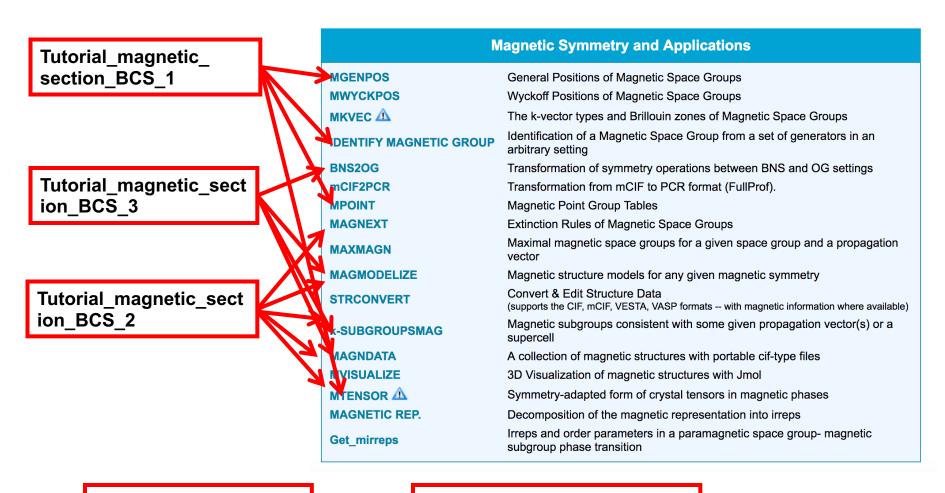




# Hands-on demonstration of BCS (MAXMAGN, MVISUALIZE, k-SUBGROUPMAG...)

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BILBAO, SPAIN

# Three main tutorials on the programs of the BCS Magnetic Section can be directly downloaded from the webpages of the programs :

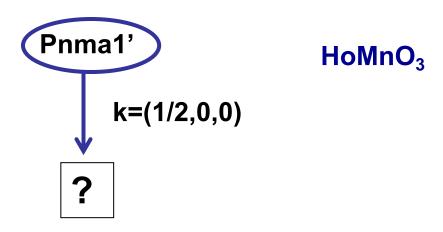


Tutorial-MAXMAGN (3 versions)

Tutorial-k-SUBGROUPSMAG (3 versions)

# Symmetry based modeling of magnetic structures

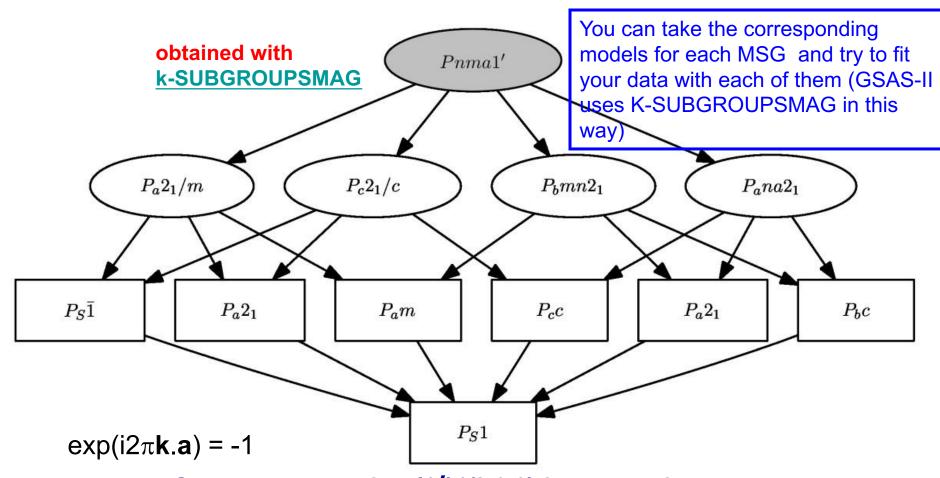
Which MSGs are possible for a magnetic structure having space group Pnma in the paramagnetic phase if we know that the magnetic ordering has propagation vector (wave vector!) k=(1/2,0,0)?



Purely mathematical problem!

