

Neutron and X-ray Diffraction for Energy Materials

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Outline

- Introduction (scope)
- Information from powder diffraction
- Phase identification
- Le Bail and Rietveld method
 - Structure factor
 - Phase quantification
 - Microstructure analysis (size and strain)
- Neutrons vs X-rays
- Examples
 - *Operando* NPD
 - Bond-valence energy landscapes
 - Synchrotron XRD depth profiling (ED)
 - XRD-CT

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Introduction (scope)

The lecture is designed a practical oriented guide for energy material researcher

The fundamentals are not covered:

- Generation of the flux
- Monochromatization
- Derivation of Bragg's law
- Crystallography

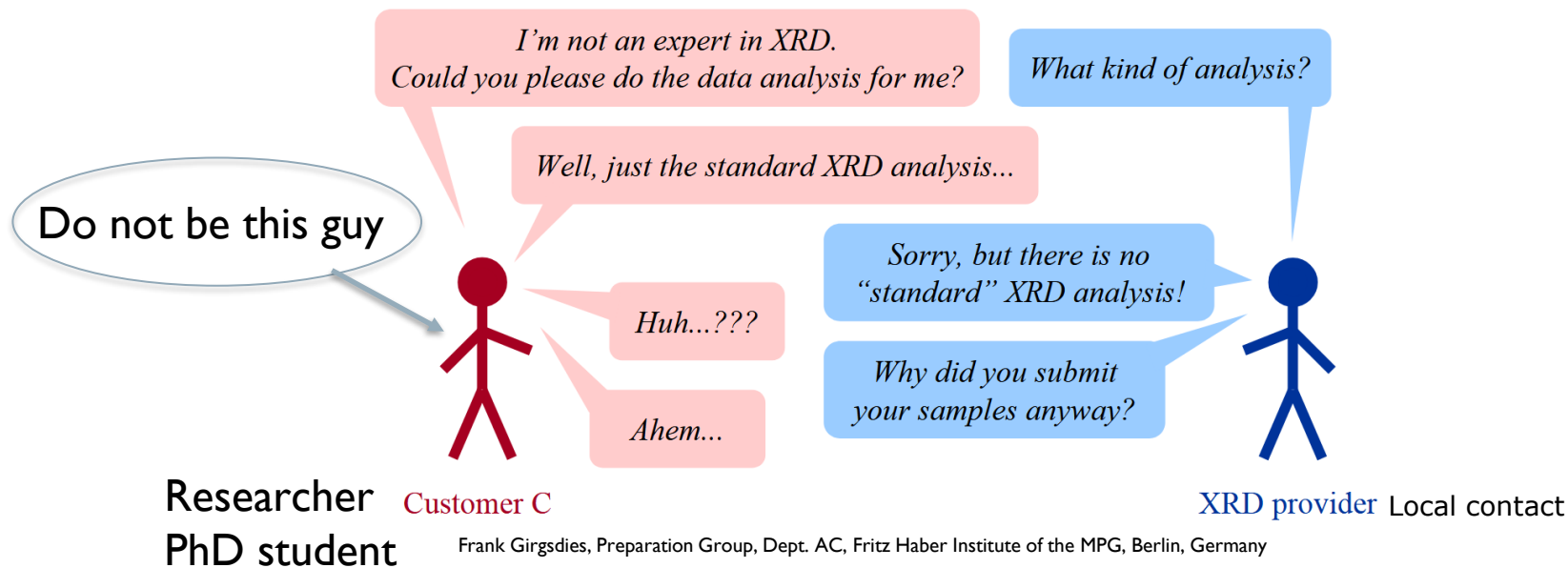
Also things not covered in this lecture:

- Single-crystal diffraction
- PDF (Pair Distribution Function)
- Magnetic structures

Introduction (scope)

Scenario 4

Yet another day, customer C comes again to the XRD service provider:
NPD



Outline

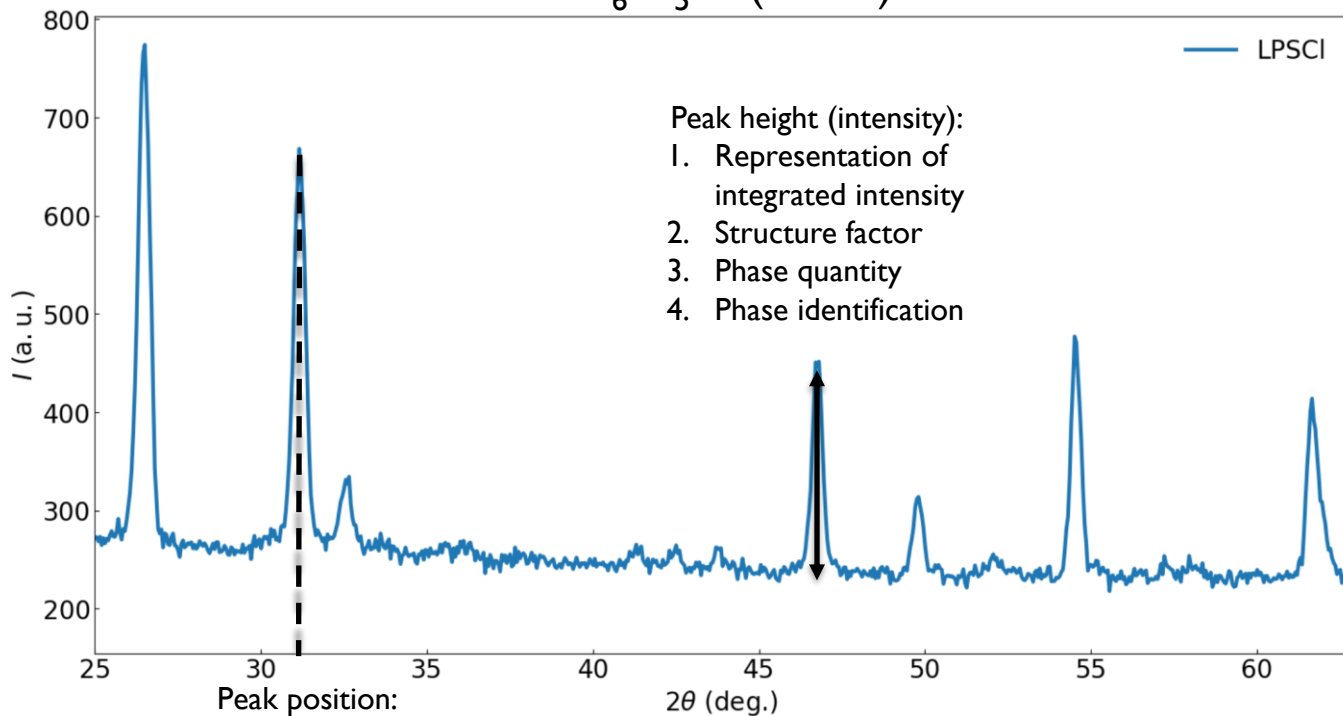
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Unit cell



Neutron Scattering - a Primer, Los Alamos Sci., vol. 19, p. 33, 1990.

Useful information from powder diffraction

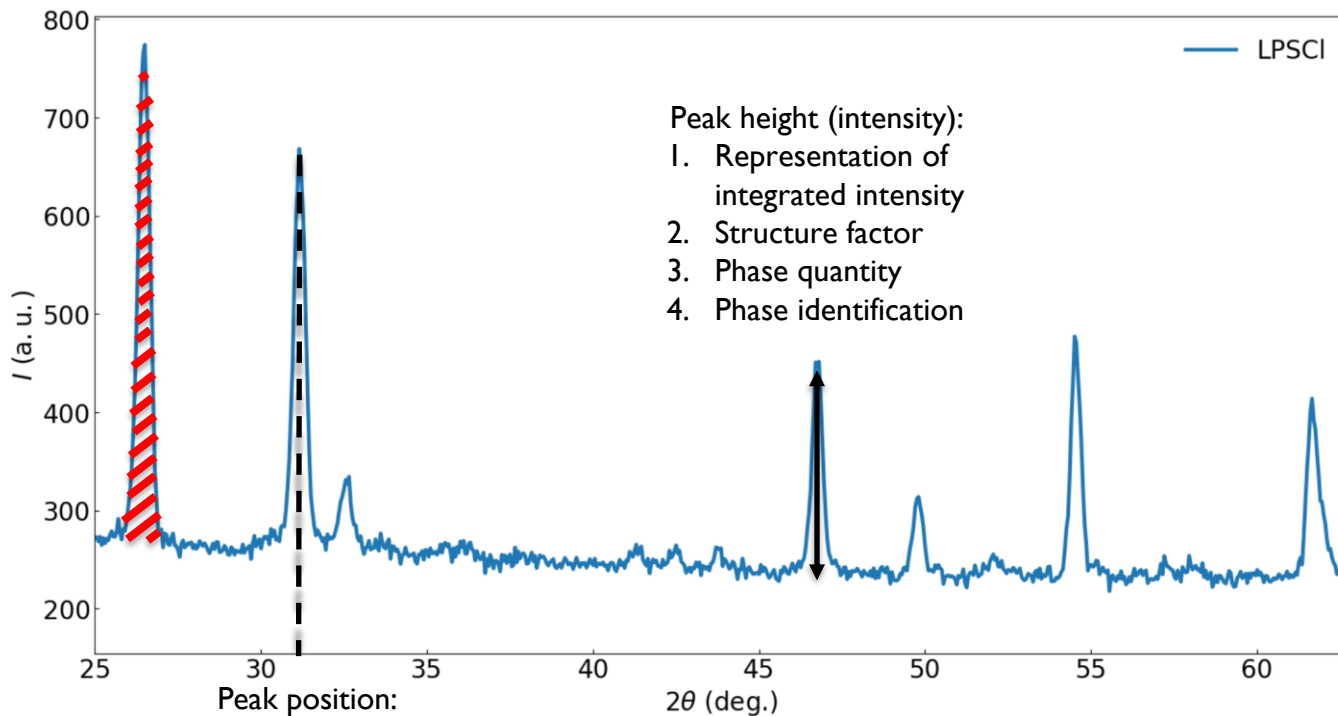


1. D-spacing
 1. Lattice parameters
2. Phase identification

Useful information from powder diffraction

Peak area:

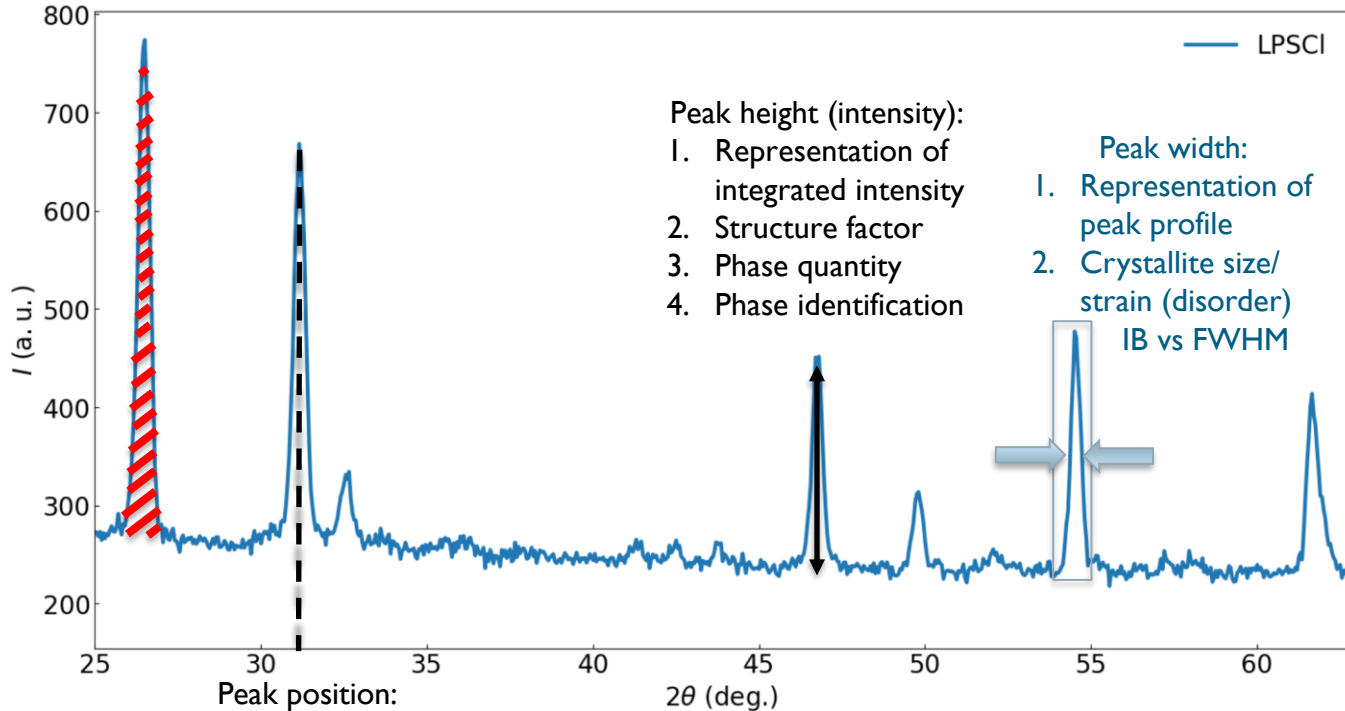
1. Structure factor
 1. Atomic occ.
 2. Atomic pos.
2. Phase quantity
3. Thermal parameters



Useful information from powder diffraction

Peak area:

1. Structure factor
 1. Atomic occ.
 2. Atomic pos.
2. Phase quantity
3. Thermal parameters



- Peak position:
1. D-spacing
 1. Lattice parameters
 2. Phase identification

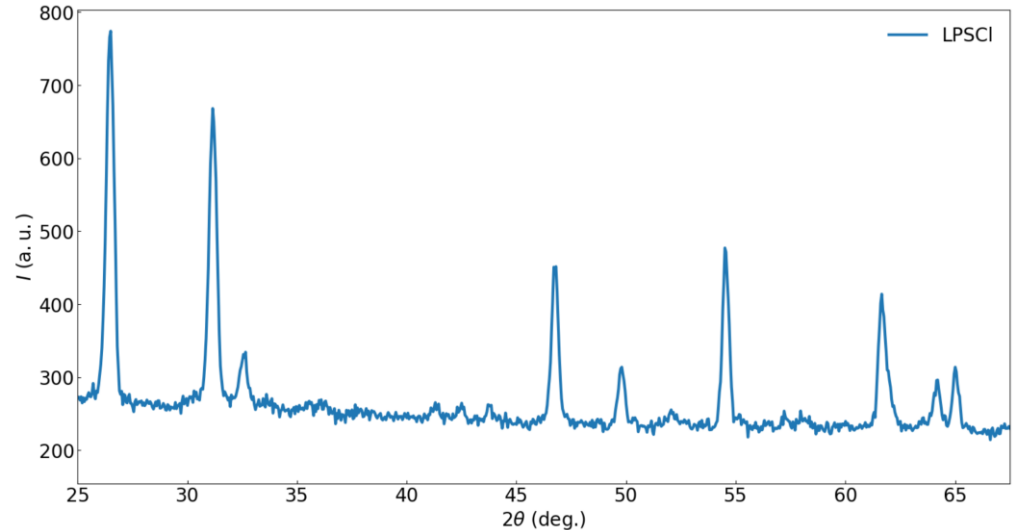
Phase identification

Important parameters:

- Peak positions
 - Correct single wavelength
- Peak intensity (or integrated intensity)

Databases:

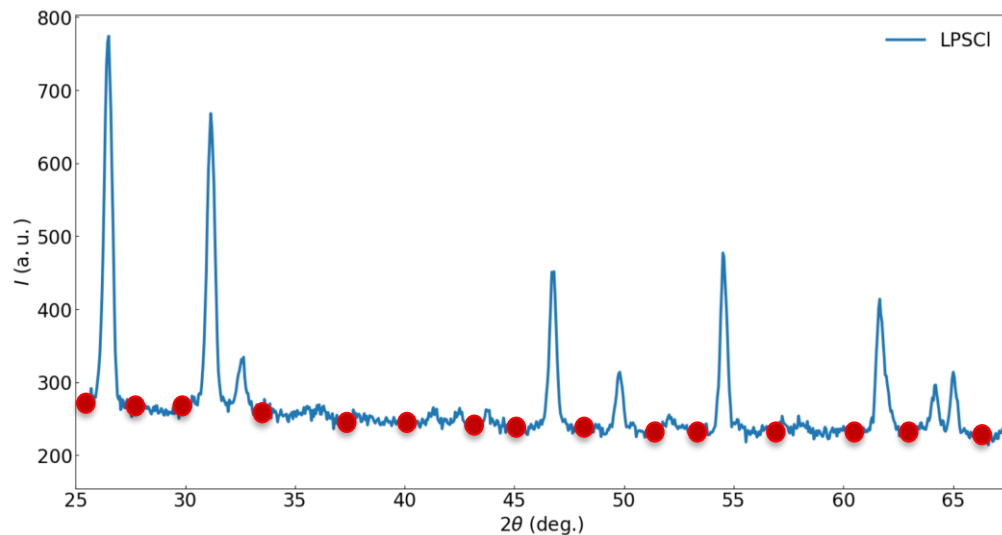
- COD (Crystallographic Open Database)
- PDF (Powder diffraction file)
- ICSD (Inorganic Crystal Structure Database)



Phase identification

Important parameters:

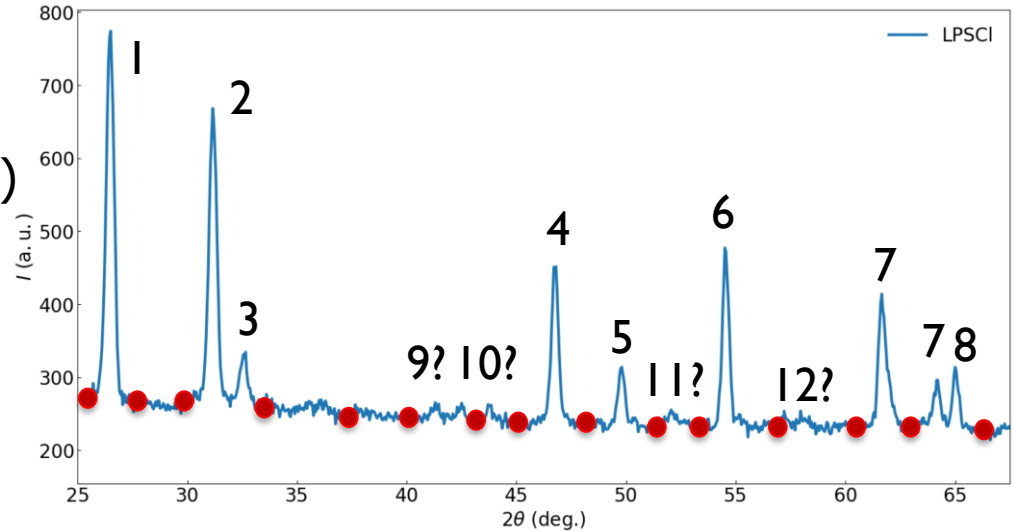
- Background



Phase identification

Important parameters:

