Recent and future developments in PDF-land

S.J.L. Billinge Columbia University, Brookhaven National Laboratory











Materials 2015







Modern materials and devices are complex!

- Photovoltaics with improved efficiency
 - Nanoparticles in the light collecting layer
- High energy density batteries
 - Electrodes
 - Electrolytes
- Fuel cells for transportation applications
 - Electrodes
 - Electrolytes
 - Catalysts
 - Hydrogen storage
- Sequestration
 - Functionalized mesoporous materials



Image credits: 10.1126/science.1185509 U. Uppsala

Real Materials

- Real-Material Structure model:
 - Crystal structure (if there is one)
 - Morphology (could be nano)
 - Surface reconstruction
 - Surface termination/dressing (ligands etc.)
 - Interfaces
 - Heterogeneities, phase separation
 - Point defects
 - Extended defects
 - Chemical short-range order
 - Distortive short-range order

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- ..

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Real material properties depend sensitively on crystalline imperfections

Examples

- Optical properties of quantum dots depend on presence or absence of surface trap states
- Photovoltaic performance depends on charge transfer and charge extraction
- Catalysis depends on surface structure
- Battery electrodes depend on access of lithium
- Broken symmetry states in the PG phase of HTSCs
- Place two insulators together and get superconductivity in the interface



21st Century Crystallography

The "Crystallography" of Real-Materials

Has to go well beyond perfect crystals Including:

- Defects
- Morphology
- Nanostructure
- Surfaces and interfaces
- Complexity!

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The Challenge with Real Material Structure Determination







The Challenge with Real Material Structure Determination



j

Local atomic structure from the Atomic Pair Distribution Function (PDF)



But there is no information at high-Q...?



The Challenge



Nanostructure refinement



PDF has been around for a long time



• Pieter Debye, 1915:

$$I = \sum_{n} \sum_{m} f_{m} f_{n}^{*} \frac{\sin q r_{mn}}{q r_{mn}}$$

• Fritz Zernike and Jon Prins, 1927:

$$4\pi r^2 \rho(r) = 4\pi r^2 \rho_a + \frac{2r}{\pi} \int_0^\infty q i(q) \sin q r dq$$











History

Debye and Menke, Z. Phys. (1930) PDFs of mercury

Tarasov, L. P., and Warren, B. E., (1936) J. Chem. Phys., 4, 236.X-ray PDFs of molten sodium



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BROOKHAVEN



Studying (nano)crystalline materials with PDF

- 1950's Rosalind Franklin
 - Carbon black, disordered carbon materials
 - (also Bert Warren!)
- I960's Roy Kaplow, Stephen Strong and Benjamin L. Averbach and computers
 - Simple metals, e.g., Lead. Interested in using them as models for liquid and glassy metals

PDP-9 factory test area, ~1967





PDF



+t/t

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A series of fortunate events

Web of science (x-ray + PDF) OR (x-ray + pair distribution function)



Studying (nano)crystalline materials with PDF

- 1950's Rosalind Franklin
 - Carbon black, disordered carbon materials
- 1960's Roy Kaplow, Stephen Strong and Benjamin L. Averbach and computers
 - Simple metals, e.g., Lead. Interested in using them as models for liquid and glassy metals
- 1980's Takeshi Egami and pulsed neutrons
 - Use of the newly available pulsed neutron source IPNS for quasicrystals then high temperature superconductors when they were discovered









A series of fortunate events

Web of science (x-ray + PDF) OR (x-ray + pair distribution function)



Synchrotron PDF

• Early x-ray PDF measurements at X7A, NSLS-II (20 keV, Ge point detector), led by Takeshi Egami



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A series of fortunate events

Web of science (x-ray + PDF) OR (x-ray + pair distribution function)



High energy synchrotron PDF

- Early x-ray PDF measurements at X7A, NSLS-II (20 keV, Ge point detector), led by Takeshi Egami
- First high resolution x-ray PDF measurement (Q_{max} = 45 A⁻¹!) using CHESS, Ge point detector, with Stefan Kycia





Workshop at the 2001 ACA annual meeting



Cartoon by Stacey Morrison, shared with me by Connie Rajnak (Chidester)





A series of fortunate events

Web of science (x-ray + PDF) OR (x-ray + pair distribution function)



Synchrotron PDF

- Early x-ray PDF measurements at X7A, NSLS-II (20 keV, Ge point detector), led by Takeshi Egami
- First high resolution x-ray PDF measurement (Q_{max} = 45 A⁻¹!) using CHESS, Ge point detector, with Stefan Kycia
- National Nanotechnology Initiative 2000