# Symmetry based modeling of magnetic structures

Possible magnetic symmetries for a magnetic phase with propagation vector (1/2,0,0) and parent space group Pnma

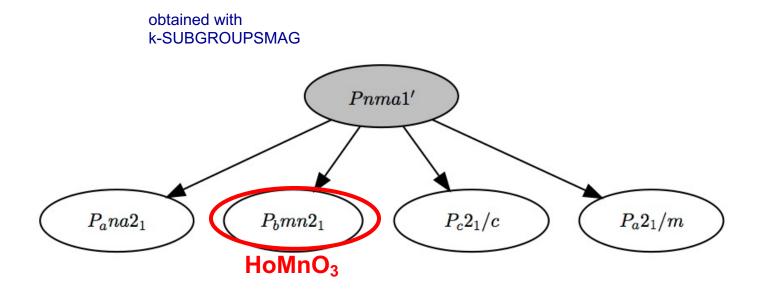


Symmetry operation {1 '|1/2,0,0} is present in any case (magnetic cell=  $(2\mathbf{a}_p,\mathbf{b}_p,\mathbf{c}_p)$ )

# Symmetry based modeling of magnetic structures

Possible magnetic symmetries for a magnetic phase with propagation vector (1/2,0,0) and parent space group Pnma

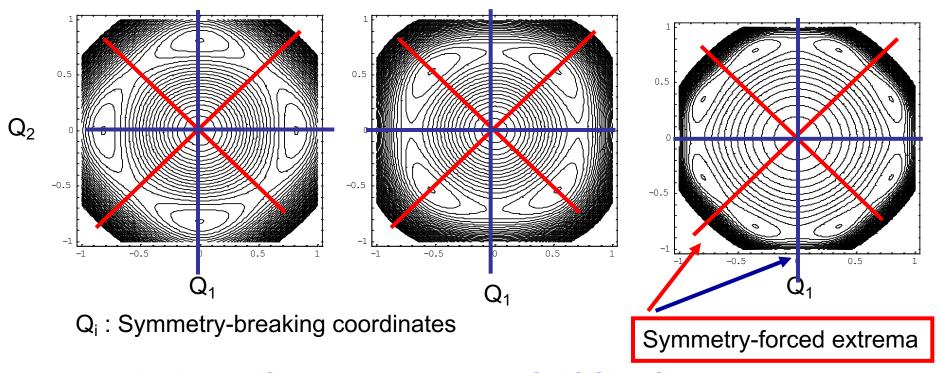
**ONLY MAXIMAL SUBGROUPS (k-maximal symmetries)** 



About 70% of all published magnetic structures have k-maximal symmetries

# Why the (magnetic) order parameter usually takes "special" directions of higher symmetry?

Domains/variants: symmetry related configurations (energy minima) around a higher-symmetry configuration



Energy in the configuration space is a SMOOTH function: Lower symmetry implies more equivalent minima, i.e. a more wavy energy function

# Construction of possible models of a magnetic structure of MAXIMAL SYMMETRY compatible with its propagation vector (1k): MAXMAGN

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	tic Symme			11197-14	
		The second second			

MGENPOS General Positions of Magnetic Space Groups

MWYCKPOS Wyckoff Positions of Magnetic Space Groups

MKVEC 
The k-vector types and Brillouin zones of Magnetic Space Groups

IDENTIFY MAGNETIC GROUP Identification of a Magnetic Space Group from a set of generators in an

arbitrary setting

BNS2OG Transformation of symmetry operations between BNS and OG settings

mCIF2PCR Transformation from mCIF to PCR format (FullProf).

MPOINT Magnetic Point Group Tables

MAGNEXT Extinction Rules of Magnetic Space Groups

MAXMAGN Maximal magnetic space groups for a given space group and a propagation

vector

MAGMODELIZE Magnetic structure models for any given magnetic symmetry

STRCONVERT Convert & Edit Structure Data

 $(supports\ the\ CIF,\ mCIF,\ VESTA,\ VASP\ formats\ --\ with\ magnetic\ information\ where\ available)$ 

k-SUBGROUPSMAG Magnetic subgroups consistent with some given propagation vector(s) or a

supercell

MAGNDATA A collection of magnetic structures with portable cif-type files

MVISUALIZE 3D Visualization of magnetic structures with Jmol

MTENSOR 

Symmetry-adapted form of crystal tensors in magnetic phases

MAGNETIC REP. Decomposition of the magnetic representation into irreps

Get mirreps and order parameters in a paramagnetic space group- magnetic

subgroup phase transition

3 Tutorials can be downloaded from the program webpage

#### **Magnetic Symmetry and Applications**

MGENPOS General Positions of Magnetic Space Groups

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MKVEC 

The k-vector types and Brillouin zones of Magnetic Space Groups

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MTENSOR (A) Symmetry-adapted form of crystal tensors in magnetic phases