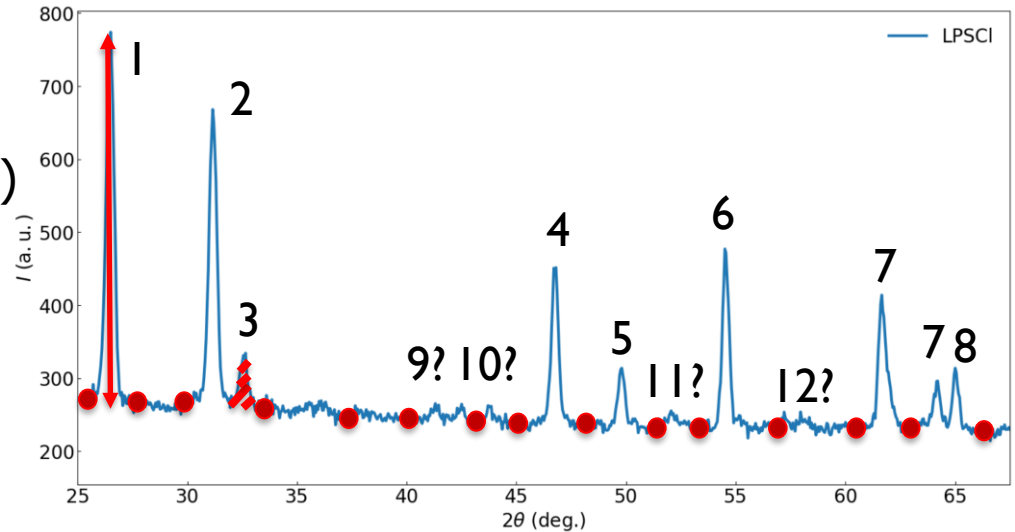
- Background
- Label peaks (if monochr, beam)



Phase identification

Important parameters:

- Background
- Label peaks (if monochr, beam)
- Get intensities for all peaks (or areas) by fitting
- Match the profile with the database using some software

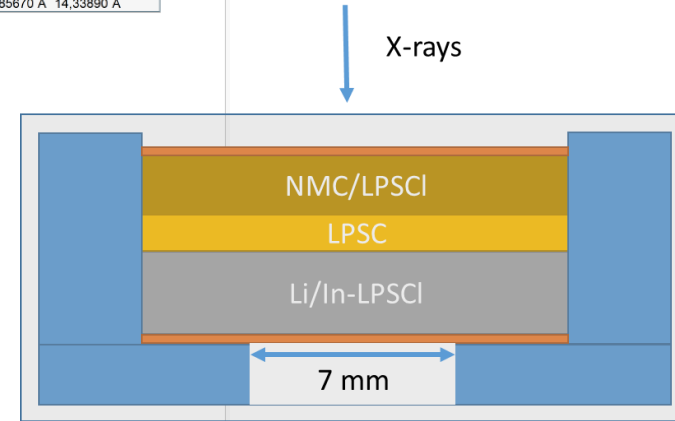
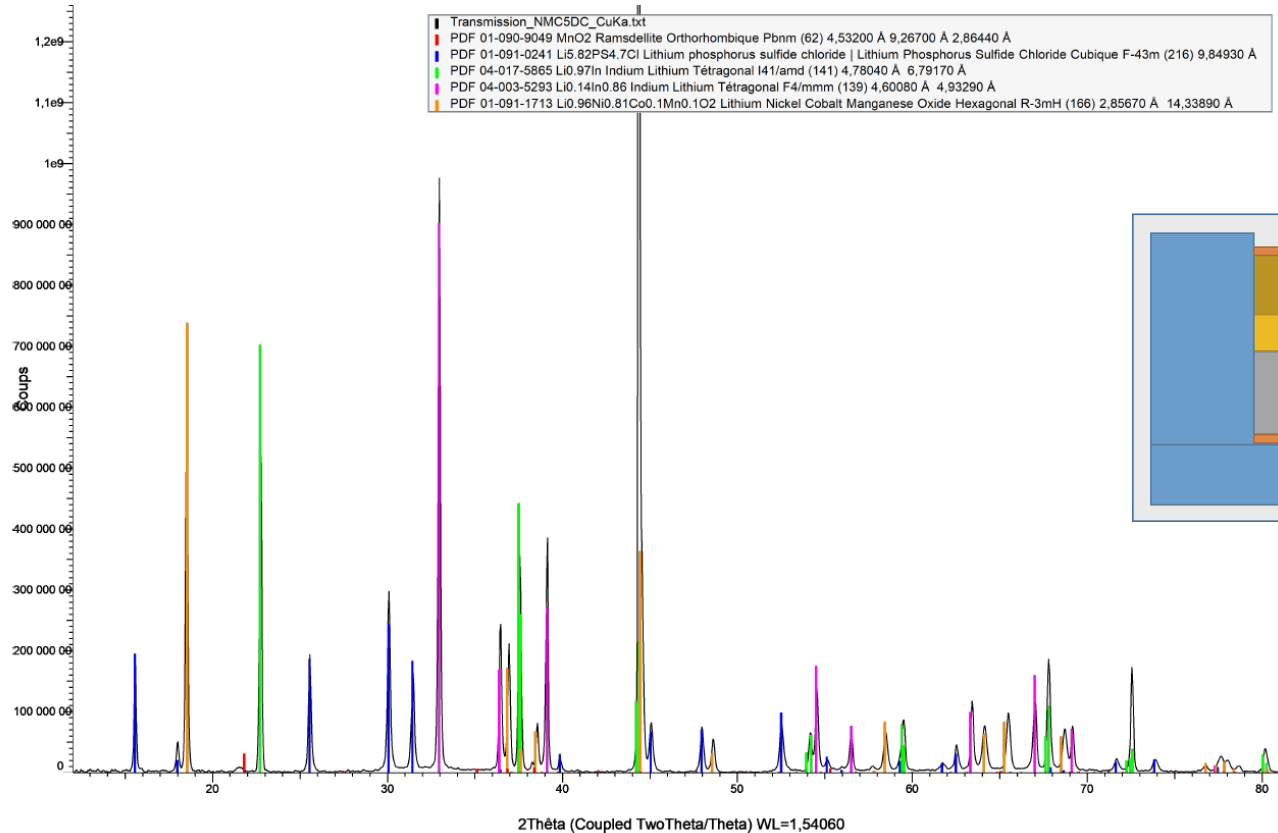


Different software:

- Match!
- Diffrac EVA

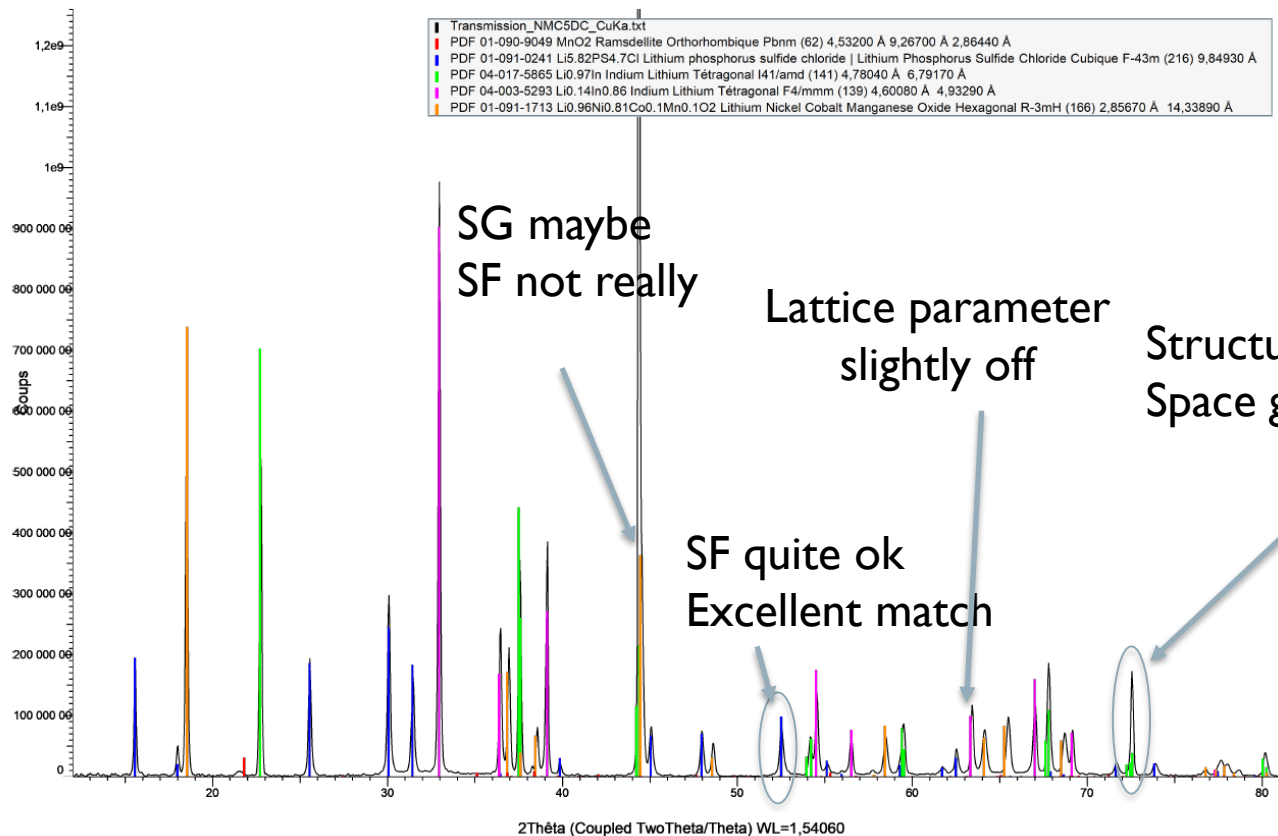
Phase identification

(Coupled TwoTheta/Theta)



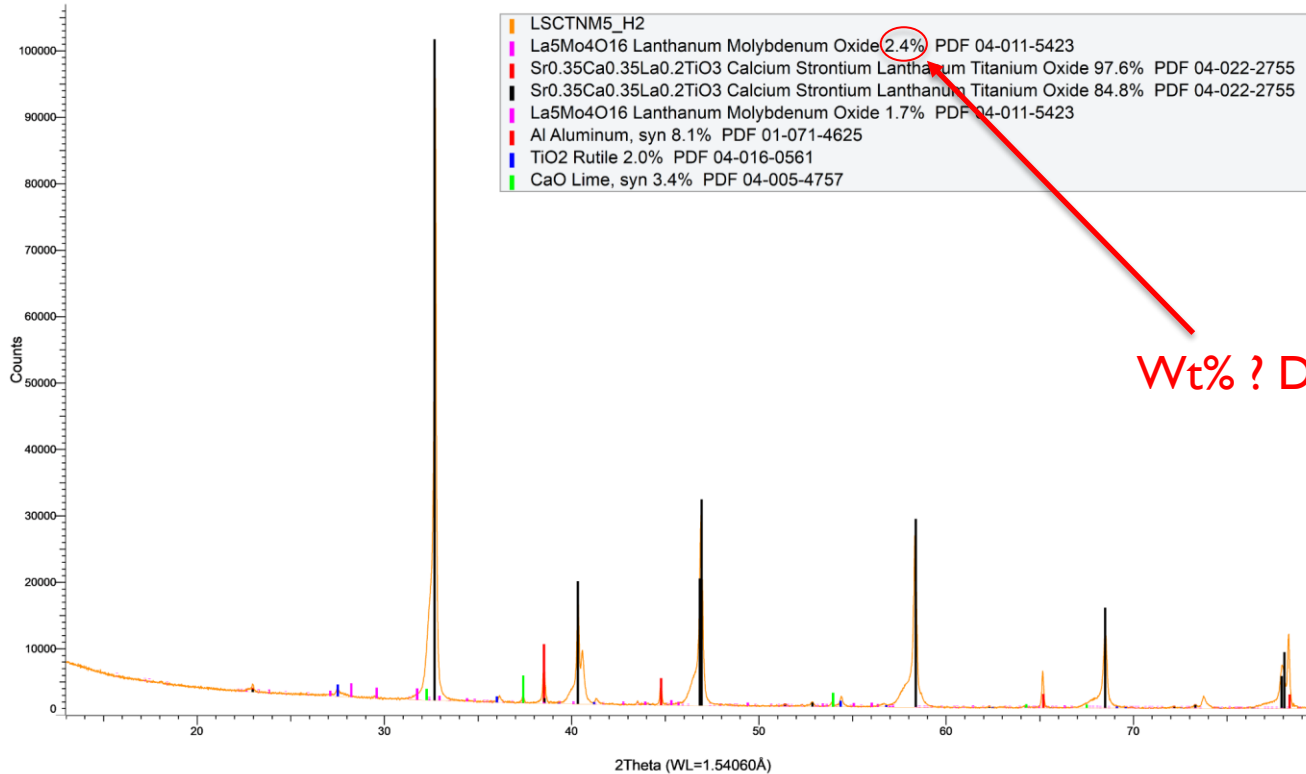
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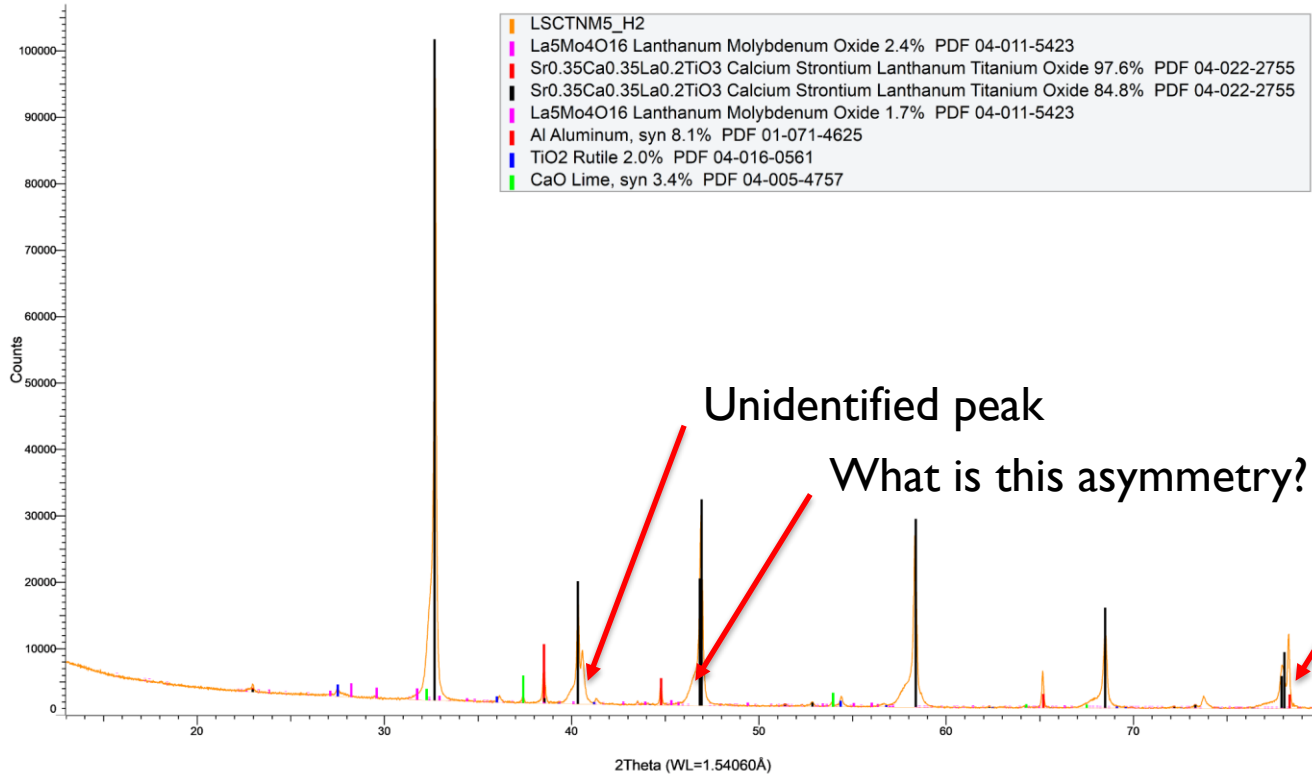
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Phase identification

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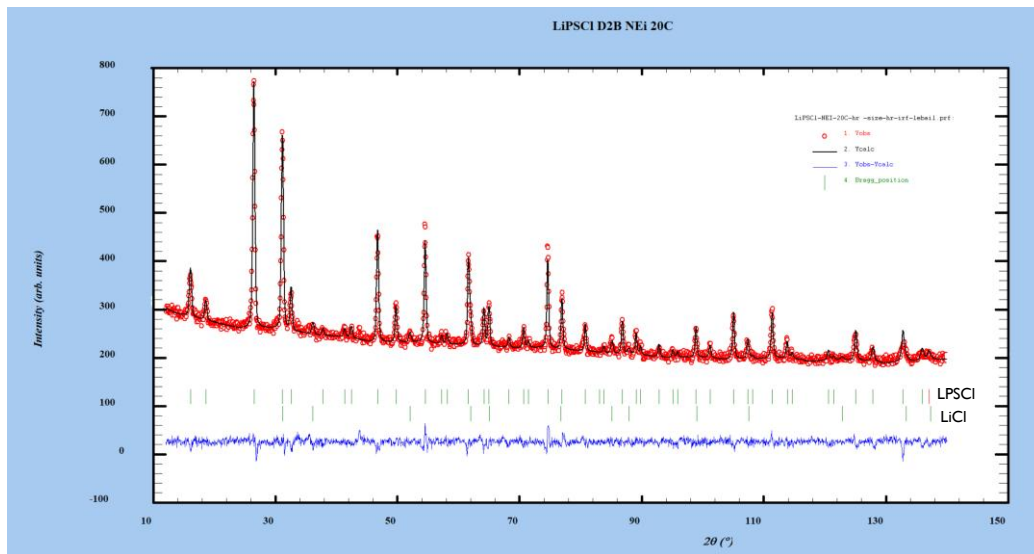


Le Bail refinement

Developed by Armel Le Bail around 1988

Starting parameters:

- unit cell parameters (r)
- space group
- Background
- peak profile parameters (r)
 - Instrumental (r)
 - Peak shape (r)
- This method **does not** extract information from **intensity**:
 - Structure (occupancies, atomic positions)
 - wt%
 - Thermal parameters