Nanoparticles could offer a new way to help eradicate polio worldwide

A new nanoparticle vaccine developed by MIT researchers could assist efforts to eradicate polio worldwide. Read more





PDF landscape in 2018

Web of science (x-ray + PDF) OR (x-ray + pair distribution function)



Synchrotron PDF

- Early x-ray PDF measurements at X7A, NSLS-II (20 keV, Ge point detector), led by Takeshi Egami
- First high resolution x-ray PDF measurement (Q_{max} = 45 A⁻¹!) using CHESS, Ge point detector, with Stefan Kycia
- National Nanotechnology Initiative
- Rapid Acquisition PDF (RAPDF) developed at 6ID-D at APS, with Pete Chupas, 2D 2003





PDF landscape in 2018

Web of science (x-ray + PDF) OR (x-ray + pair distribution function)



Synchrotron PDF

- Early x-ray PDF measurements at X7A, NSLS-II (20 keV, Ge point detector), led by Takeshi Egami
- First high resolution x-ray PDF measurement (Q_{max} = 45 A⁻¹!) using CHESS, Ge point detector, with Stefan Kyci
- National Nanotechnology Initiative
- Rapid Acquisition PDF (RAPDF) developed at 6ID-D at APS, 2003 with Pete Chupas, 2D





The perfect storm







IN THE



Sources/detectors + computing + nanoscience



You must remember this



Zr/Sn phenyl phosphate, unconventional MOFs



Clearfield, A. Dalton Trans. 2008, 44, 6089-6102.

Collaboration with the group of Abe Clearfield, Texas A&M

THE COL

• Work of Chenyang Shi, Max Terban and Rita Silbernagel

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HTTP://thebillingegro

Try ZrP structures on H-Zr sample, PDFgui





- Fits are good up to 7 Å: basic motifs, i.e. ZrO_6 and PO_4 are similar in all models.
- Fits of phenyl and alpha ones are similar
- Fits of phenyl and alpha are better.



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Studying the layer stacking

- ZrPP layers
- Smear out electron-density in, but not perpendicular to the layers (gold)
- Get beautiful "Warren lineshape" signal extending to high-r
- Comes from the layer stacking, regardless of any intra-order

Finding Tb intercalated into ZrPP


X-ray PDF of weakly scattering organics

BRUUKH



collaboration with Prof. Martin U. Schmidt and Dragica Prill, Inst. fur Anorg. Chemie, Goethe-Univ., Frankfurt am Main

quinacridone – $C_{20}H_{12}N_2O_2$

- industrially important pigments, red and violet paints
- can form many phases, some (alpha-II) do not crystallize and have unknown structure
- experimental PDFs measured at APS ANL beamline 11-ID-B
- standard refinement with PDFgui has poor quality even for the known beta phase



PDF modeling of β-quinacridone





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monoclinic P2₁/c with
 2 molecules per unit cell

- refinement in PDFgui gives poor $R_w = 0.41$
 - low-r peaks too wide
 - high-r peaks too sharp
- peak widths depend strongly on r
 - sharp peaks for strongly bonded intra-molecular atom pairs
 - broad peaks for inter-molecular correlations
- Debye-Waller model of independent atom displacements is grossly inaccurate
- PDF model has to account for different displacements for pairs in the same molecule and intermolecular pairs

PDF modeling of β-quinacridone





PDF calculation with separate intra- and inter-molecular contributions

- (a) PDF from a single-molecule, small atom displacements U_{intra}
- (b) PDF from a crystal with large displacements U_{inter}
- (c) PDF from a molecule with large displacements U_{inter}
- (b) (c) PDF from inter-molecular interactions only
- (a) + (b) (c) total PDF reflecting both displacements U_{intra} , U_{inter}



PDF modeling of β-quinacridone







• remnant fit difference due to anisotropic molecule displacements, displacement anisotropy can be studied with improved models

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 $U_{inter} = 0.0014(2)$ Å² $U_{intra} = 0.023(2)$ Å²

D. Prill *et al.*, J. Appl. Crystallogr. 48, 171-178 (2015)

 $R_w = 0.41 \rightarrow R_w = 0.28$

D. F

significant fit improvement

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Studying conformational degrees of Freedom



Dilute signals from drugs in suspension



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- Blue: 5wt%
- Green 0.66 wt%
- Red 0.25 wt%

Can see nanocrystalline API even at the 0.25wt% level!



Recrystallization of lactose

 Various A-form samples aged at, 40°C/75% RH



Understanding crystallization

• How does the crystallinity grow in?