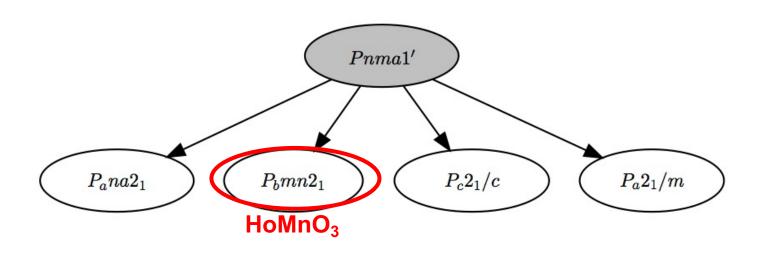
MAGNETIC REP. Decomposition of the magnetic representation into irreps

Get mirreps and order parameters in a paramagnetic space group- magnetic

subgroup phase transition

# Program MAXMAGN

N	Group (BNS)	Transformation matrix	General positions	Properties	Magnetic structure
1	P <sub>a</sub> na2 <sub>1</sub> (#33.149) Go to a subgroup	$\begin{pmatrix} 2 & 0 & 0 & 1/4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
2	P <sub>b</sub> mn2 <sub>1</sub> (#31.129) Go to a subgroup	$\begin{pmatrix} 0 & -2 & 0 & 1/4 \\ 1 & 0 & 0 & 1/4 \\ 0 & 0 & 1 & 0 \end{pmatrix}$ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
3	P <sub>c</sub> 2 <sub>1</sub> /c (#14.82) Go to a subgroup	$\begin{pmatrix} 0 & 0 & 2 & 1/2 \\ 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{pmatrix}$ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
4	P <sub>a</sub> 2 <sub>1</sub> /m (#11.55) Go to a subgroup	( 2 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show



# Unambiguous description of a MSG as subgroup of a parent gray group:

HoMnO<sub>3</sub> case

Group→subgroup	Tr	ansf	orma	ation	matrix
Pnma1' (N. 62.442)→P <sub>b</sub> mn2 <sub>1</sub> (N. 31.129)	(	0 -1 0	2 0 0	0 0 1	1/4 1/4 0

**Pnma1'**  $\rightarrow$  **P<sub>b</sub>mn2<sub>1</sub>** (-b, 2a, c; 1/4, 1/4, 0)

transformation to standard of the MSG

(P,p)

 $\mathbf{P} = 3x3 \text{ matrix}$  $p = (p_1, p_2, p_3)$ 

 $(a^{s},b^{s},c^{s})=(a_{p},b_{p},c_{p}).P$ ,  $O^{s}=O_{p}+p_{1} a_{p}+p_{2} b_{p}+p_{3} c_{p}$ 

MSG standard unit cell parent unit cell

origin shlft

# Transformation to standard setting:

symmetry operation: 
$$\begin{pmatrix} R^s & \mathbf{t}^s \\ \hline 0 & 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} \mathbf{p} & \mathbf{p} \\ \hline 0 & 0 & 0 & 1 \end{pmatrix}^{-1} \begin{pmatrix} R & \mathbf{t} \\ \hline 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \mathbf{p} & \mathbf{p} \\ \hline 0 & 0 & 0 & 1 \end{pmatrix}$$

positions:

$$\begin{pmatrix} x^s \\ y^s \\ z^s \\ 1 \end{pmatrix} = \begin{pmatrix} \mathbf{p} & \mathbf{p} \\ \hline 0 & 0 & 0 & 1 \end{pmatrix}^{-1} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} \qquad \begin{pmatrix} m_x^s/a^s \\ m_y^s/b^s \\ m_x^s/c^s \end{pmatrix} = \mathbf{P} \begin{pmatrix} m_x/a \\ m_y/b \\ m_x/c \end{pmatrix}$$

magnetic moment (absolute) components:

$$\left(egin{array}{c} m_x^s/a^s \ m_y^s/b^s \ m_z^s/c^s \end{array}
ight) = \mathbf{P}^{-1} \!\!\left(egin{array}{c} m_x/a \ m_y/b \ m_z/c \end{array}
ight)$$