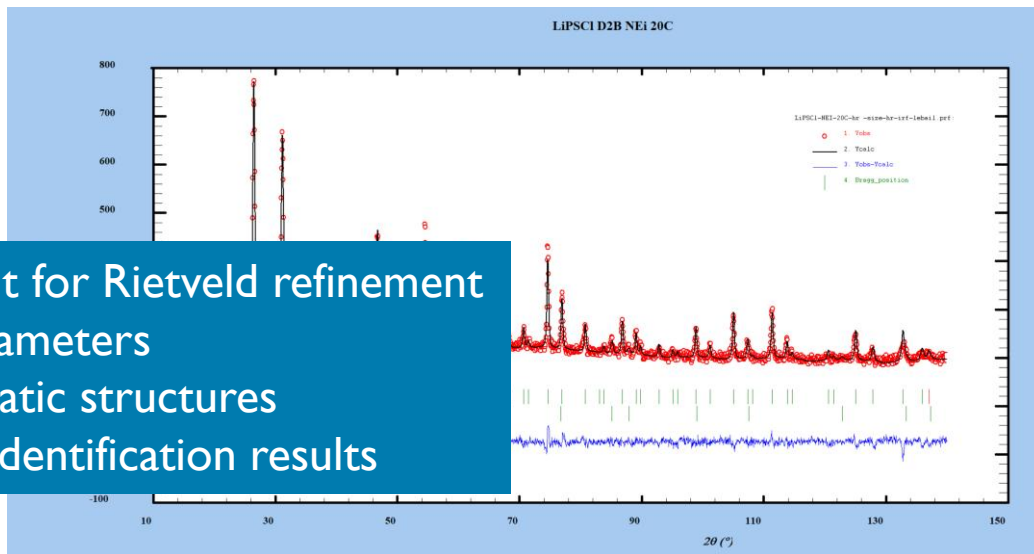
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Good starting point for Rietveld refinement
Refining lattice parameters
Unknown/problematic structures
Confirming phase identification results

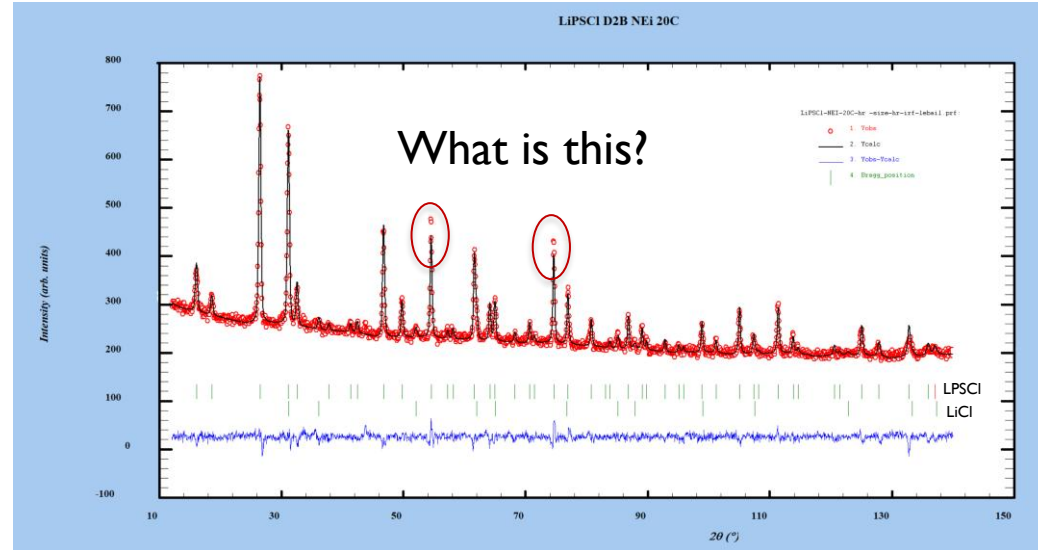


Le Bail refinement

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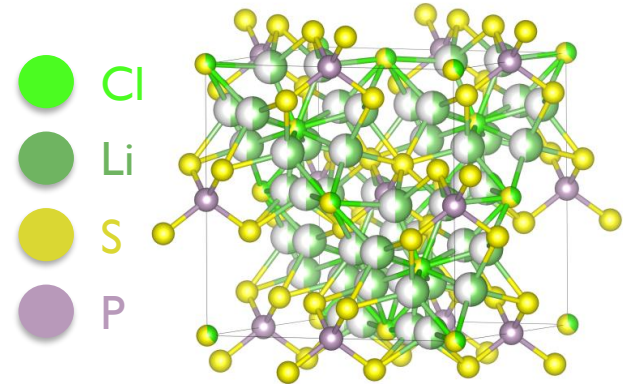
Rietveld refinement

Developed by Hugo Rietveld around 1967

- Background
- Space group
- lattice parameters
- peak profile:
 - microstructure (strain, crystallite size)
 - Instrumental
- magnetic structure (for neutron diffraction)
- weight percentages of phases
- Structure factor (database):
 - atomic coordinates
 - occupancies
 - thermal parameter(s) (atomic displacement)

Like Le Bail

Integrated intensity



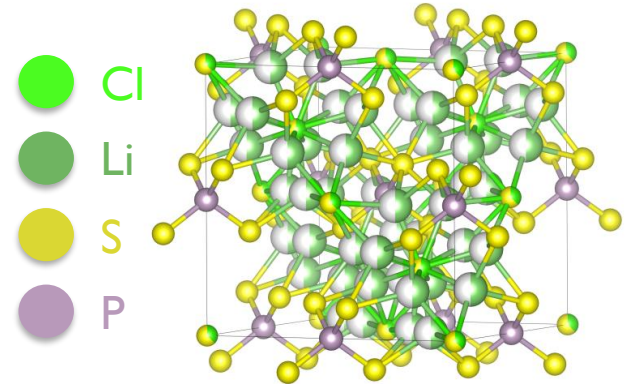
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 - microstructure (strain, crystallite size)
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- magnetic structure (for neutron diffraction)
- weight percentages of phases
- Structure factor (database):
 - atomic coordinates
 - occupancies
 - thermal parameter(s) (atomic displacement)

Like Le Bail

F -4 3 M		←--Space group symbol									
!Atom	Typ	X	Y	Z	Biso	Occ	In	Fin	N_t	Spc	/Codes
P1	P	0.00000	0.00000	0.50000	2.80412	0.04166	0	0	0	0	
		0.00	0.00	0.00	111.00	0.00					
Li1	Li	0.31732	0.02912	0.68267	2.41177	0.25000	0	0	0	0	
		81.00	91.00	-81.00	101.00	0.00					
S1	S	0.25000	0.25000	0.75000	1.51958	0.02021	0	0	0	0	
		0.00	0.00	0.00	121.00	131.00					
Cl1	Cl	0.25000	0.25000	0.75000	1.51958	0.02145	0	0	0	0	
		0.00	0.00	0.00	121.00	-131.00					
S2	S	0.12000	-0.12000	0.62000	2.29082	0.16667	0	0	0	0	
		0.00	0.00	0.00	31.00	0.00					
S3	S	0.00000	0.00000	1.00000	1.00000	0.02145	0	0	0	0	
		0.00	0.00	0.00	0.00	-131.00					
Cl3	Cl	0.00000	0.00000	1.00000	1.00000	0.02021	0	0	0	0	
		0.00	0.00	0.00	0.00	131.00					



Integrated intensity

Calculated intensity of one phase

$$y_i^{calc.}(2\theta_i) = s \sum_k L_k |F_k|^2 P_k A_k \phi(2\theta_i - 2\theta_k) + y_i^{background}$$

Sum over all
Bragg peaks

Calculated intensity of one phase

- Scale factor:
- Amount of phase
 - Flux/sensitivity

Structure factor:

- Atomic positions
- Atomic occ.
- Thermal param.
- Atomic scattering factors

$$y_i^{calc.}(2\theta_i) = s \sum_k L_k |F_k|^2 P_k A_k \phi(2\theta_i - 2\theta_k) + y_i^{background}$$

Peak profile function:

- Instrumental
- microstructure

Calculated intensity of one phase

- Scale factor:
- Amount of phase
 - Flux/sensitivity

Structure factor:

- Atomic positions
- Atomic occ.
- Thermal param.
- Atomic scattering factors

Preferred orientation
(alignment in certain direction)

Absorption

$$y_i^{calc.}(2\theta_i) = s \sum_k L_k |F_k|^2 P_k A_k \phi(2\theta_i - 2\theta_k) + y_i^{background}$$

Lorentz-polarization factor:
monochromator
polarization (0 for neutrons)

Peak profile function:

- Instrumental
- microstructure

Amorphous part
Air scattering
Instr. noise
Incoherent scat.

Phase fraction in Fullprof

$$W_{\phi} = \frac{S_{\phi} (ZMV)_{\phi} \cdot f_{\phi}^2 / \tau_{\phi}}{\sum_{i=1}^{N_{\phi}} S_i \cdot (ZMV)_i \cdot f_i^2 / \tau_i} = \frac{S_{\phi} ATZ_{\phi} \cdot V_{\phi}}{\sum_{i=1}^{N_{\phi}} S_i ATZ_i \cdot V_i}$$

W = weight fraction of the phase

S = scale factor

Z = number of formula units of phase

M = molecular weight of phase

V = unit cell volume of a phase

t = Brindley coefficient (Micro-absorp.)

f = value to transform the site multipl.

To its real value

$$ATZ_i = Z_i M_i f_i^2 / \tau_i$$

ATZ calculated automatically (if you put 0)

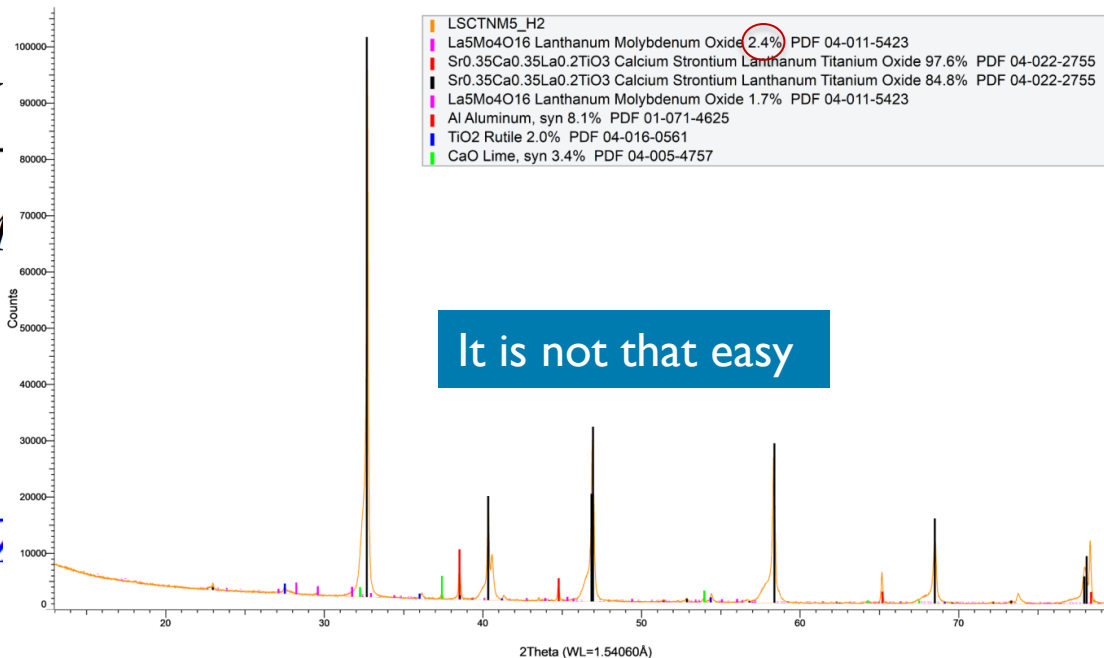
Only crystalline phases!

Phase fraction in Fullprof

$$W_{\phi} = \frac{S_{\phi}(ZMV)}{\sum_{i=1}^{N_{\phi}} S_i(ZM)}$$

ATZ

(Coupled TwoTheta/Theta)

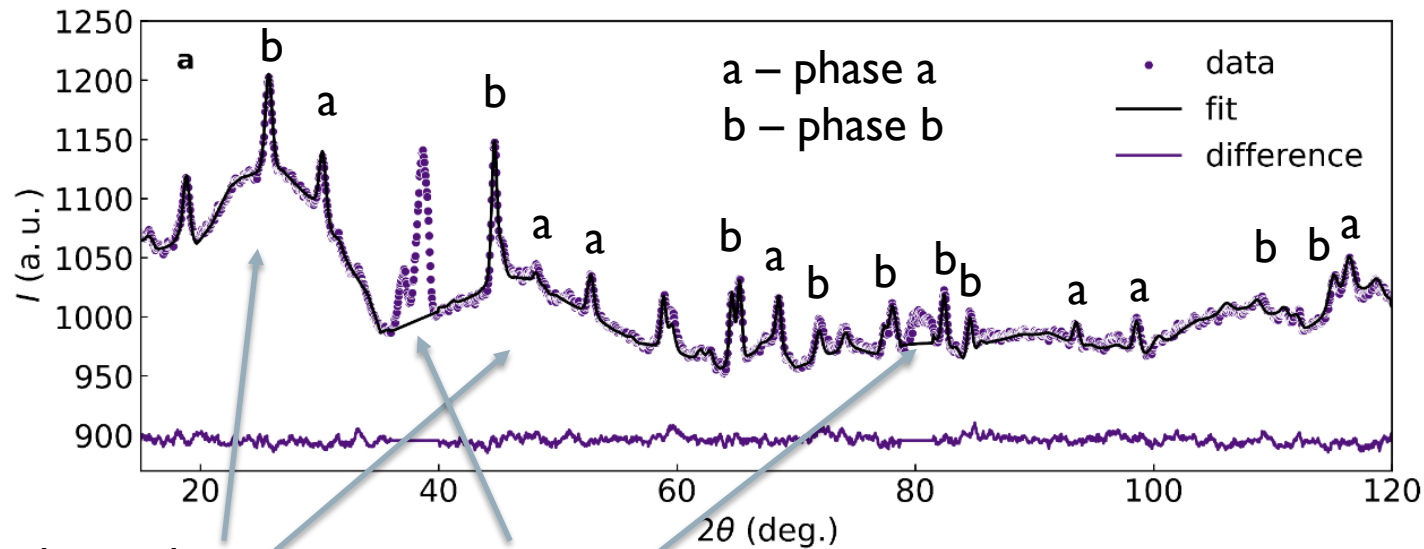


of the phase

in units of phase
 weight fraction
 of a phase
 τ (Micro-absorp.)
 τ the site multipl.

if you put 0)

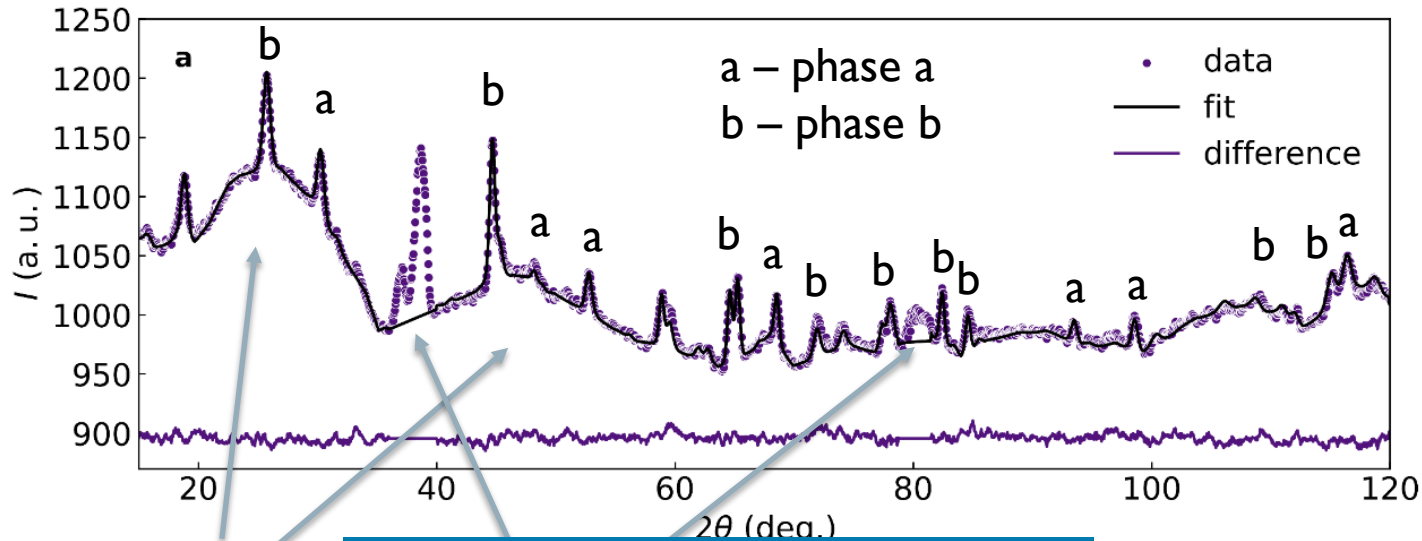
Quantitative analysis



Amorphous phase
(lets presume)

Unknown phase

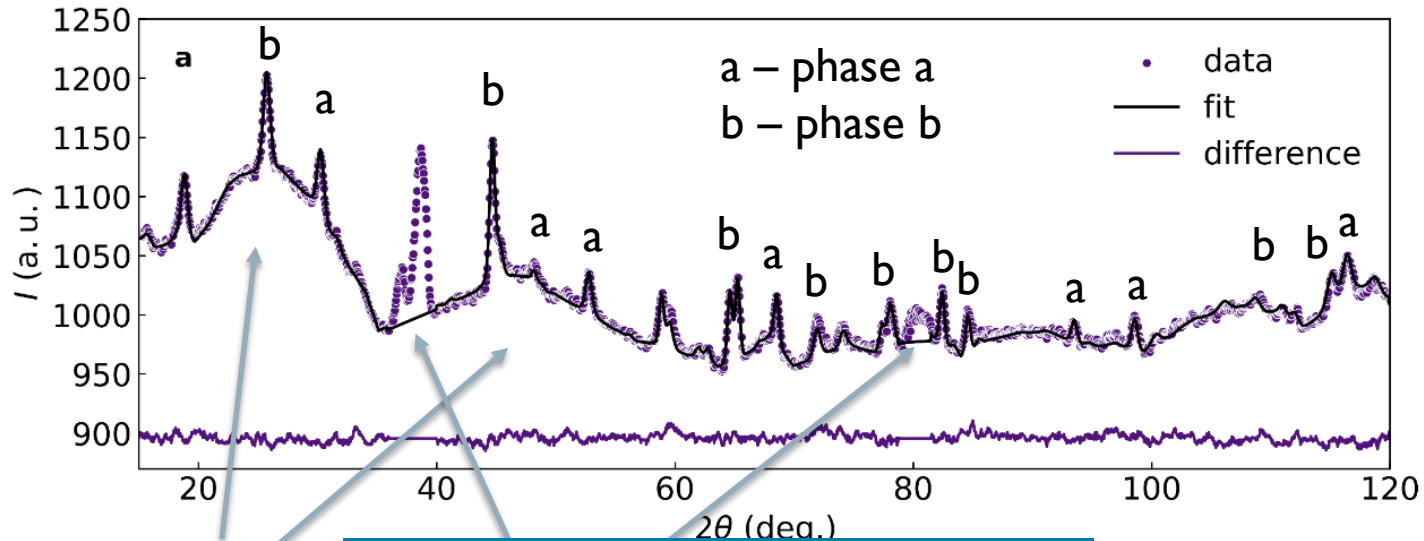
Quantitative analysis exercise



Amorphous phase
(lets presume)

Can we get absolute phase % of a/b?