Drug candidate: conformation changes in the amorphous state

Modeling of structure in the amorphous state

Findings:

- Conformational disorder: Need to assign a separate thermal factor between different intraregions of the molecule.
- Subtle differences between
 different micronization methods



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Hydrogen bonding interactions vary depending on how the material was amorphized



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Distinct differences found between the PDFs of differently produced amorphous forms

- prepared via mechanical versus solution based methods
- A sharp feature in the residual corresponds to the minimum and maximum hydrogen bonding distances, indicating a slight change in the intermolecular packing.







PDFgui

- Used to be called "real-space Rietveld"
 - Starting point is a crystallographic description of the model
 - Small Unit cell, periodic boundary conditions
 - Fits to G(r) which is the FT of F(Q)
- PDFgui
 - Available from diffpy.org
 - Development funded by NSF-DANSE program





PbSe-480K.ddp (~\Documents\gl\16papers\16eb_pbse-emphanisis\new\20170412\Structure modeling\Recent data\PbSe-480K.ddp) - PDFgui													
File Edit View Fits Phases Data Calculations Help													
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□ ₩ PbSe ₩ PbSe.cif ₩ PbSe.gr	P	ha	se	Co	ont	figur	ation		_				
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	alp	oha 90	.0			beta 90	.0	gamma	90.0				
	So	ale Fact	tor 1	.0									
		delt	a1 0	.0		de	lta2 1.0		spdia	meter	0.0		
		sra	tio 1	.0			rcut 0.0		st	epcut	0.0		
	In	cluded F	Pairs	s all-all									
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	1	Pb	0.5	0.5	0.5	0.0186431	0.0186431	0.0186431	0.0	0.0	0.0	1.0	
Plot Control X	2	Pb	0.5	0.0	0.0	0.0186431	0.0186431	0.0186431	0.0	0.0	0.0	1.0	
	4	Pb	0.0	0.0	0.5	0.0186431	0.0186431	0.0186431	0.0	0.0	0.0	1.0	
step	5	Se	0.0	0.0	0.0	0.0143116	0.0143116	0.0143116	0.0	0.0	0.0	1.0	
Y	6	Se	0.0	0.5	0.5	0.0143116	0.0143116	0.0143116	0.0	0.0	0.0	1.0	
lat(1)	7	Se	0.5	0.0	0.5	0.0143116	0.0143116	0.0143116	0.0	0.0	0.0	1.0	
lat(2)	8	se	0.5	0.5	0.0	0.0143116	0.0143116	0.0143116	0.0	0.0	0.0	1.0	
lat(3)													
pscale													
u11(1)													
u11(2) -													
offset -5													
Plot Reset													
PDFfit2 Output													

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PDFfit2 Output

+

CMI: complex modeling infrastructure

CMI

- Also available at diffpy.org
- Very powerful
- Very difficult to use
- We are working on a more friendly user interface and better documentation, but for now it is advised to contact us and we can help you get started





Diffpy-Complex Modeling Infrastructure: Diffpy-CMI

S DiffPy Community Publications Products -

DiffPy-CMI

DiffPy-CMI is our complex modeling framework. It is a highly flexible library of Python modules for robust modeling of nanostructures in crystals, materials.

The software provides functionality for storage and manipulation of structure data and calculation of structure-based quantities, such as PDF, SA overlaps, bond lengths, and coordinations. Most importantly the DiffPy-CMI package contains a fitting framework for combining multiple experime problem.

This is an early release of code that is under intense development, with support for installation on Unix, Linux, and Macintosh machines. The sco will evolve rapidly, but we want to make the code available at the earliest possible date. Please make use of the software and provide feedback a but please be patient and check back frequently for updates.