### One should not confuse:

### When describing a subgroup of the parent group:

Parent Pnma unit cell ( $\mathbf{a}_p$ ,  $\mathbf{b}_p$ ,  $\mathbf{c}_p$ ;0,0,0):

**Pnma1'** 
$$\rightarrow$$
 **P**<sub>b</sub>**mn2**<sub>1</sub> (-b, 2a, c; 1/4, 1/4, 0)

transformation to standard from the parent setting of *Pnma* 

description of the subgroup by its type of MSG and a unit cell and origin with respect to the parent unit cell where it WOULD adquire its standard form

# When describing a magnetic structure under this MSG using a non-standard setting:

Unit cell used  $(2\mathbf{a}_p, \mathbf{b}_p, \mathbf{c}_p; 0,0,0)$ :

$$P_bmn2_1$$
 (-b, a, c; 1/8, 1/4, 0)

transformation to standard from the setting used for the MSG.

Alternative unit cell and origin with respect to the unit cell used where the MSG WOULD adquire its standard form

```
_parent_space_group.name_H_M_alt_ 'P n m a'
_parent_space_group.IT_number 62
_parent_space_group.transform_Pp_abc 'a,b,c;0,0,0'

loop_
_parent_propagation_vector.id
_parent_propagation_vector.kxkykz
k1 [1/2 0 0]
```

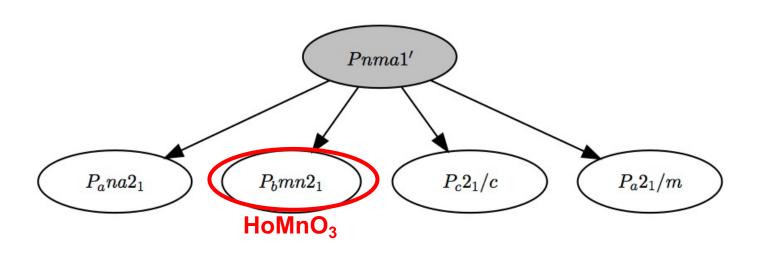
parent space group.child transform Pp abc '2a,b,c;0,0,0'
space group magn.transform BNS Pp abc 'b,-a,c;1/8,1/4,0'

```
space group magn.number BNS 31.129
                           "P_b m
space group magn.name BNS
                                    n 2 1"
_cell_length_a
                          11.67080
_cell_length_b
                          7.36060
_cell_length_c
                           5.25720
cell angle alpha
                           90.00
_cell_angle_beta
                          90.00
_cell_angle_gamma
                          90.00
```

```
loop
space group symop magn operation.id
space group symop magn operation.xyz
1 x, y, z, +1
2 -x+1/4,-y,z+1/2,+1
3 \times ,-y+1/2,z,+1
4 -x+1/4,y+1/2,z+1/2,+1
loop
space group symop magn centering id
space group symop magn centering xvz
1 x, y, z, +1
2 x+1/2, y, z, -1
loop_
_atom_site_label
_atom_site_type_symbol
atom site fract x
_atom_site_fract_y
atom site fract z
Ho 1 Ho 0.04195 0.25000 0.98250
Ho 2 Ho 0.95805 0.75000 0.01750
Mn Mn 0.00000 0.00000 0.50000
01 1 0 0.23110 0.25000 0.11130
01 2 0 0.76890 0.75000 0.88870
02 1 0 0.16405 0.05340 0.70130
02 2 0 0.83595 0.55340 0.29870
loop
_atom_site_moment.label
atom site moment.crystalaxis x
atom site moment.crystalaxis y
atom site moment.crystalaxis z
 atom site moment.symmform
Ho 1 0.00000 0.00000 0.00000 0.mv,0
Ho_2 0.00000 0.00000 0.00000 0,my,0
Mn 1.00000 0.00000 0.00000 mx,my,mz
```