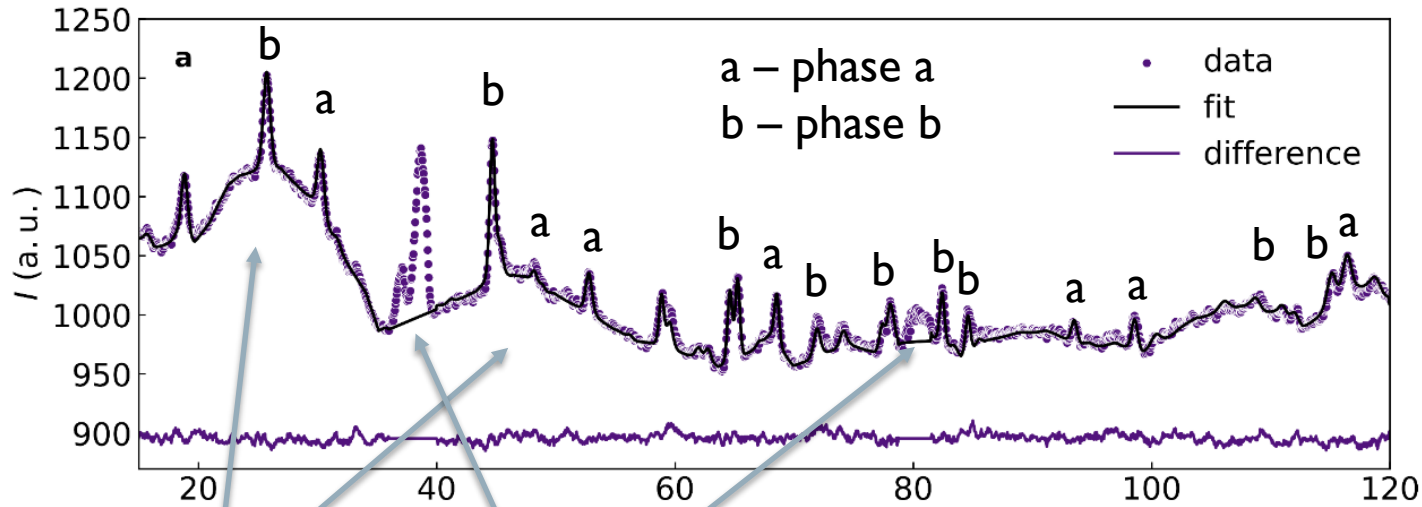
Quantitative analysis exercise



Amorphous phase
(lets presume)

Can we get absolute phase % of a/b?
Can we get their relative phase %?

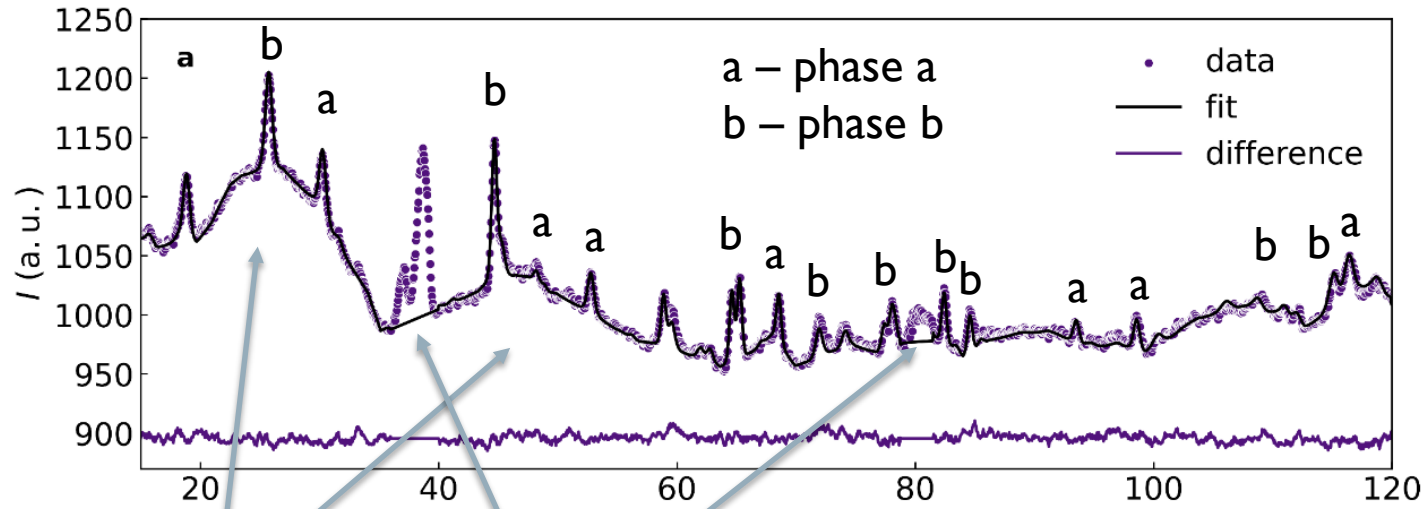
Quantitative analysis exercise



Amorphous phase
(lets presume)

Can we get absolute phase % of a/b?
Can we get their relative phase %?
Is there a way to get absolute phase wt% of a/b?
Is there any way to give wt% to amorphous phase?

Quantitative analysis exercise



Amorphous
(lets presume)

Can we get absolute phase % of a/b? No

Can we get their relative phase %? Yes

Is there a way to get absolute phase wt% of a/b? Internal standard

Is there any way to give wt% to amorphous phase? No

Crystallite size/strain analysis

- Peak broadening:
 - Instrumental broadening
 - Size/strain

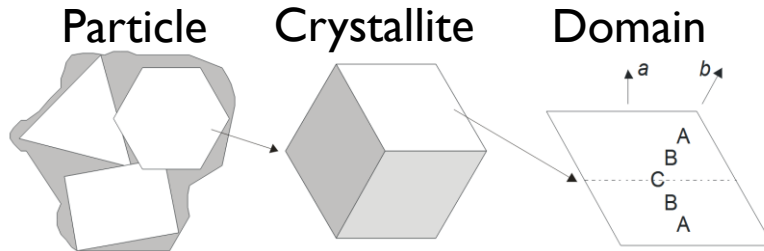
Instrumental broadening needs to be taken into account when doing size/strain analysis

Crystallite size/strain analysis

- Peak broadening:
 - Instrumental broadening
 - Size/strain

Instrumental broadening needs to be taken into account when doing size/strain analysis

- Crystallite size = the size of a single coherent crystal domain that scatters X-rays or neutrons coherently.
 - Perfect Bragg diffraction exists only with infinite crystals, but since that is not the case there is peak broadening
- Crystallite strain = Instead of all lattice planes having exactly the same spacing d , some regions are slightly compressed or slightly stretched.



Topas technical reference

Crystallite size analysis

- Scherrer equation (1918)

$$\beta = \frac{\lambda}{\varepsilon \cos \theta}$$

- β - FWHM (irf corrected)

- λ - wavelength

- ε - crystallite apparent size

- l_{vol} - column size (weighted mean column length)

- k - scherrer constant (depends on crystallite shape)

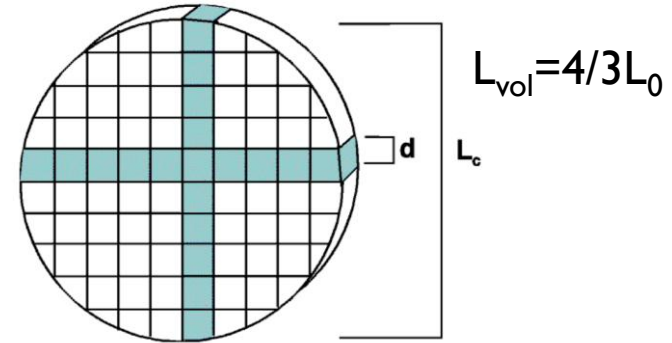
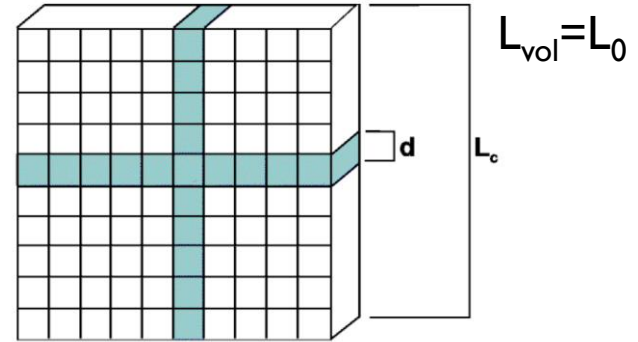
$$\varepsilon = \frac{l_{vol}}{k}$$

$$\beta = \frac{k\lambda}{l_{vol} \cos \theta}$$

- Laue (1926)

$$l_{vol} = \frac{\lambda}{\beta_{ib} \cos \theta}$$

- β_{ib} = Integral breadth (IRF corrected)



Crystallite size analysis

- Scherrer equation (1918)

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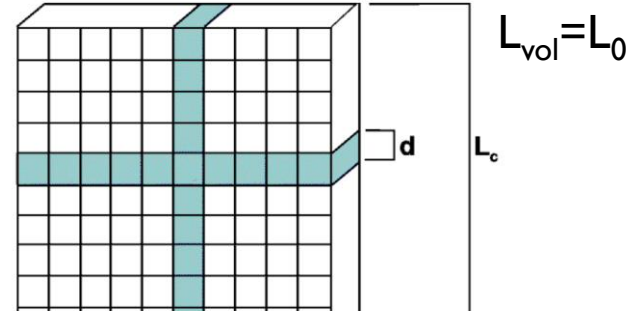
- ε - crystallite apparent size

- l_v

- k

$$\varepsilon = \frac{l_{vol}}{k}$$

$$\beta = \frac{k\lambda}{l_{vol} \cos \theta}$$



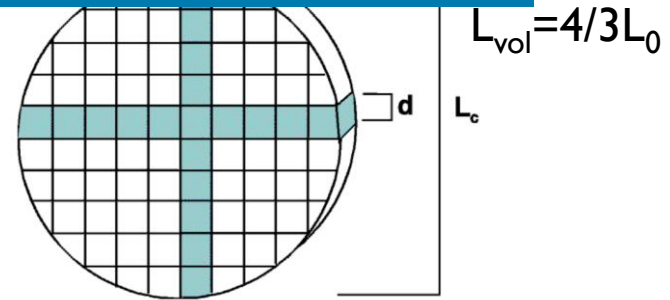
Not the best method (although still widely used)!

Multi peak/whole pattern analysis would give information on anisotropy/strain.

- Laue (1926)

$$l_{vol} = \frac{\lambda}{\beta_{ib} \cos \theta}$$

- β_{ib} = Integral breadth (IRF corrected)



Crystallite strain analysis

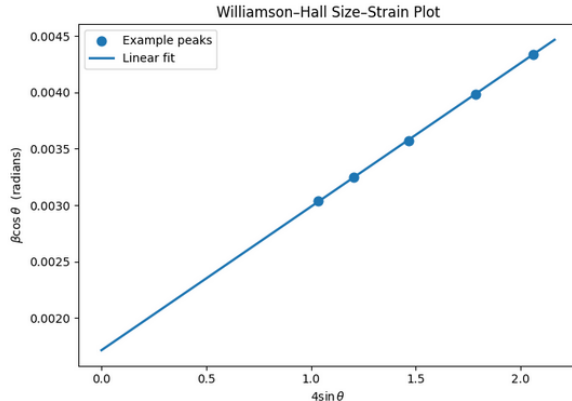
- Williamson and hall (1953)
- Assumption: both size and shape are Lorentzian
 - Can add $\beta = \beta_{size} + \beta_{strain}$
 - $\beta \cos(\theta)$ vs $4\sin(\theta)$: slope – strain, intercept – CS (sometime $2\sin(\theta)$ is used, depending on strain definition)

$$\beta_{size} = \frac{\lambda}{l_{vol} \cos \theta}$$

$$\beta_{strain} = 4\varepsilon \tan \theta$$

$$\beta \cos \theta = \frac{\lambda}{l_{vol}} + 4\varepsilon \sin \theta$$

Williamson–Hall Size–Strain Plot



AI generated plot

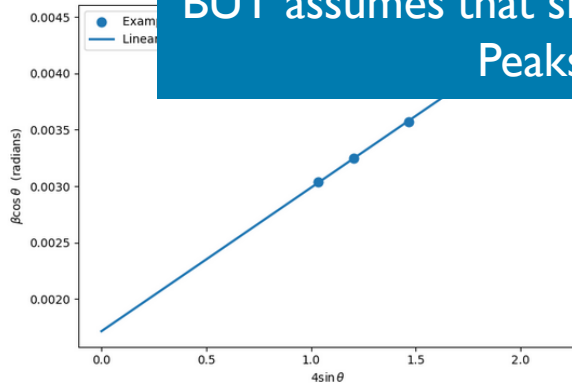
Crystallite strain analysis

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(sometime $2\sin(\theta)$ is used, depending on strain definition)

$$\beta_{size} = \frac{\lambda}{l_{vol} \cos \theta}$$

$$\beta_{strain} = 4\varepsilon \tan \theta$$

Williamson-Hall Size-Strain



Better than Scherrer method,
BUT assumes that size and strain are purely Lorentzian
Peaks must be separated

AI generated plot

Crystallite size/strain analysis (profile fitting)

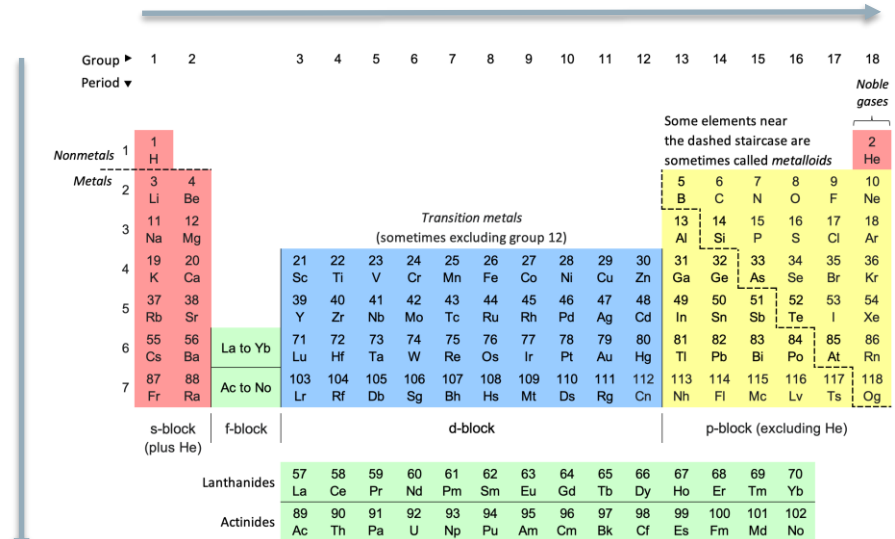
- Double Voigt approach
 - Size broadening ->Voigt function
 - Strain Broadening ->Voigt function
 - Uses full profile (not just width)
- Voigt function – convolution of Lorentzian and Gaussian
- Applied both in Fullprof and Topas
 - Instrumental broadening
 - Topas – FP peak type
 - Fullprof – IRF file
 - Fullprof peak type 7 (Thompson-Cox-Hastings formula)

Allows for more reliable determination of crystallite size and microstrain than simple width-based methods.
Do not trust the absolute values.

Neutrons vs x-rays

X-rays:

- Interact with the electrons.
- Scattered by the electron cloud.
- X-ray form factor (scattering factor) has atomic number dependence.
- „Small penetration depth“ (depends on energy)
 $\text{CuK}\alpha \sim 10 - 20 \mu\text{m}$
 $75 \text{ keV (ID31 ESRF)} \sim 5 - 20 \text{ mm}$
 (depends on materials)



Wikimedia commons

Neutrons vs x-rays

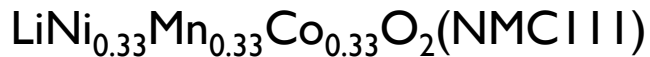
X-rays:

- Interact with the electrons.
- Scattered by the electron cloud.
- X-ray form factor (scattering factor) has atomic number dependence.
 - not so easy to distinguish between „neighbors“
- „Small penetration depth“ (depends on energy)
CuK α \sim 10 – 20 μ m
75 keV (ID31 ESRF) \sim 5 – 20 mm
(depends on materials)

neutrons:

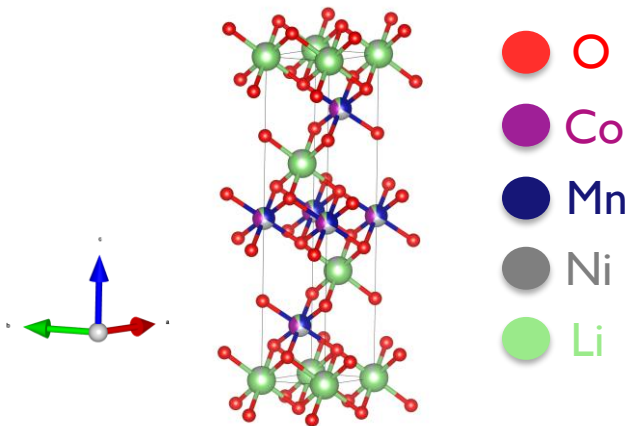
- Interact with nuclei (strong nuclear force).
- Point scattering from nuclei.
 - Strong reflections also at high angle.
- Scattering length density is „random“.
- Deep penetration depth.
- Isotope sensitive.
- Magnetic structure.
 - Neutrons have a spin (1/2), an additional scattering due to dipole-dipole interaction.