TITIT

```
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File Edit Selection Find View Goto Tools Project Preferences Help
◀ ►
        untitled
       import numpy as np
import pylab
        from scipy.optimize.minpack import leastsq
       from diffpy.Structure import loadStructure
       from diffpy.srfit.pdf import PDFContribution
       from diffpy.srfit.fitbase import FitRecipe, FitResults
        dataFile = "ni-q27r100-neutron.gr"
        structureFile = "ni.cif"
        spaceGroup = "Fm-3m"
       niPDF = PDFContribution("nickel")
       niPDF.loadData(dataFile)
       niPDF.setCalculationRange(xmin=1, xmax=20, dx=0.01)
       niStructure = loadStructure(structureFile)
       niPDF.addStructure("nickel", niStructure)
       niFit = FitRecipe()
       niFit.addContribution(niPDF)
Line 107 Column 1
       IN THE CITY OF NEW YORK
```

```
untitled • - Sublime Text
File Edit Selection Find View Goto Tools Project Preferences Help
◀ ►
        untitled
                          ۰
       niFit.clearFitHooks()
       print "Refine PDF using scipy's least-squares optimizer:"
       print " variables:", niFit.names
       print " initial values:", niFit.values
       leastsq(niFit.residual, niFit.values)
       print " final values:", niFit.values
       print
       niResults = FitResults(niFit)
       print "FIT RESULTS\n"
       print niResults
       r = niFit.nickel.profile.x
       gobs = niFit.nickel.profile.y
       gcalc = niFit.nickel.evaluate()
       baseline = 1.1 * gobs.min()
       gdiff = gobs - gcalc
       pylab.figure()
       pylab.plot(r, gobs, 'bo', label="G(r) data",
               markerfacecolor='none', markeredgecolor='b')
       pylab.plot(r, gcalc, 'r-', label="G(r) fit")
       pylab.plot(r, gdiff + baseline, 'g-', label="G(r) diff")
       pylab.plot(r, np.zeros like(r) + baseline, 'k:')
       pylab.xlabel(r"r ($\AA$)")
       pylab.ylabel(r"G ($\AA^{-2}$)")
       pylab.legend()
       pylab.show()
Line 107 Column 1
```

Diffpy project (BNL LDRD) Complex Modeling infrastructure: Diffpy-CMI

Official release of Diffpy-CMI v2.0 (also Python 3 version available)

🗱 DiffPy	Community Publications Products -	Search
DiffPy-CMI is now	vailable! Get DiffPy-CMI Credits	www.diffpy.org
DiffPy -	Atomic Structure Analysis in Python	

A free and open source software project to provide python software for diffraction analysis and the study of the atomic structure of materials.

=> Spatially Resolved PDFs

 Anton Kovyakh, Soham Banerjee, Chia Hao Liu

=> Combine PDF and tomography (ctPDF)

ctPDF developed with Simon Jacques, Marco DiMichiel, Andy Beal and Bob Cernik

10,000 2D datasets per image, 30 mins per image ~10Tb/day Simon D. M. Jacques, Marco Di Michiel, Simon A. J. Kimber, Xiaohao Yang, Robert J. Cernik, Andrew M. Beale and Simon J. L. Billinge, *Nat. Commun.* 4, 2536 (2013).//thebillingegroup.com Jensen, Corr, Di Michiel, SJLB et al., *J. Electrochem. Soc.* (2015)

mPDF: PDF of short-range magnetic correlations

 Benjamin A. Frandsen, Xiaohao Yang and Simon J.L. Billinge, Acta Crystallogr. A 70, 3-11 (2014).

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MnO

Top: *Blue*: measured nPDF signal *Red* (top) calculated structural PDF Btm: *Blue*: difference between nPDFsignal and calculated structural PDF *Red*: calculated mPDF for AF MnO

Benjamin A. Frandsen, M. Brunelli, K. Page, Y. J. Uemura, Julie B. Staunton, SJLB, arXiv:1512.06270.

Frandsen, SJLB, Acta Crystallogr. A 71, 20325-334 (2015)

Intuitive way to resolve interesting questions

• Henry Fischer poster!

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Software Projects

Software Projects that go wrong

- Who: US department of homeland security
- What: Develop a GUI for the US president to undertake his most important functions
- Functional Requirements: Must be very simple and easy to use

PDFgui2.0

• PDFFIT2 + gui = PDFgui

C. L. Farrow, P. Juhás, J. W. Liu, D. Bryndin, E. S. Božin, J. Bloch, Th. Proffen and S. J. L. Billinge, PDFfit2 and PDFgui: computer programs for studying nanostructures in crystals, *J. Phys.: Condens. Matter* **19**, 335219 (2007)

• Diffpy-CMI + gui = PDFgui2.0

PDFgui2.0 is indistinguishable from PDFgui

But PDFgui2.1....

• Cluster modeling in a gui.....