# Program MAXMAGN

N	Group (BNS)	Transformation matrix	General positions	Properties	Magnetic structure
1	P <sub>a</sub> na2 <sub>1</sub> (#33.149) Go to a subgroup	$\begin{pmatrix} 2 & 0 & 0 & 1/4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
2	P <sub>b</sub> mn2 <sub>1</sub> (#31.129) Go to a subgroup	$\begin{pmatrix} 0 & -2 & 0 & 1/4 \\ 1 & 0 & 0 & 1/4 \\ 0 & 0 & 1 & 0 \end{pmatrix}$ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
3	P <sub>c</sub> 2 <sub>1</sub> /c (#14.82) Go to a subgroup	$\begin{pmatrix} 0 & 0 & 2 & 1/2 \\ 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{pmatrix}$ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
4	P <sub>a</sub> 2 <sub>1</sub> /m (#11.55) Go to a subgroup	( 2 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show



#### Selected magnetic space group: 3- P<sub>c</sub>2<sub>1</sub>/c (#14.82)

Setting parent-like (2a, b, c; 0, 0, 0)

Parent space group Pnma (No. 62)

Lattice parameters: a=11.67070, b=7.36060, c=5.25720, alpha=90.00, beta=90.00, gamma=90.00

[Go to setting standard (-c, b, 2a; 1/2, 0, 0)] [Go to an alternative setting]

Export data to MCIF file/Visualize Go to a subgroup

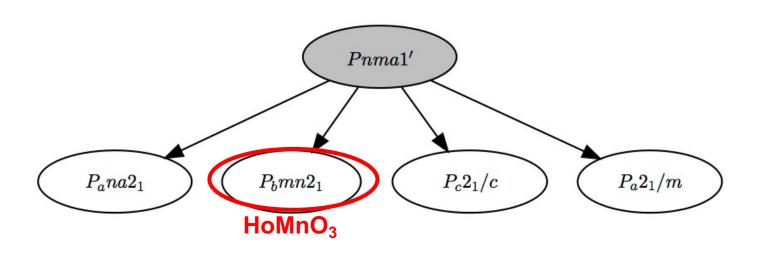
#### Atomic positions, Wyckoff positions and Magnetic Moments

N	Atom	New WP	Multiplicity	Magnetic moment	Values of M <sub>x</sub> , M <sub>y</sub> , M <sub>z</sub>
1	Ho1_1 Ho 0.04195 0.25000 0.98250	$ \begin{array}{c} (x,1/4,z\mid m_{x},0,m_{z})\;(-x,3/4,-z\mid -m_{x},0,-m_{z})\\ (x+1/2,1/4,z\mid -m_{x},0,-m_{z})\;(-x+1/2,3/4,-z\mid m_{x},0,m_{z}) \end{array} $	4	(M <sub>x</sub> ,0,M <sub>z</sub> )	$M_X = 0.00001$ $M_Z = 0.00001$
	Ho1_2 Ho 0.20805 0.75000 0.48250	$ \begin{array}{l} (-x+1/4,3/4,z+1/2\mid m_{X},0,m_{Z})\;(x+1/4,1/4,-z+1/2\mid m_{X},0,m_{Z})\\ (-x+3/4,3/4,z+1/2\mid -m_{X},0,-m_{Z})\;(x+3/4,1/4,-z+1/2\mid -m_{X},0,-m_{Z}) \end{array} $	4	(M <sub>x</sub> ,0,M <sub>z</sub> )	$M_X = 0.00001$ $M_Z = 0.00001$
	Mn1_1 Mn 0.00000 0.00000 0.50000	(0,0,1/2   0,0,0) (0,1/2,1/2   0,0,0) (1/2,0,1/2   0,0,0) (1/2,1/2,1/2   0,0,0)	4	(0,0,0)	
2	Mn1_2 Mn 0.25000 0.00000 0.00000	(1/4,0,0   m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (1/4,1/2,0   m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub> ) (3/4,0,0   -m <sub>x</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (3/4,1/2,0   -m <sub>x</sub> ,m <sub>y</sub> ,-m <sub>z</sub> )	4	(M <sub>x</sub> ,M <sub>y</sub> ,M <sub>z</sub> )	$M_x = 0.00001$ $M_y = 0.00001$ $M_z = 0.00001$
3	O1_1 O 0.23110 0.25000 0.11130	$ \begin{array}{c} (x,1/4,z\mid m_x,0,m_z) \; (-x,3/4,-z\mid -m_x,0,-m_z) \\ (x+1/2,1/4,z\mid -m_x,0,-m_z) \; (-x+1/2,3/4,-z\mid m_x,0,m_z) \end{array} $	4	-	-
3	O1_2 O 0.01890 0.75000 0.61130	$ \begin{array}{l} (-x+1/4,3/4,z+1/2\mid m_{X},0,m_{Z})\;(x+1/4,1/4,-z+1/2\mid m_{X},0,m_{Z})\\ (-x+3/4,3/4,z+1/2\mid -m_{X},0,-m_{Z})\;(x+3/4,1/4,-z+1/2\mid -m_{X},0,-m_{Z}) \end{array} $	4	-	-
4	O2_1 O 0.16405 0.05340 0.70130	$ \begin{array}{c} (x,y,z\mid m_x,m_y,m_z)\;(-x,y+1/2,-z\mid -m_x,m_y,-m_z)\\ (-x,-y,-z\mid -m_x,-m_y,-m_z)\;(x,-y+1/2,z\mid m_x,-m_y,m_z)\\ (x+1/2,y,z\mid -m_x,-m_y,-m_z)\;(-x+1/2,y+1/2,-z\mid m_x,-m_y,m_z)\\ (-x+1/2,-y,-z\mid m_x,m_y,m_z)\;(x+1/2,-y+1/2,z\mid -m_x,m_y,-m_z) \end{array}$	8	-	-
4	O2_2 O 0.08595 0.94660 0.20130	(-x+1/4,-y,z+1/2   m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (x+1/4,-y+1/2,-z+1/2   m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub> ) (x+1/4,y,-z+1/2   m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (-x+1/4,y+1/2,z+1/2   m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub> ) (-x+3/4,-y,z+1/2   -m <sub>x</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (x+3/4,-y+1/2,-z+1/2   -m <sub>x</sub> ,m <sub>y</sub> ,-m <sub>z</sub> ) (x+3/4,y,-z+1/2   -m <sub>x</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> )	8	-	-

