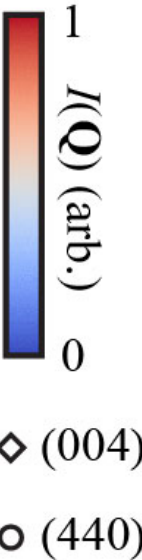
- ❑ 3D diffuse-scattering patterns traditionally **slow** to calculate
 - Many atoms/spins, many wavevectors
 - Real-space processing ("sub-boxes") employed to reduce noise
 - Fast Fourier transform considered unsuitable



water ice

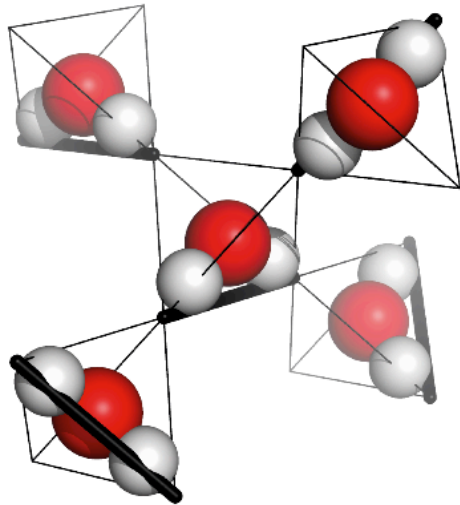


(110) plane*
DFT + sub-boxes

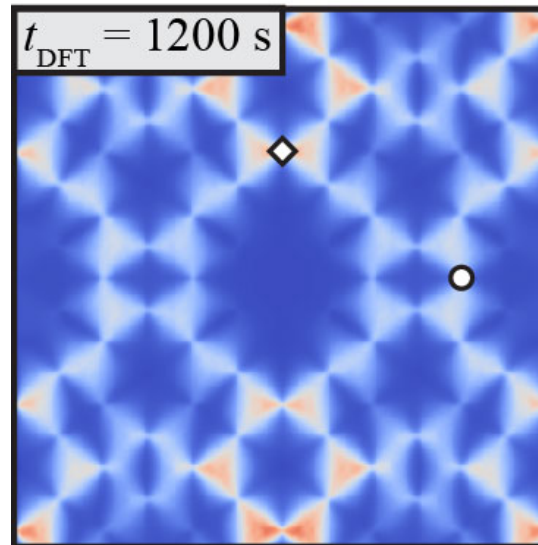


Ultrafast calculation of 3D diffuse scattering

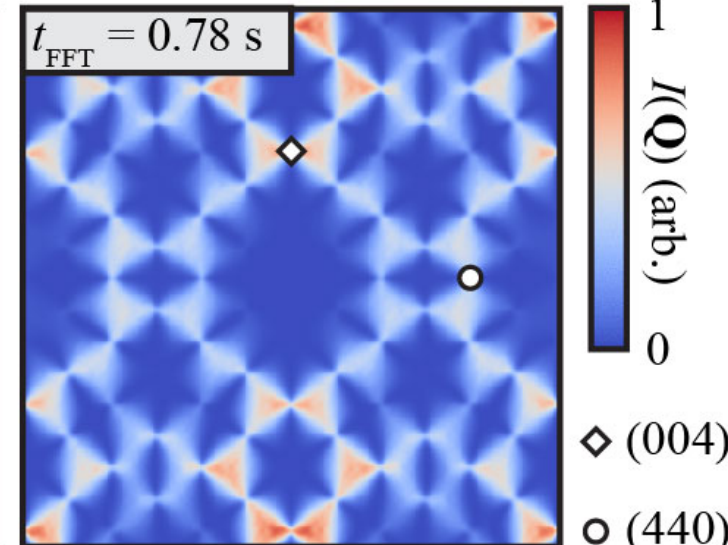
- Accelerate 3D diffuse-scattering calculations using two results
 - Average structure always periodic \rightarrow FFT **can** be used
 - Nyquist theorem \rightarrow complete scattering pattern can be reconstructed from supercell Bragg intensities