IN TH

	1		PDFgui2.0					
			PDEqui2 0					
it Tree	8		FDFguiz.0	Configure	Constraints	Results		
🔻 📓 Fit 1				Configure	Constraints	Results		
🛱 cluster.xyz	Phase Cor	nfiguratio	n					
🛄 cluster.gr		-						
	a 1.0	b	1.0	(c 1.0			
	alpha 90.0	beta	90.0	gamma	a 90.0			
				Ŭ				
	Scale Factor	1.0						
0	delta1	0.0	delta2 0.	0	spdiameter 0	.0		
ot Control	Sector	1.0	reut 0	0	stencut 0	0		
	STATIO	1.0	Tout 0.	,	stepcut 0.	.0		
step	✓							
	Included Pairs	all						
	elem	c						
pscale	1 Mn -15.0	171						
u11(2)	2 0 -12.8	47	5 -				O G(r) data	
u11(3)	3 O -15.2	829		8			G(r) fit	
u11(4)	4 0 -14.8	018	1				G(r) diff	
u11(5)	5 N -14.9	995	4	86				
u11(6)	6 N -14.2	43		6				
11(7)	7 N -17.1	806	3 -	A 66	8			
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PDFgui2.X

- PDFgui2.2: Log normal particle distributions
- PDFgui2.3: mPDF integration
- PDFgui2.4: organics
- PDFgui2.5: Your dream here!

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Status: Work of Long Yang, collaboration with Matt Tucker @ORNL. We have working prototypes of PDFgui2.0 and PDFgui2.1

It is an open-source community coding project. If you are interested in contributing, please let us know!

High throughput + penetrating x-rays + dilute systems => in-situ synthesis

- We can see precursor species in solution
- We can measure Nanoparticle structural parameters
- High energy x-rays can penetrate relatively thick walled vessels
- => Let's do in-situ studies of synthesis
- Rich collaboration with the group of Bo Iversen (Aarhus)

Image credit Christoffer Tyrsted

lingegroup.com

Data analysis/modeling as pipes

Data as streams through those pipes

Experiments as sets of asynchronous streams

Example 3: Asynchronously Monitor During a Scan

xpdAn/xpdtools

Monitor data as it comes

- Define Quantities of Interest (QOI's)
- Monitor the QOI's
- E.g., projection coefficients onto principle components

• Chapman et al., JAC 2015, PCA on gold nanoparticle formation

Other physical measures

- It is straightforward to incorporate other statistical measures into the pipelines.
- E.g., if you want a more physical matrix decomposition, use Nonnegative matrix factorization (NMF)
- Slower and less convergent, but more physical



xpdtools







PDFmorph

- Has my sample undergone a phase transition?
- Plot high and low-T data on top of each other, are they different?



• Yes, um no, um, not sure





PDFmorph



5

10

15

r(Å)

20

25

30

- Apply reasonable transformations to the data in a regression loop:
 - Stretch
 - Smear
 - Scale
 - Low-cost model
 independent way to
 account for "uninteresting"
 effects such as thermal
 expansion and thermal
 broadening

PDFmorph



- If there is a phase transformation, stretching, smearing and scaling won't cut it!
- Been using PDFmorph in the group for some time but we are getting close to a public release

Put PDFmorph into the pipeline

- I. Define something as a scalar "feature"
 - I. E.g., the Rw or the Pearson correlation coefficient of the current PDF morphed onto either the previous or the first PDF in the stream
- 2. Incorporate this as a node in the data analysis pipeline graph
- 3. Visualize the QOI vs. index

Pipelines can be run at data collection time (xpdAn@NSLSII) but using xpdtools, it can be run on data that you take home from any experiment.







Automating modeling

• Can we think about how to make modeling more automated, and possibly introducing it into the pipeline?





Standard approach

11111(C)

- I PDF
- I model
- 20 parameters
- Vary the parameters until the model agrees as well as possible with the data.
- Emphasis on parameter estimation, not on model selection
- Challenge is finding the right model COLUMBIA UNIVERSITY



New approach: Structure-Mining

- I PDF
- many models
- few parameters
- Iterate over large numbers of models
- Emphasis on model selection
- Advantage: find multiple nearby models!
- Challenge: structure must be in the structure-mine









Structure-Mining I: Metallic nanoparticles

BROOK



~3 nm Pd nanoparticles































































- Modern materials are complex
 - => Real Materials "crystallography"
- But modern synchrotrons/neutron sources are bright
- And modern computers are fast

Use PDF/total scattering

Avoid Fake News





Acknowledgements



- A special thank you to all my current and former students and post-docs
- Also my many wonderful collaborators, mentioned during the talk
- Facilities:
 - APS, CHESS, NSLS, NSLS-II (and people therein)
 - MLNSC, ISIS, SNS (and people therein)
- Funding: DOE-BES and NSF-DMR



Questions?

NEWS IN BRIEF

Seagull With Diarrhea Barely Makes It To Crowded Beach In Time

2/19/13 9:45am • SEE MORE: NATURE ~





NAPLES, FL—Describing it as a "real close call," a local seagull suffering from an acute case of diarrhea told reporters that he was barely able to make it to a crowded public beach in time to relieve himself Monday. "Oh,