half of the Mn atoms must have zero spins

# Program MAXMAGN

N	Group (BNS)	Transformation matrix	General positions	Properties	Magnetic structure
1	P <sub>a</sub> na2 <sub>1</sub> (#33.149) Go to a subgroup	$\begin{pmatrix} 2 & 0 & 0 & 1/4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
2	P <sub>b</sub> mn2 <sub>1</sub> (#31.129) Go to a subgroup	$\begin{pmatrix} 0 & -2 & 0 & 1/4 \\ 1 & 0 & 0 & 1/4 \\ 0 & 0 & 1 & 0 \end{pmatrix}$ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
3	P <sub>c</sub> 2 <sub>1</sub> /c (#14.82) Go to a subgroup	$\begin{pmatrix} 0 & 0 & 2 & 1/2 \\ 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{pmatrix}$ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
4	P <sub>a</sub> 2 <sub>1</sub> /m (#11.55) Go to a subgroup	( 2 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show



#### Selected magnetic space group: 2- P<sub>b</sub>mn2<sub>1</sub> (#31.129)

Setting parent-like (2a, b, c; 0, 0, 0)

Parent space group Pnma (No. 62)

Lattice parameters: a=11.67070, b=7.36060, c=5.25720, alpha=90.00, beta=90.00, gamma=90.00

[Go to setting standard (b, -2a, c; 1/4, 1/4, 0)] [Go to an alternative setting]