Neutrons vs x-rays

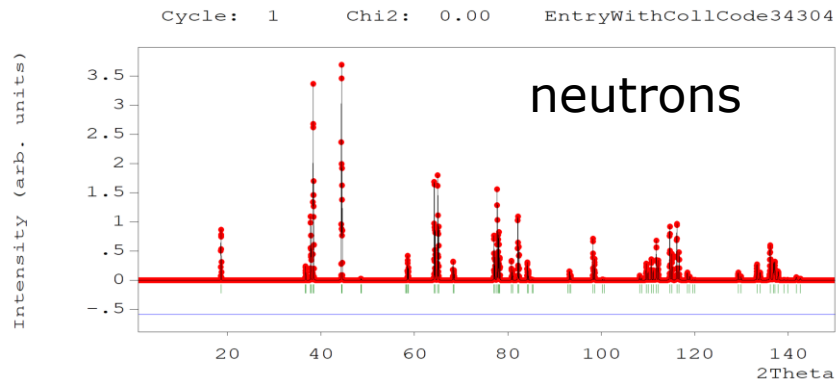
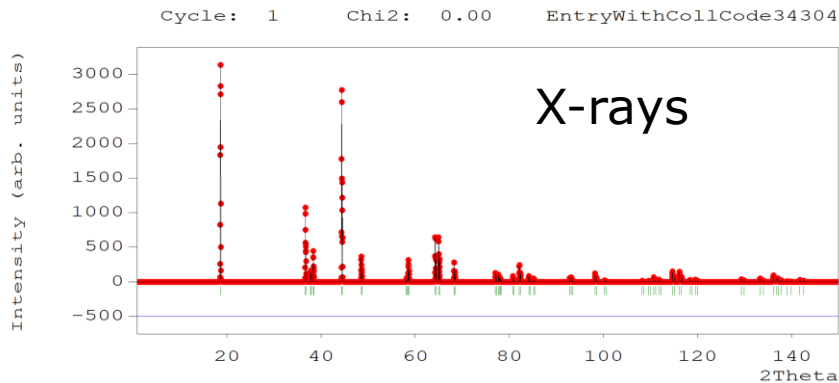


_atom_site_occupancy

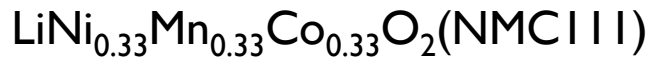
```
Li1 Li1+ 3 a 0 0 0 0.025 0.92(4)
Co1 Co3+ 3 b 0 0 0.5 0.015(9) 0.3333
Ni1 Ni3+ 3 b 0 0 0.5 0.015(9) 0.26(4)
Mn1 Mn3+ 3 b 0 0 0.5 0.015(9) 0.3333
O1 O2- 6 c 0 0 0.245(4) 0.017(2) 1
Li2 Li1+ 3 b 0 0 0.5 0.015(9) 0.08(4)
Ni2 Ni3+ 3 a 0 0 0 0.025 0.08(4)
```



Simulated patterns

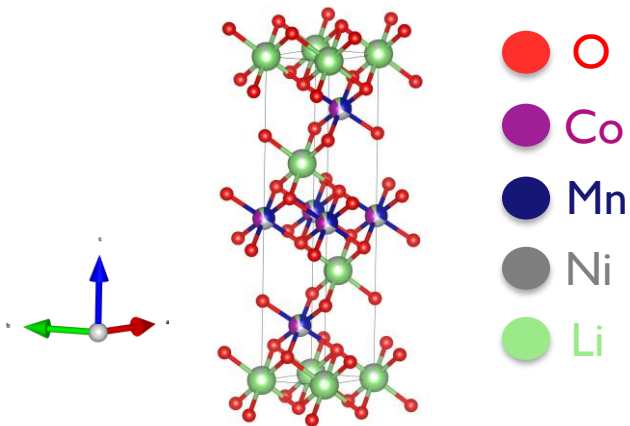


Neutrons vs x-rays

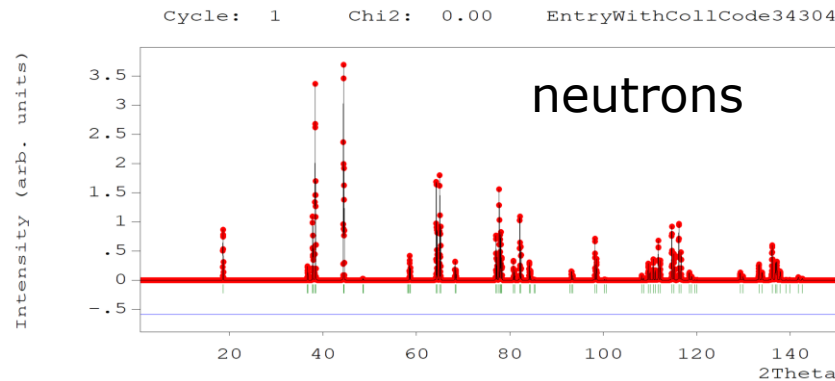
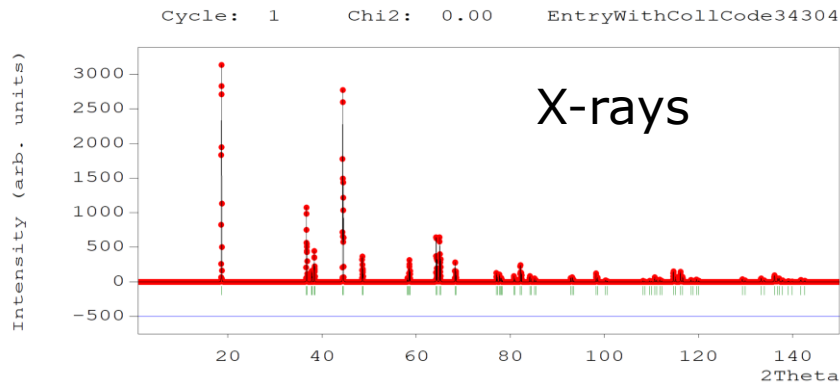


	Mn	Co	Ni
Neutron cross-sec	-3.75	2.490	10.30
X-rays z	25	27	28

https://www.ncnr.nist.gov/resources/activation/scattering_table.html#mn



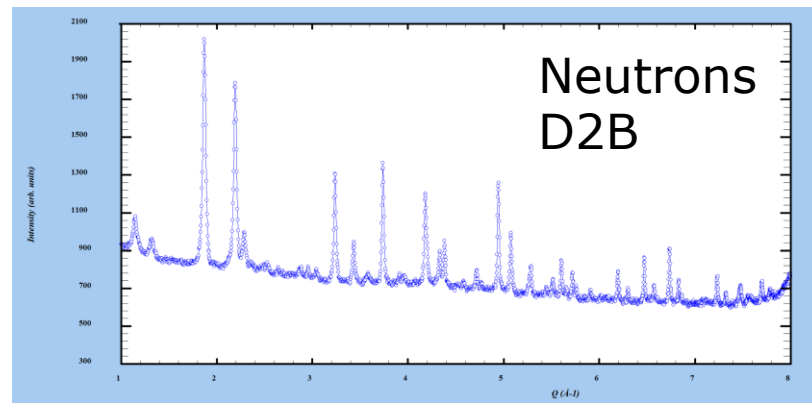
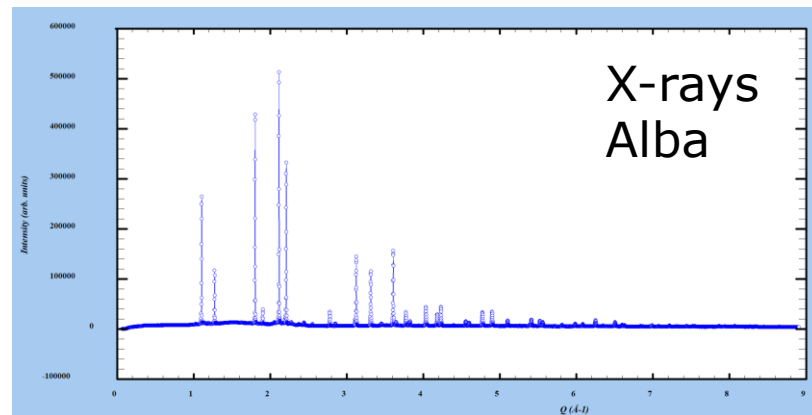
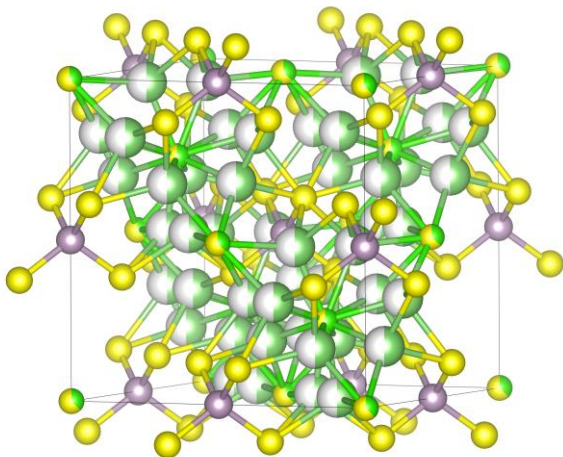
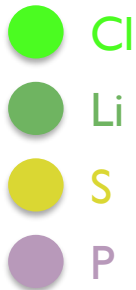
Simulated patterns



Neutrons vs x-rays

Li₆PS₅Cl (MSE)

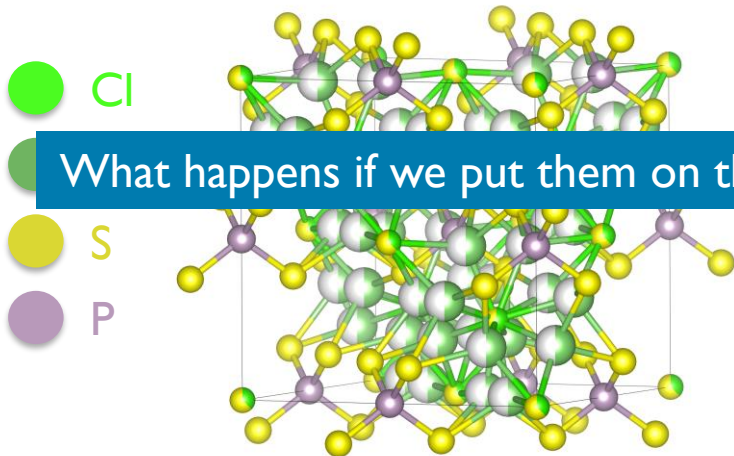
```
Li1 Li1+ 48 h 0.3202 0.0183 0.6798 5.5 0.5
Cl1 Cl1- 4 a 0 0 1 3.94(9) 0.385
Cl2 Cl1- 4 d 0.25 0.25 0.75 2.96(8) 0.615
P1 P5+ 4 b 0 0 0.5 2.49(3) 1
S1 S2- 4 d 0.25 0.25 0.75 2.96(8) 0.385
S2 S2- 16 e 0.1200(2) -0.1200(2) 0.6200(2) 4.48(5) 1
S3 S2- 4 a 0 0 1 3.94(9) 0.615
```