water ice



(110) plane
DFT + sub-boxes*



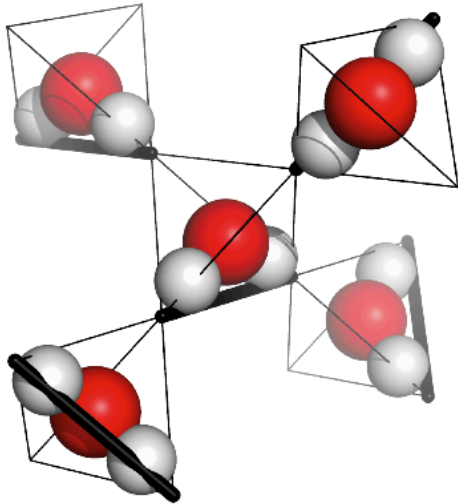
(110) plane
FFT + filtering*

Ultrafast calculation of 3D diffuse scattering

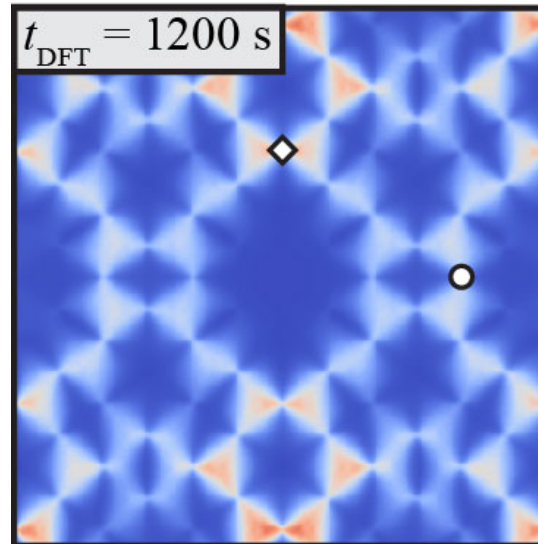
Ultrafast calculation of diffuse scattering from atomistic models

Joseph A. M. Paddison*

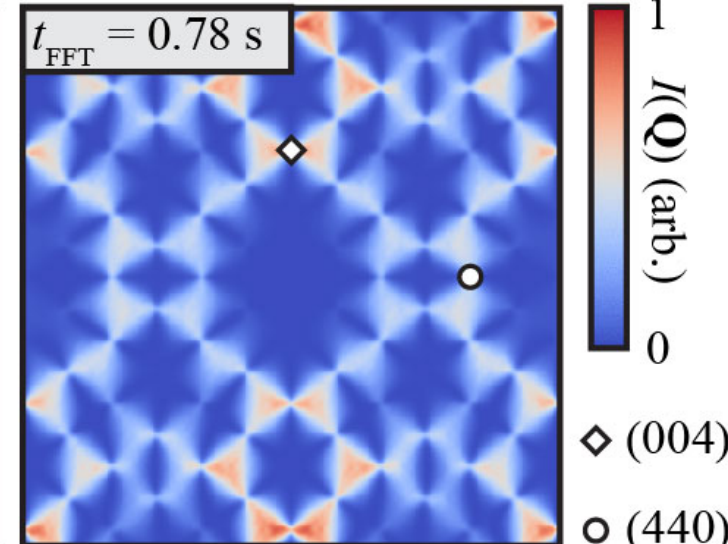
paddisongroup.wordpress.com/software



water ice



(110)* plane
DFT + sub-boxes



(110)* plane
FFT + filtering

Paddison, Acta Cryst A 75, 14-24 (2019)

Roth et al, IUCrJ 5, 410 (2018)

Thanks for listening!

Andrew Goodwin, University of Oxford, UK

Ross Stewart, STFC-ISIS, UK

Martin Mourigal, Georgia Tech, USA

Pascale Deen, University of Copenhagen, Denmark & ESS, Sweden

Henrik Jacobsen, University of Copenhagen, Denmark & ESS, Sweden

Maria Teresa Fernández-Díaz, ILL, France

Oleg Petrenko, University of Warwick, UK

Matthias Gutmann, STFC-ISIS, UK

Dave Keen, STFC-ISIS, UK

Matt Tucker, Oak Ridge National Lab, USA



**UNIVERSITY OF
CAMBRIDGE**

Useful info

paddisongroup.wordpress.com/software

email: jamp3@cam.ac.uk or paddison@gatech.edu

Software references:

Spinvert: Paddison, Stewart, and Goodwin, *JPCM* **25**, 454220 (2013)

Scatty: Paddison, *Acta Cryst A* **75**, 14-24 (2019)

Examples of use:

Paddison *et al.*, *Nature Commun.* **7**, 13842 (2016)

Paddison *et al.*, *Science* **350**, 179 (2015)

Nilsen *et al.*, *Phys. Rev. B* **91**, 054415 (2015)

Saines *et al.*, *Materials Horizons* **2**, 528 (2015)

Paddison *et al.*, *Phys. Rev. B* **90**, 014411 (2014)

Bonus – Absolute powder data normalization

Three steps

- 1) Rietveld (Fullprof) refinement to nuclear profile to determine refined scale factor, FullprofScale
- 2) $AbsScale = FullprofScale \times MagicNumber$
- 3) $NormalizedData = RawData / AbsScale$

The small print: Assumes absorption, preferred orientation, and other special intensity corrections **not** included in Fullprof model. Also, site occupancy $Occ = (\text{occupancy of special position}) / (\text{occupancy of general position})$.

Bonus – Fullprof “magic numbers”

(to normalize intensity in units barn sr⁻¹ spin⁻¹)

Constant-wavelength diffraction

$$\text{MagicNumber} = \frac{2\pi^2 NV}{45\lambda^3}$$

where N is number of spins per unit cell, V is unit-cell volume in Å³, and λ is neutron wavelength in Å.

Time-of-flight diffraction

$$\text{MagicNumber} = \frac{4\pi NV \sin \theta}{\text{DIFC}}$$

where θ is scattering angle of detector and **DIFC** (sometimes called **dt1**) is instrument parameter relating to TOF in μs to d -spacing in Å.