Export data to MCIF file/Visualize Go to a subgroup

#### Atomic positions, Wyckoff positions and Magnetic Moments

N	Atom	New WP	Multiplicity	Magnetic moment	Values of M <sub>x</sub> , M <sub>y</sub> , M <sub>z</sub>
	Ho1_1 Ho 0.04195 0.25000 0.98250	(x,1/4,z   0,m <sub>y</sub> ,0) (-x+1/4,3/4,z+1/2   0,-m <sub>y</sub> ,0) (x+1/2,1/4,z   0,-m <sub>y</sub> ,0) (-x+3/4,3/4,z+1/2   0,m <sub>y</sub> ,0)	4	(0,M <sub>y</sub> ,0)	M <sub>y</sub> = 0.00001
	Ho1_2 Ho 0.95805 0.75000 0.01750	(-x,3/4,-z   0,m <sub>y</sub> ,0) (x+1/4,1/4,-z+1/2   0,-m <sub>y</sub> ,0) (-x+1/2,3/4,-z   0,-m <sub>y</sub> ,0) (x+3/4,1/4,-z+1/2   0,m <sub>y</sub> ,0)	4	(0,M <sub>y</sub> ,0)	M <sub>y</sub> = 0.00001
2	Mn1 Mn 0.00000 0.00000 0.50000	(0,0,1/2   m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (1/4,0,0   -m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub> ) (0,1/2,1/2   -m <sub>x</sub> ,m <sub>y</sub> ,-m <sub>z</sub> ) (1/4,1/2,0   m <sub>x</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (1/2,0,1/2   -m <sub>x</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (3/4,0,0   m <sub>x</sub> ,m <sub>y</sub> ,-m <sub>z</sub> ) (1/2,1/2,1/2   m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub> ) (3/4,1/2,0   -m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub> )	8	(M <sub>x</sub> ,M <sub>y</sub> ,M <sub>z</sub> )	$M_X = 1$ $M_y = 0.00001$ $M_z = 0.00001$
	O1_1 O 0.23110 0.25000 0.11130	(x,1/4,z   0,m <sub>y</sub> ,0) (-x+1/4,3/4,z+1/2   0,-m <sub>y</sub> ,0) (x+1/2,1/4,z   0,-m <sub>y</sub> ,0) (-x+3/4,3/4,z+1/2   0,m <sub>y</sub> ,0)	4	-	-
3	O1_2 O 0.76890 0.75000 0.88870	(-x,3/4,-z   0,m <sub>y</sub> ,0) (x+1/4,1/4,-z+1/2   0,-m <sub>y</sub> ,0) (-x+1/2,3/4,-z   0,-m <sub>y</sub> ,0) (x+3/4,1/4,-z+1/2   0,m <sub>y</sub> ,0)	4	-	-
	O2_1 O 0.16405 0.05340 0.70130	(x,y,z   m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (-x+1/4,-y,z+1/2   -m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub> ) (x,-y+1/2,z   -m <sub>x</sub> ,m <sub>y</sub> ,-m <sub>z</sub> ) (-x+1/4,y+1/2,z+1/2   m <sub>x</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (x+1/2,y,z   -m <sub>x</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (-x+3/4,-y,z+1/2   m <sub>x</sub> ,m <sub>y</sub> ,-m <sub>z</sub> ) (x+1/2,-y+1/2,z   m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub> ) (-x+3/4,y+1/2,z+1/2   -m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub> )	8	-	-
4	O2_2 O 0.83595 0.55340 0.29870	(-x,y+1/2,-z   m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (x+1/4,-y+1/2,-z+1/2   -m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub> ) (-x,-y,-z   -m <sub>x</sub> ,m <sub>y</sub> ,-m <sub>z</sub> ) (x+1/4,y,-z+1/2   m <sub>x</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (-x+1/2,y+1/2,-z   -m <sub>x</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (x+3/4,-y+1/2,-z+1/2   m <sub>x</sub> ,m <sub>y</sub> ,-m <sub>z</sub> ) (-x+1/2,-y,-z   m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub> ) (x+3/4,y,-z+1/2   -m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub> )	8	-	-