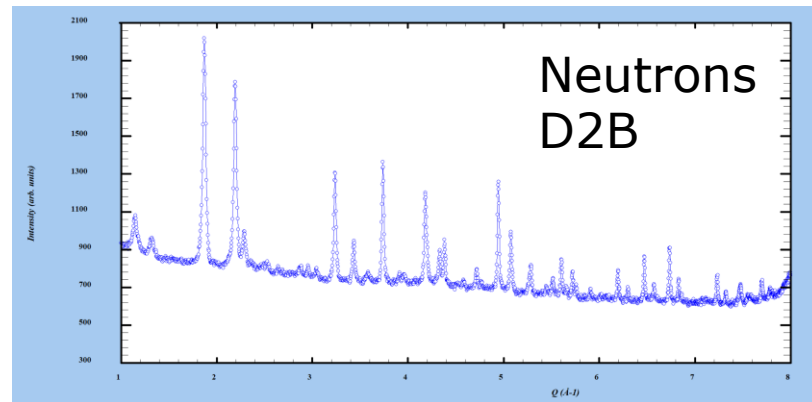
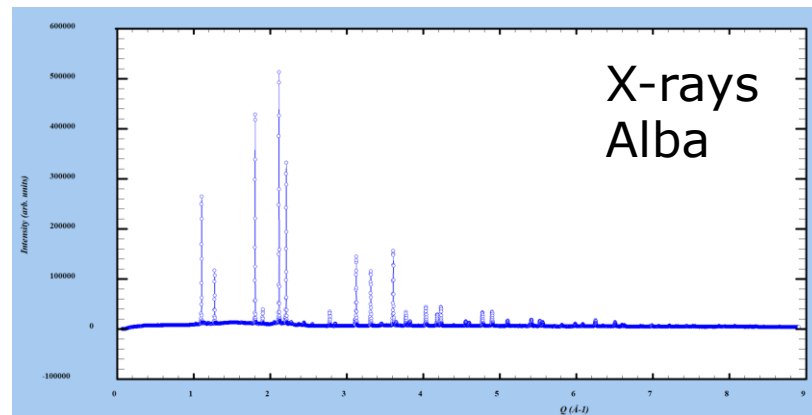
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S2 S2- 16 e 0.1200(2) -0.1200(2) 0.6200(2) 4.48(5) 1
S3 S2- 4 a 0 0 1 3.94(9) 0.615
```



What happens if we put them on the same graph?



Neutrons vs x-rays (in general)

X-rays (synchrotron):

- Possibility of lab-scale
- Super high flux
- Fast measurements
- Lower penetration
 - Less choice for sample cells
- Sensitive to heavy elements
- No magnetic structure
- Possibility of profiling, and special methods (XRD-CT)

neutrons:

- No lab-scale
- Good to determine atomic positions, isothermic factors
- Slower measurements
- Higher penetration
 - Sample cell versatility (no hydrogen containing plastic)
- Sensitive to light elements
- Magnetic structure

Microstructure

Neutrons vs x-rays (in general)

X-rays (synchrotron):

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neutrons:

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- Higher penetration
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- Sensitive to light elements
- Magnetic structure

Why not use both ? measurements

Microstructure

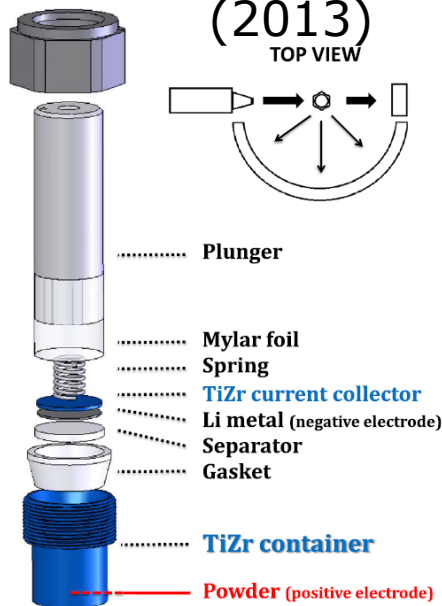
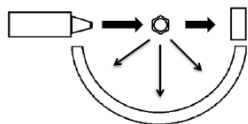
Neutron *operando* cells for EC

Neutrons can have **negative** scattering lengths (wave is shifted in phase by π (180°) relative to the incident wave)

Bianchini et al., J. Electrochem. Soc., 160 (11) A2176-A2183 (2013)

ILLBAT#1

(2013)
TOP VIEW



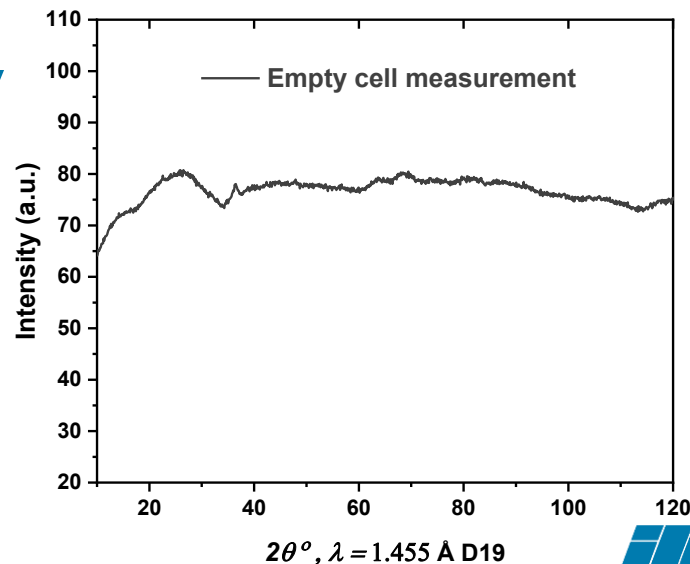
Ti_{2.08}Zr
Null-matrix Alloy

$$b_{\text{Ti}} = -3.44 \text{ fm}$$

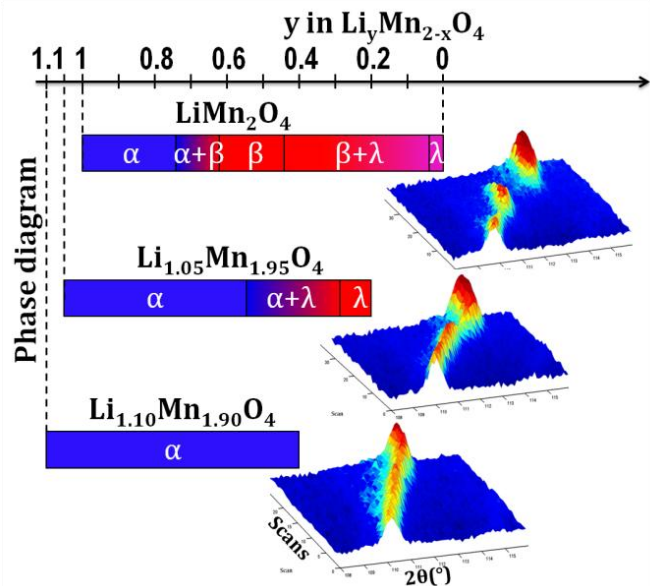
$$b_{\text{Zr}} = 7.16 \text{ fm}$$



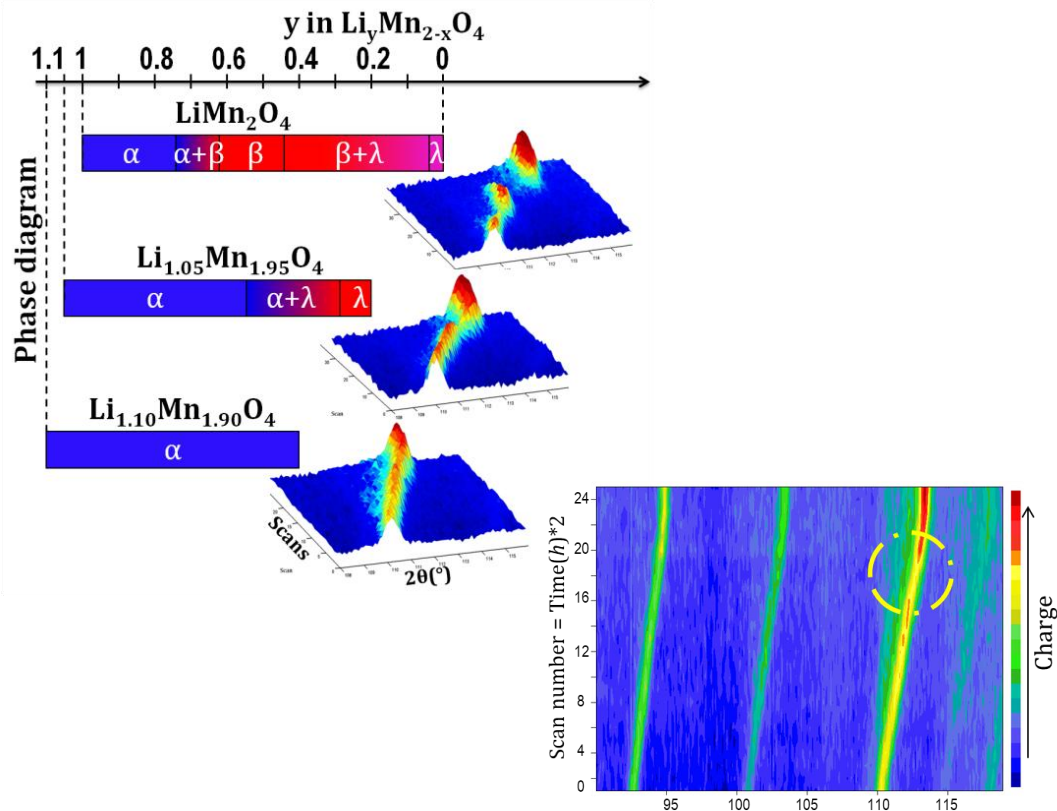
Prof. Matteo Bianchini



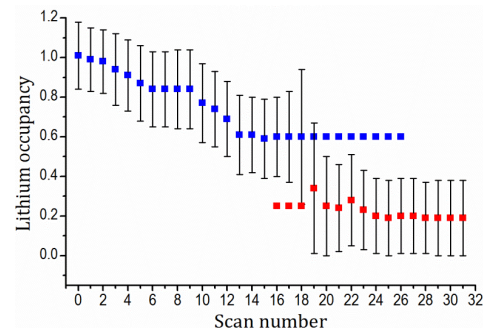
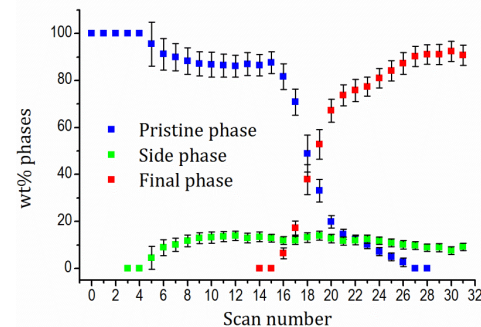
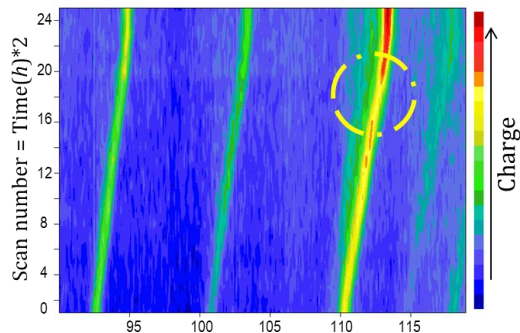
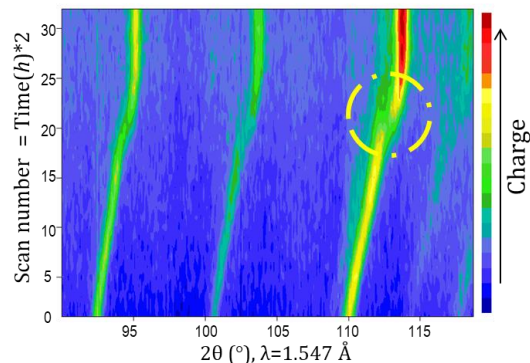
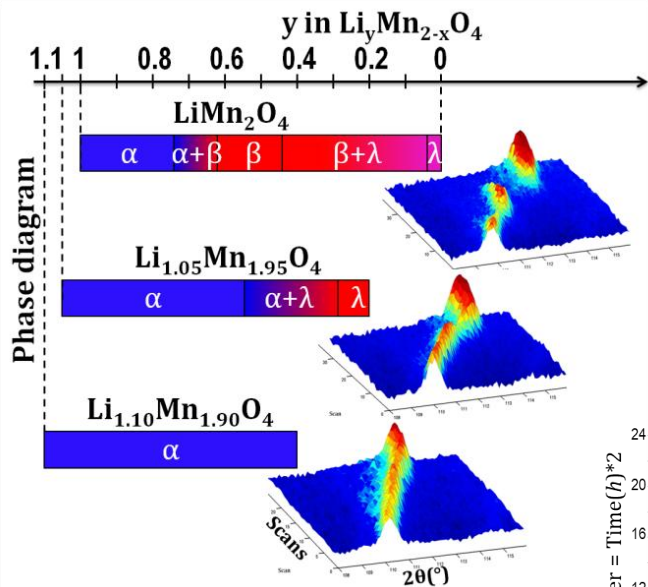
$\text{Li}_{1+x}\text{Mn}_{2-x}\text{O}_4$ *operando* cycling



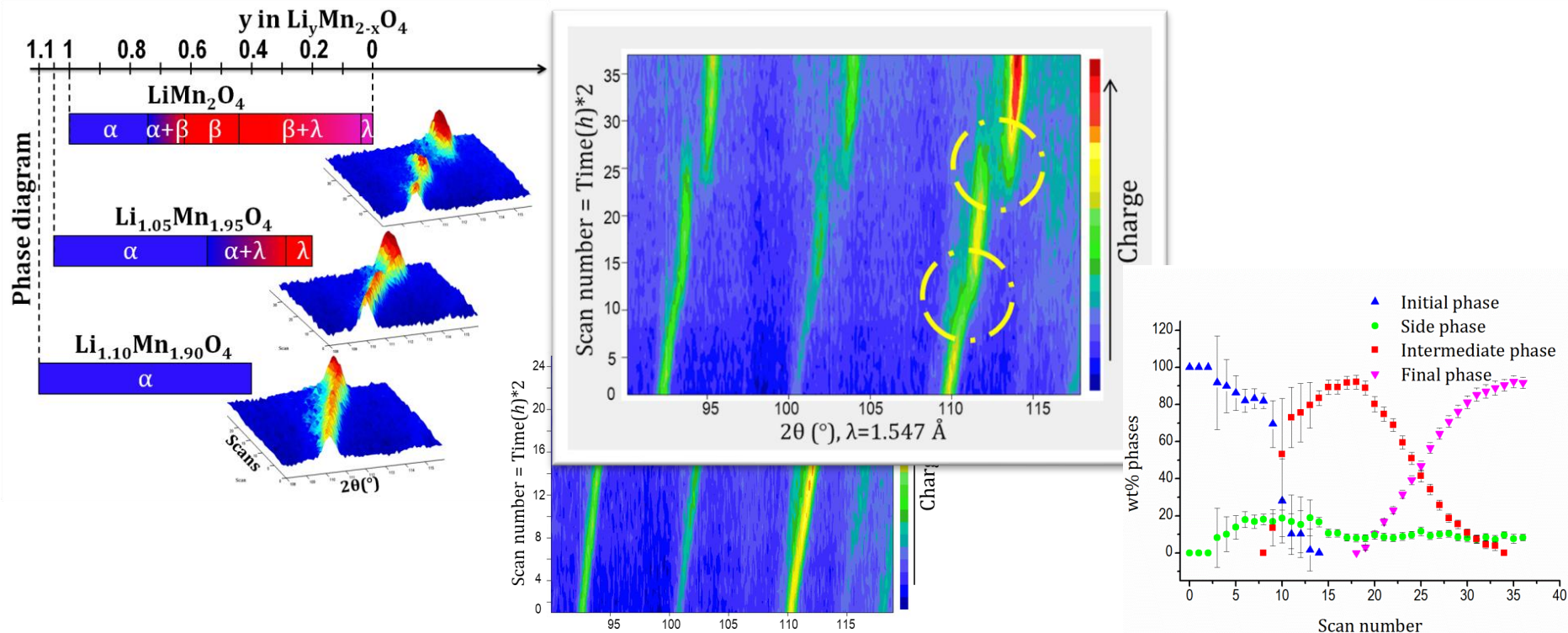
$\text{Li}_{1+x}\text{Mn}_{2-x}\text{O}_4$ *operando* cycling



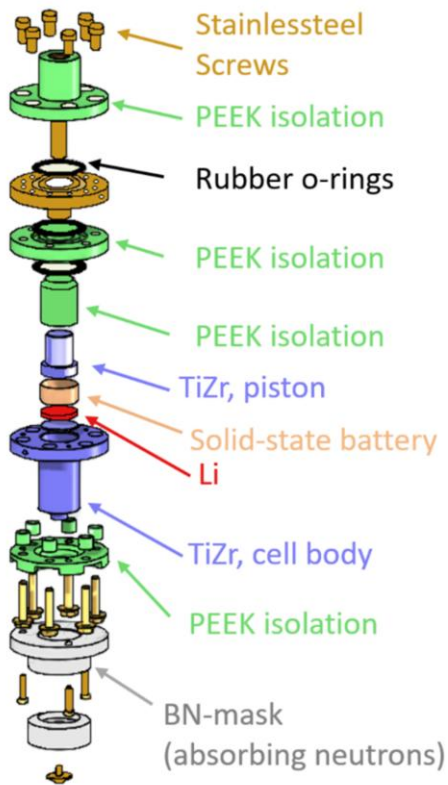
Li_{1+x}Mn_{2-x}O₄ *operando* cycling



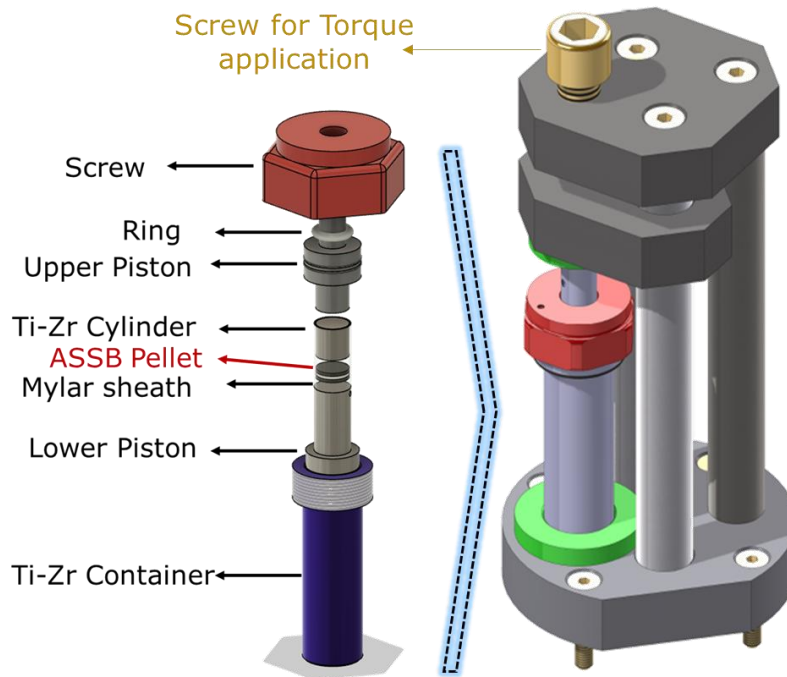
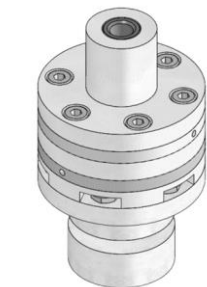
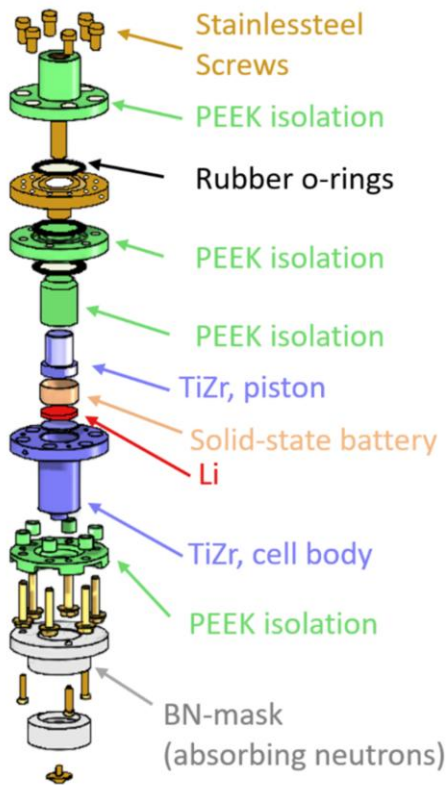
$\text{Li}_{1+x}\text{Mn}_{2-x}\text{O}_4$ *operando* cycling



Cycling of solid-state batteries



Cycling of solid-state batteries

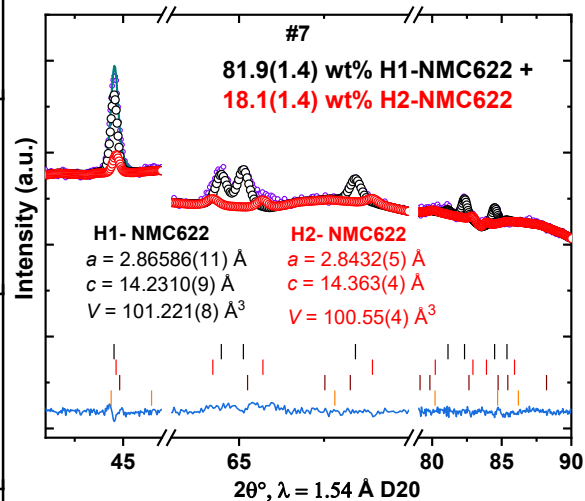
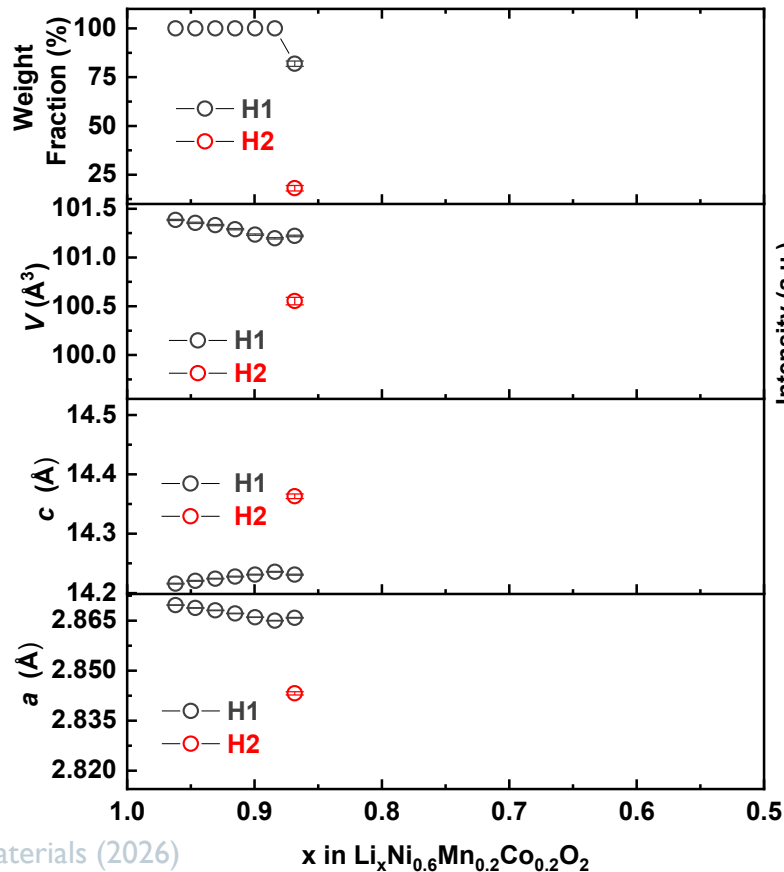
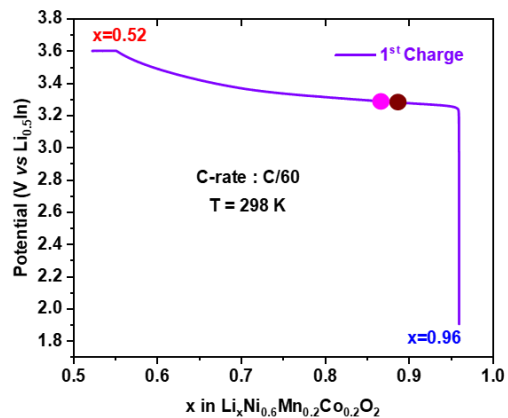


Dr. Anil Kumar



S.A.Kumar et al. Advanced Energy Materials (2026)

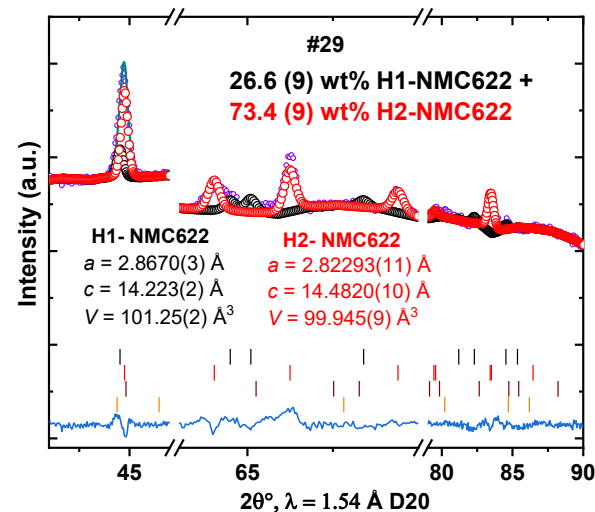
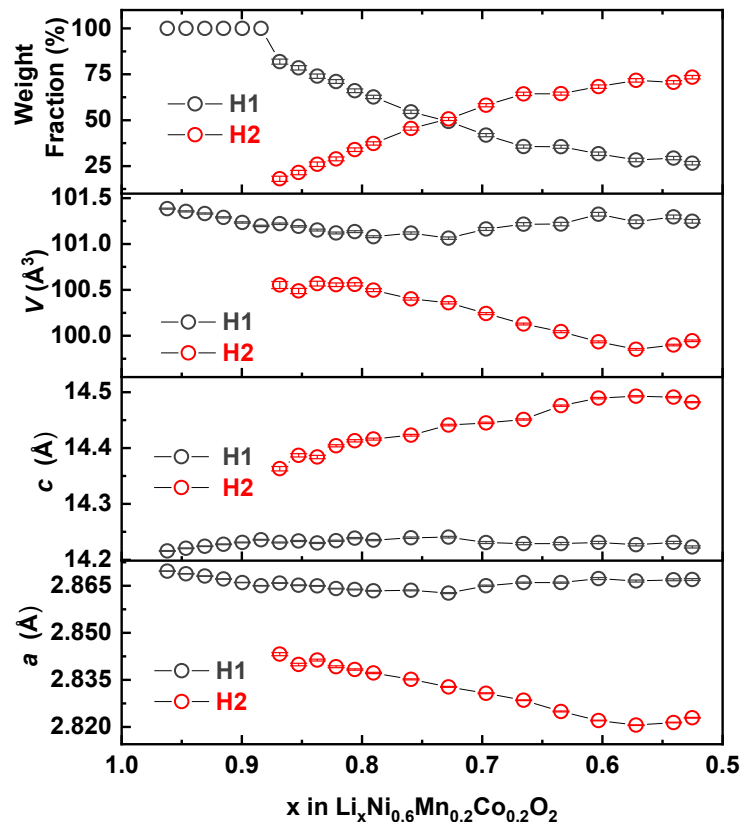
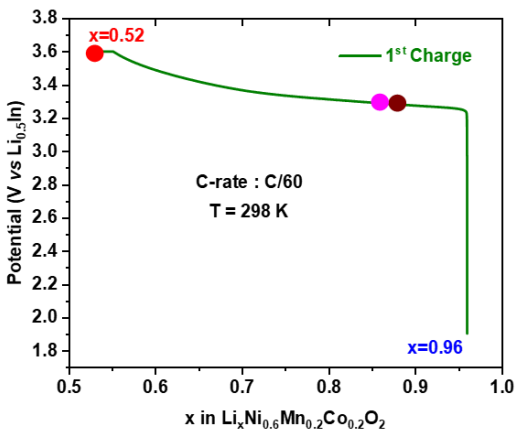
Cycling of solid-state batteries



Solid solution
mechanism until:
 $\text{Li}_{0.88}\text{NMC622}$ structure

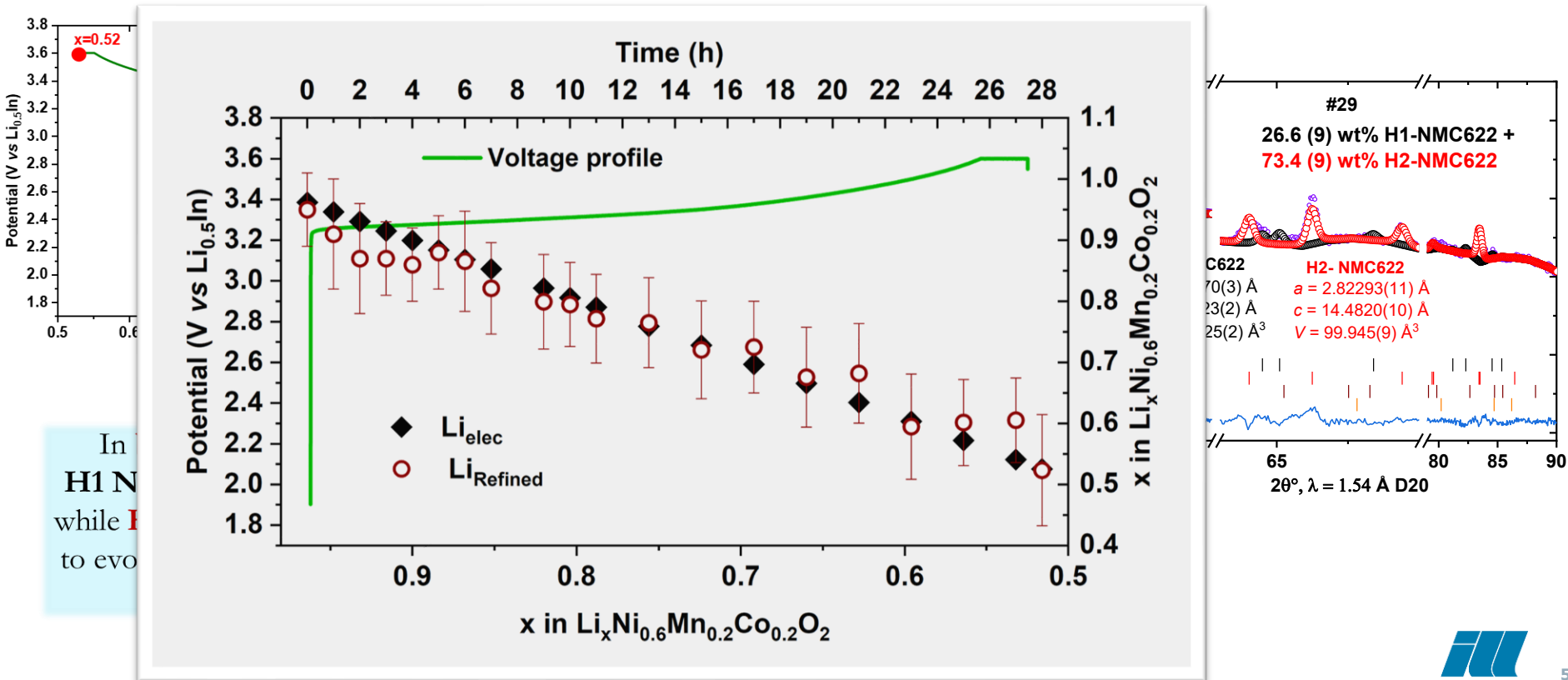
In **biphasic** regime: :
H1 phase \rightarrow $\text{Li}_{0.88}\text{NMC622}$
structure

Cycling of solid-state batteries



In **biphasic** regime:
H1 NMC remains stable
while H2 NMC continues
to evolve in structure and
composition

Cycling of solid-state batteries



In
H1 N
while I
to evo

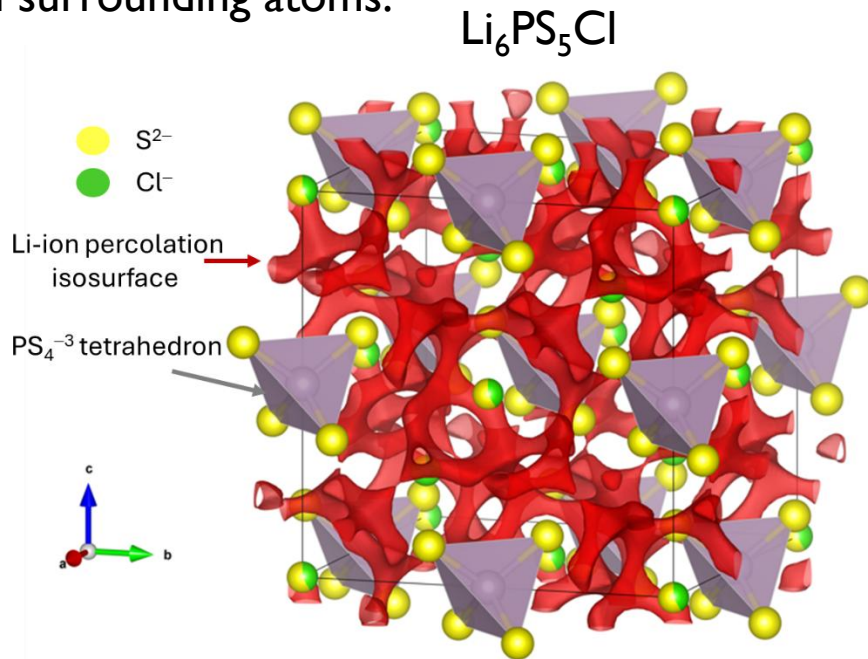
Bond valence energy landscapes

BVEL is a semi-empirical method based on the bond valence model.

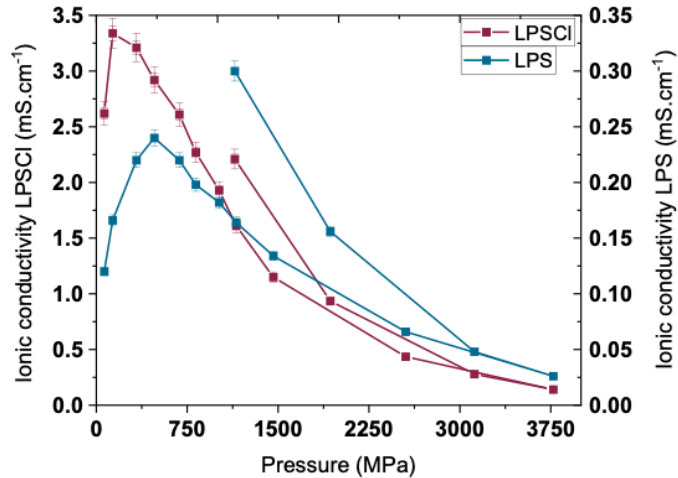
It estimates the energy of placing an ion in the structure using bond valence mismatch with surrounding atoms.

Workflow:

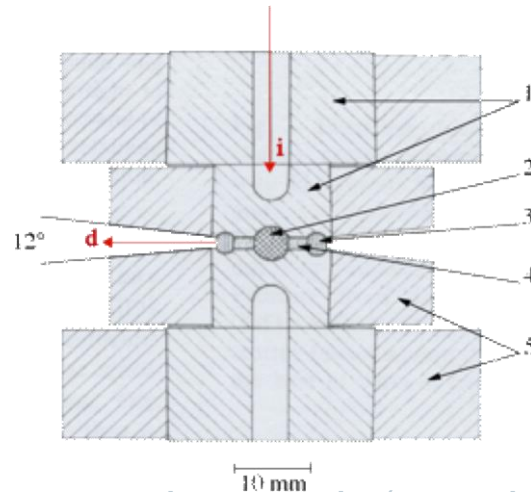
- Refine structure (Fullprof)
- Export CIF
- Remove mobile ions
- Run BVEL calculation
- Visualize pathways



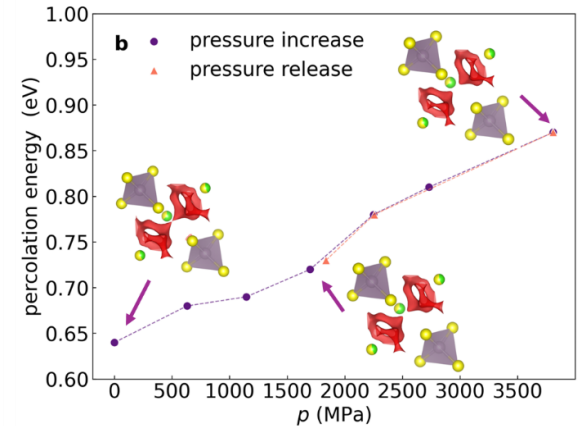
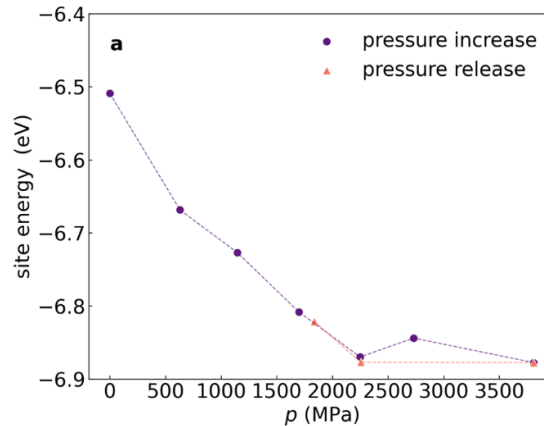
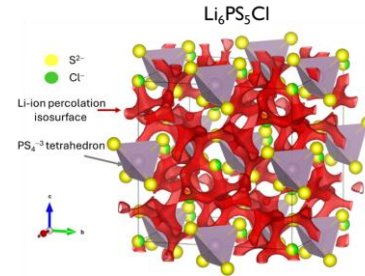
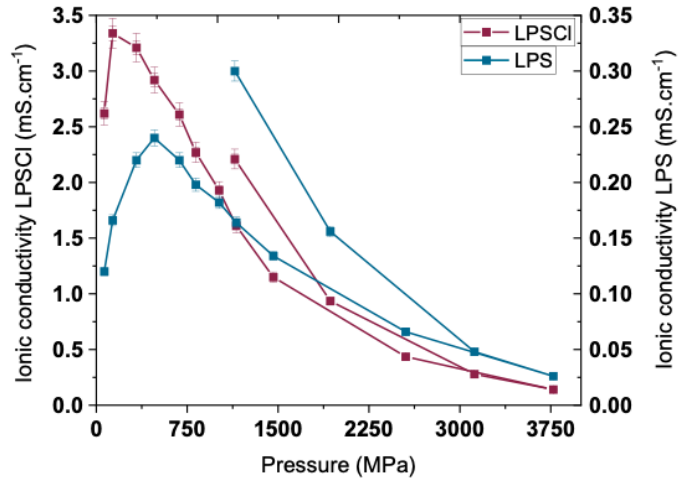
High pressure application on LPSCI



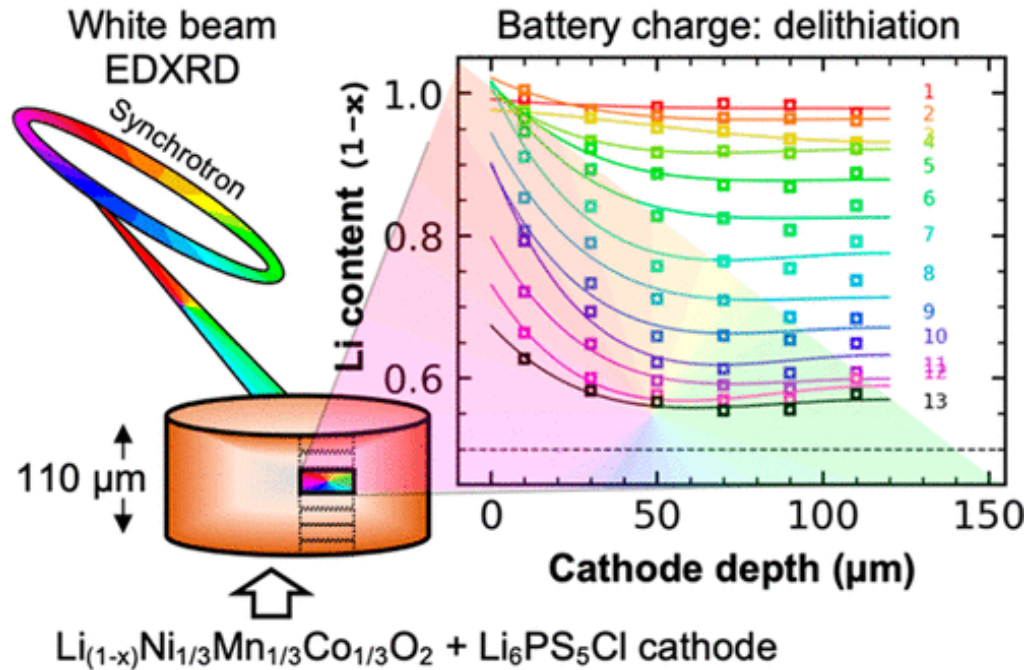
10 GPa maximum
Ø3 x 0.6mm < 10 GPa
Ø6 x 0.6mm < 5 GPa



High pressure application on LPSCI

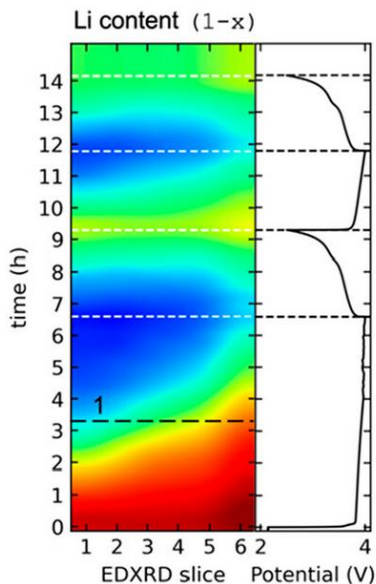


Depth profiling using at synchrotron

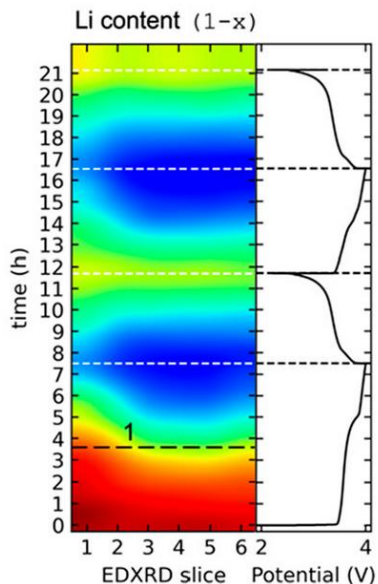


Depth profiling using at synchrotron

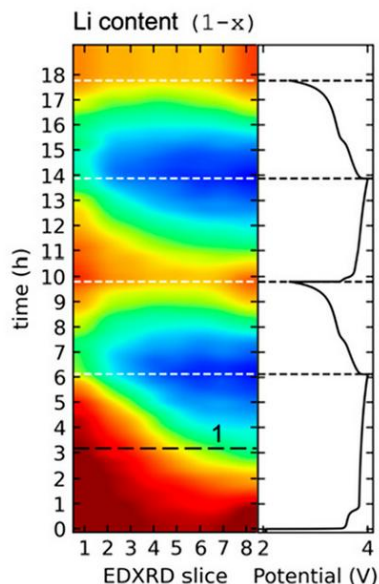
(a) 80% CAM cell



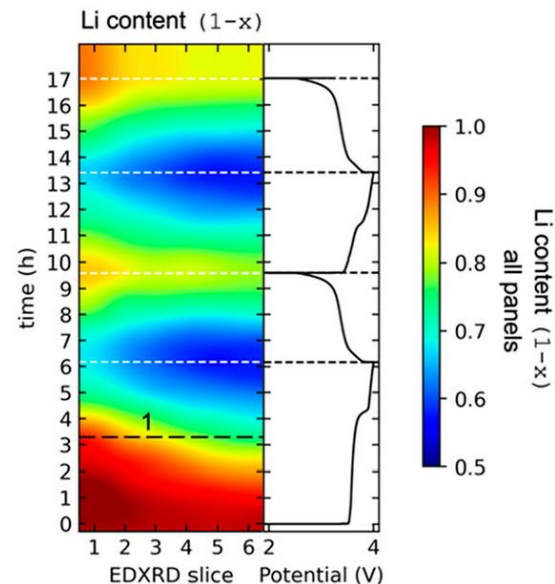
(b) 70% CAM cell



(c) 40% CAM cell

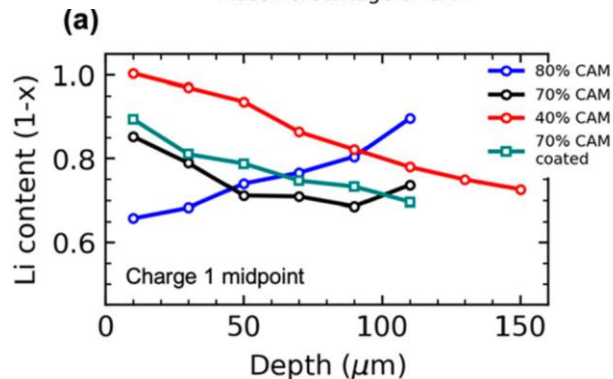
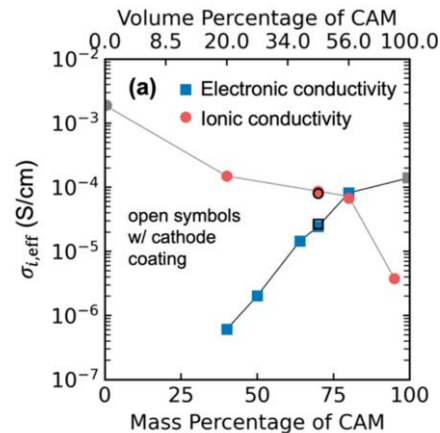
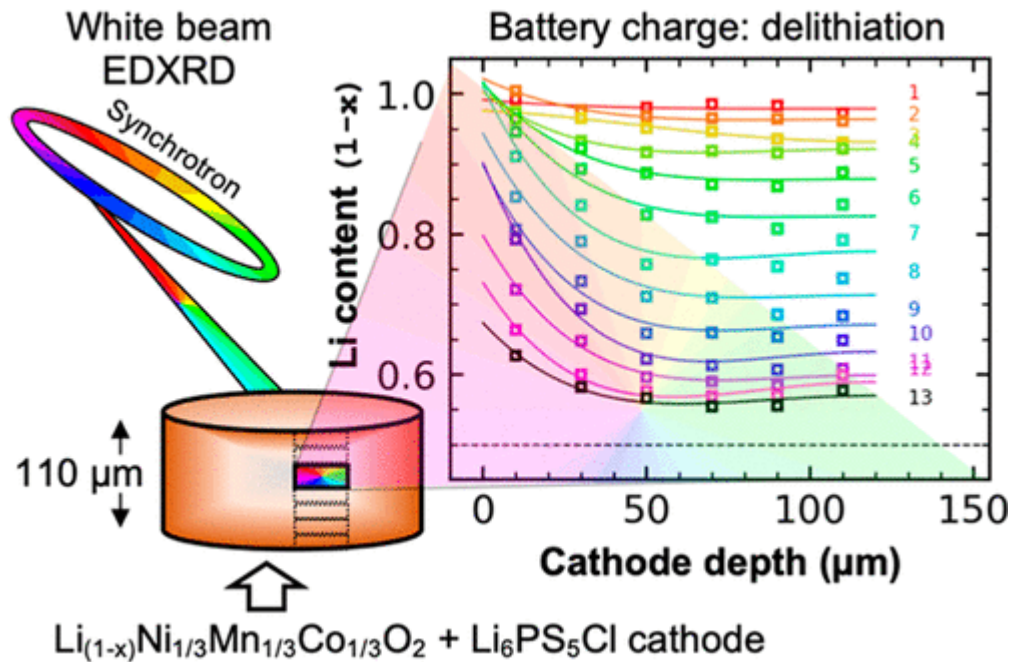


(d) 70% CAM cell with cathode coating

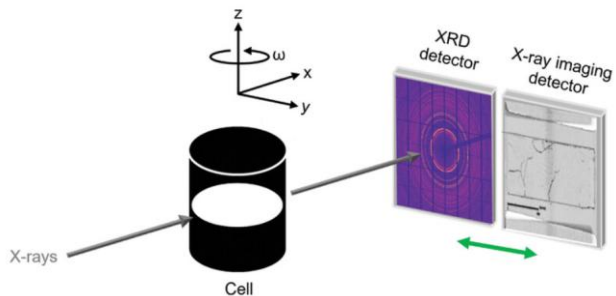


1 slice 20 μm

Depth profiling using at synchrotron



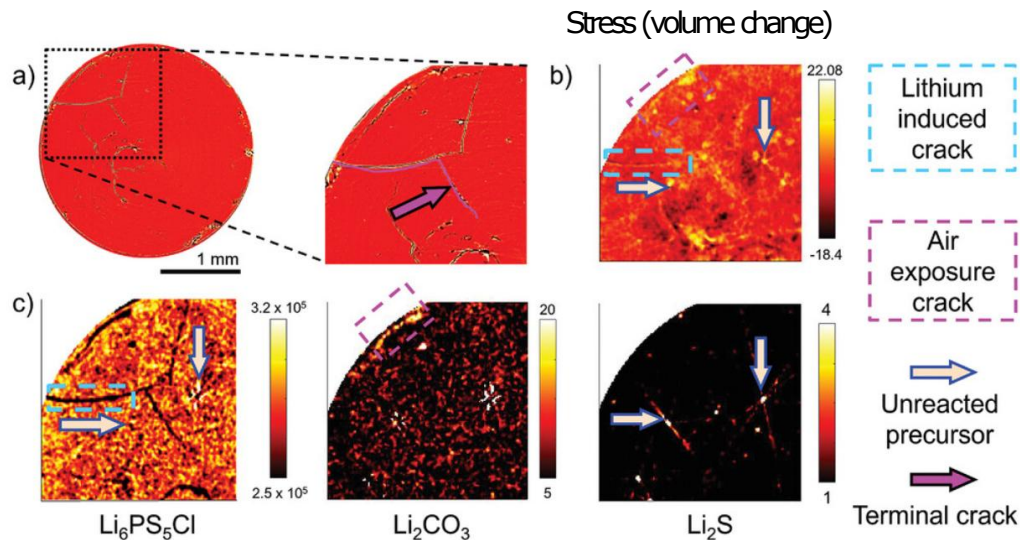
XRD-CT



$$\mathcal{E} = \frac{a_{\text{Li}_6\text{PS}_5\text{Cl}}^3 - a_{\text{mean}}^3}{a_{\text{mean}}^3}$$

a_{mean} – LP at bulk

LPSCl degradation Li|Li₆PS₅Cl|Li

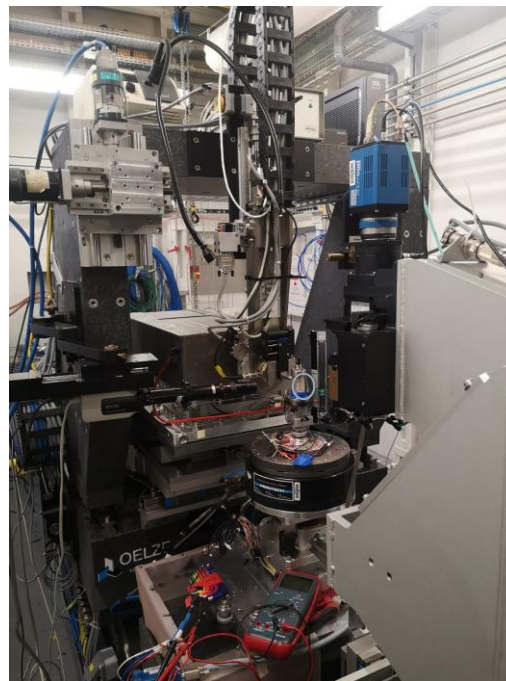
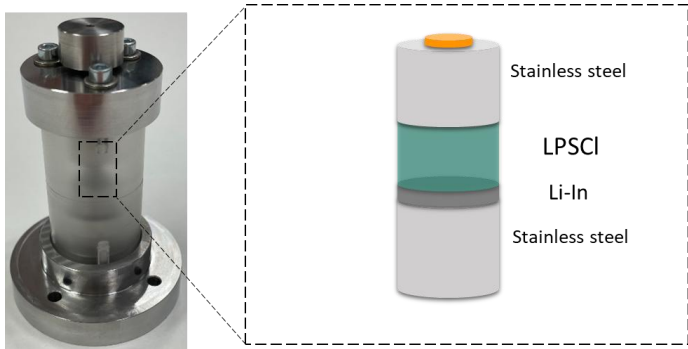


Rietveld refinement(topas7):
(wt%, LP)

XRD-CT

0 – 2V vs Li-In

Li-In | LPSCI | Stainless steel



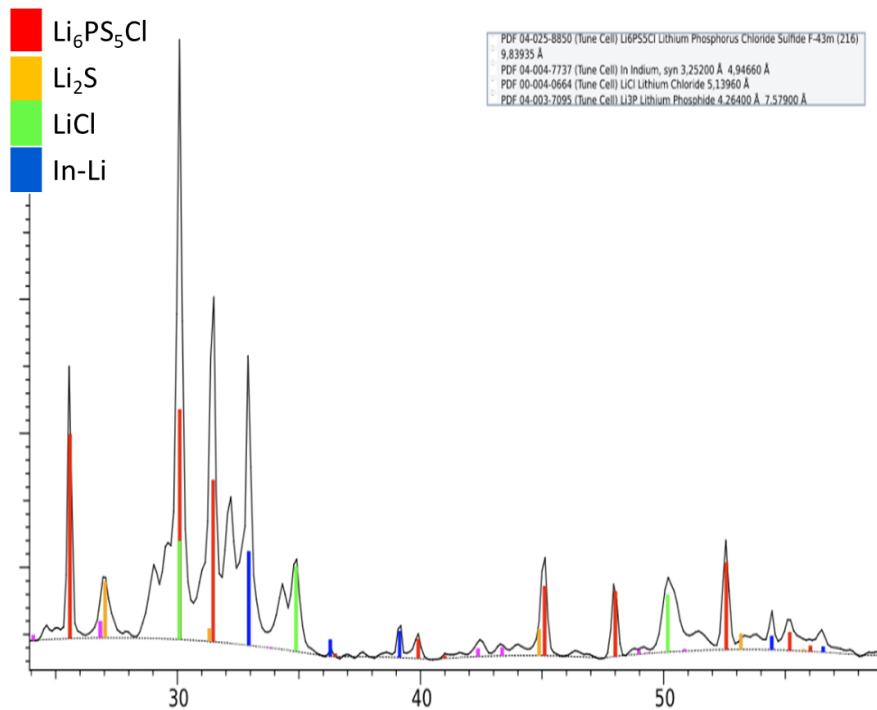
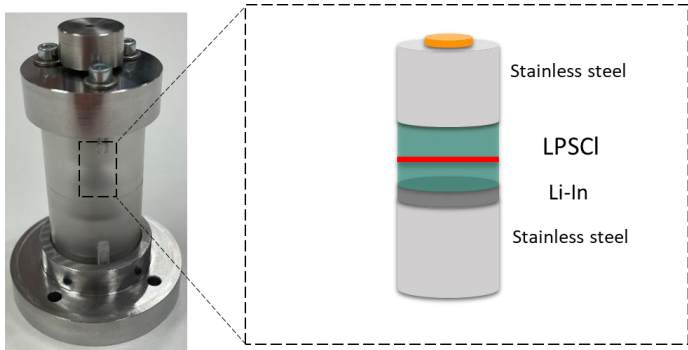
Oskar Thompson



XRD-CT

0 – 2 V vs Li-In

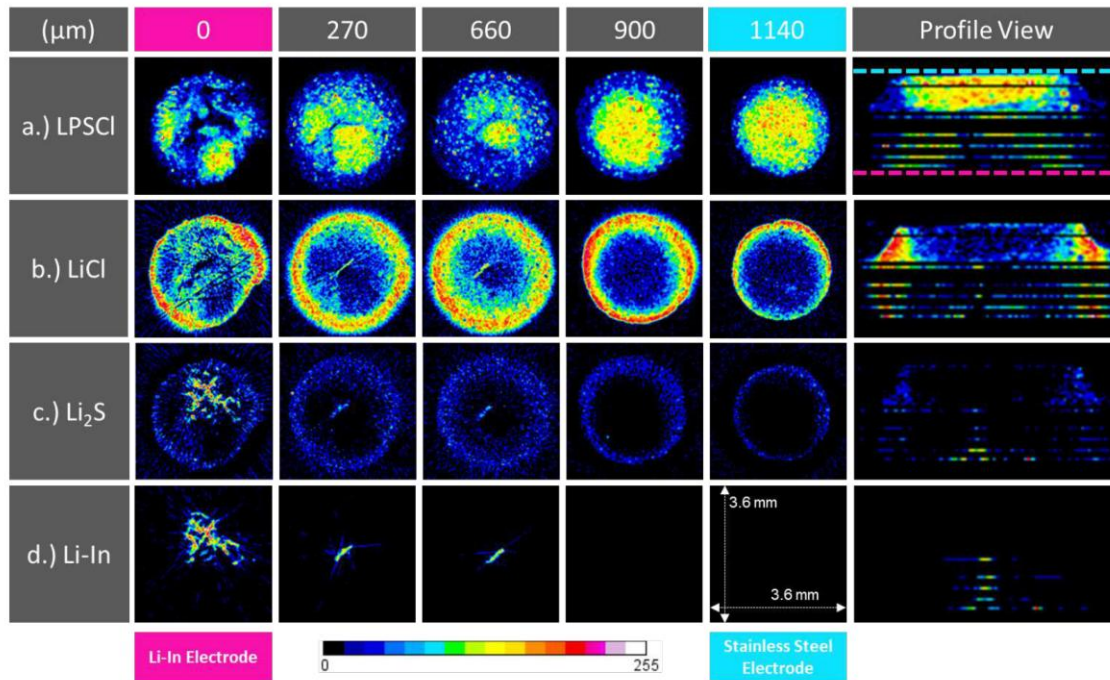
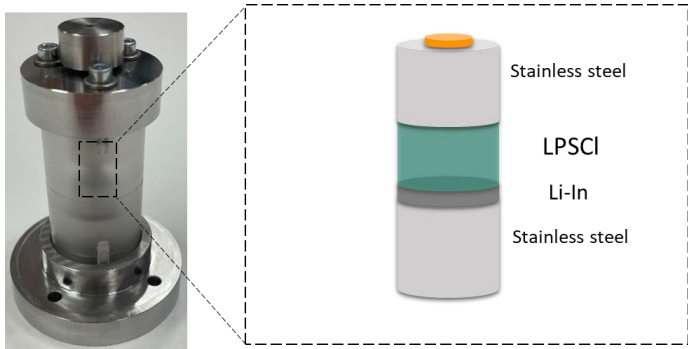
Li-In | LPSCI | Stainless steel



XRD-CT

0 – 2 V vs Li-In

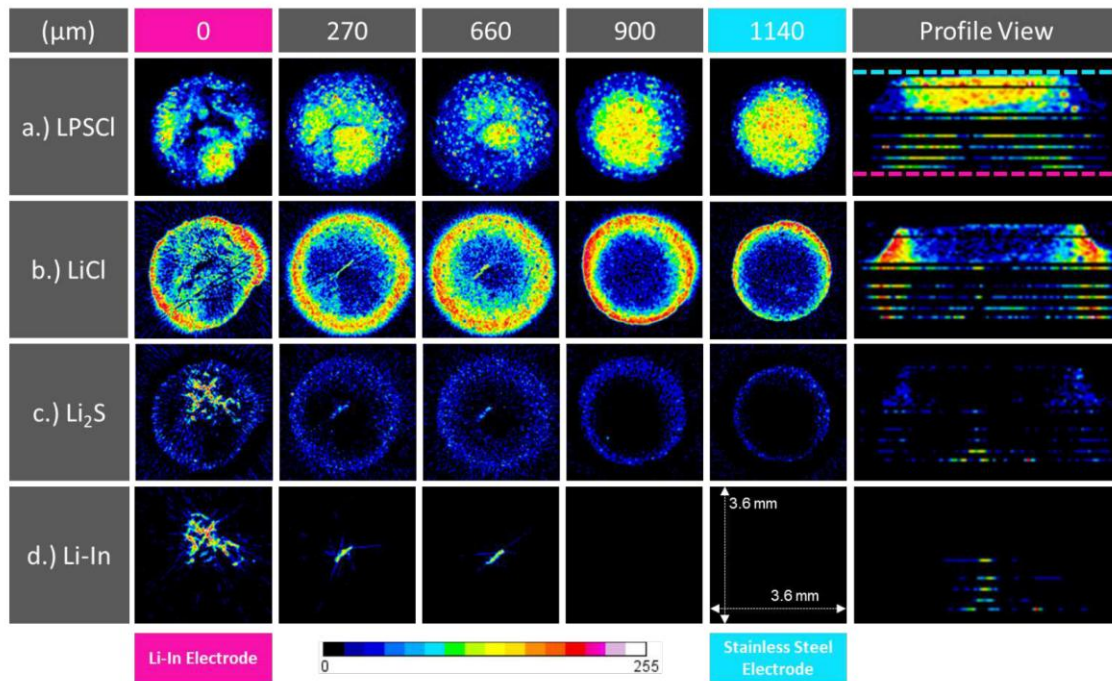
Li-In | LPSCI | Stainless steel



XRD-CT



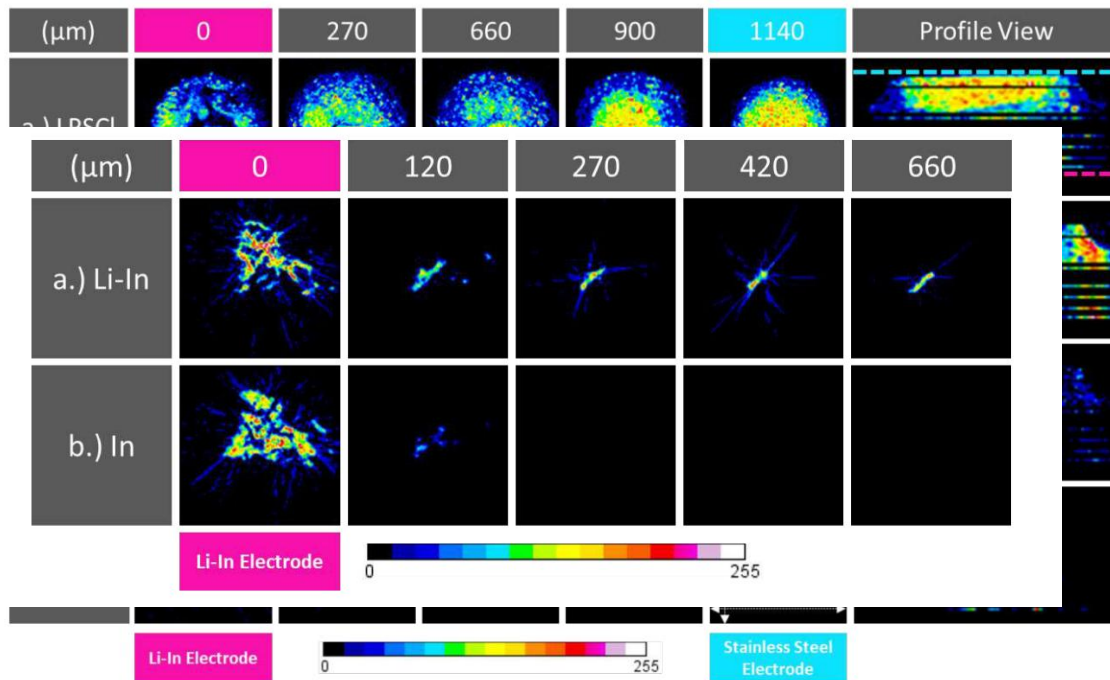
- LPSCI/LiCl signal inversely proportional
- Porosity is greater around the perimeter of the cell
- Perimeter porosity appears to be correlated to degradation



XRD-CT



- Li/In-phases with different Li-content



Thank You





INSTITUT LAUE-LANGEVIN