#### mCIF file of the structure



#### Download mCIF file: bcs\_file.mcif

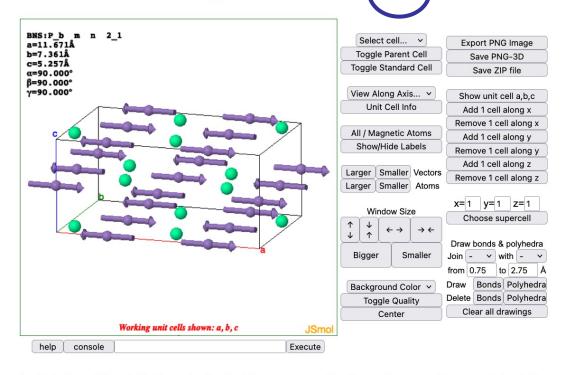
[The preview text below is non-editable, only copy-allowed]

```
#\#CIF_2.0
# Created by the Bilbao Crystallographic Server
# http://www.cryst.ehu.es
# Date: 26/10/2025 17:42:49
# HoMn03_Munoz_icsd_165196.cif
data_5y0htAoR
_audit_creation_date
                                2025-10-26
                                "Bilbao Crystallographic Server"
_audit_creation_method
_citation_journal_abbrev
                                ?
_citation_journal_volume
                                ?
                                ?
_citation_page_first
_citation_page_last
                                ?
_citation_article_id
_citation_year
                                ?
_citation_DOI
                                ?
loop_
_citation_author_name
_atomic_positions_source_database_code_ICSD ?
_atomic_positions_source_other
_transition_temperature ?
_experiment_temperature ?
loop_
_irrep_id
_irrep_dimension
_irrep_small_dimension
_irrep_direction_type
_irrep_action
_irrep_modes_number
_irrep_presence
? ? ? ? ? ? ?
_exptl_crystal_magnetic_properties_details
_active_magnetic_irreps_details
k-maximal magnetic symmetry
_parent_space_group.name_H-M_alt 'P n m a'
```

#### MVISUALIZE: 3D Visualization of magnetic structures with Jmol

#### **MVISUALIZE Main Page**

Show/Hide File



Note: If the application stops working right or any malfunction is observed, it is probably a temporal problem due to the cache memory of your browser. Clear your web browser cache to solve it.

If you still observe any malfunction, write an e-mail to cryst@wm.lc.ehu.es explaining the problem in detail.

#### Maximal magnetic space groups for the space group 64 (Cmce) and the propagation vector k = (1, 0, 0)

Group (BNS)	Transformation matrix	General positions	Systematic absences	Magnetic structure
P <sub>C</sub> nma (#62.455)	0 1 0 1/4 -1 0 0 1/4 0 0 1 0 Alternatives (twin-related)	Show	Show	Show
Pobca (#61.439)	1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	Show	Show	Show
P <sub>A</sub> bcn (#60.429)	0 1 0 1/4 0 0 1 1/4 1 0 0 0 0	Show	Show	Show
P <sub>B</sub> bcm (#57.390)	0 0 1 1/4 1 0 0 1/4 0 1 0 0 Alternatives (twin-related)	Show	Show	Show
P <sub>A</sub> ccn (#56.374)	0 1 0 0 0 0 1 0 0 1 0 0 1 0 0 0 0 0 0 0	Show	Show	Show
P <sub>A</sub> bam (#55.362)	0 0 1 0 0 0 1 0 1 0 0 1 0 0 1 0 0 0 0 0	Show	Show	Show
Рдсса (#54.349)	0 1 0 1/4 0 0 1 1/4 1 0 0 0 0	Show	Show	Show
Pcmna (#53.335)	1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 1 0	Show	Show	Show

La<sub>2</sub>CuO<sub>4</sub>

Parent symmetry group:

Cmce (Cmca.1')Cu at WP 4a

propagation vector: k=(1,0,0)

(it is NOT equivalent to k=0!)

**MAXMAGN:** 

Possible alternative maximal magnetic symmetries and corresponding models of the magnetic structure

#### Selected magnetic space group: 5- $P_A$ ccn (#56.374)

#### Setting of the parent group

Lattice parameters: a=5.35700, b=13.14800, c=5.40600, alpha=90., beta=90., gamma=90.

#### Magnetic Moments associated to magnetic atoms

N	Atom	New WP	Multiplicity	Magnetic moment	Values of M <sub>x</sub> , M <sub>y</sub> , M <sub>z</sub>
1	Cu1 Cu 0.00000 0.00000 0.00000	(0,0,0   0,m <sub>y</sub> ,m <sub>z</sub> ) (0,1/2,1/2   0,-m <sub>y</sub> ,m <sub>z</sub> ) (1/2,1/2,0   0,-m <sub>y</sub> ,-m <sub>z</sub> ) (1/2,0,1/2   0,m <sub>y</sub> ,-m <sub>z</sub> )	4	(0,M <sub>y</sub> ,M <sub>z</sub> )	$M_y = 0.00001$ $M_z = 0.00001$
2	La1 La 0.00000 0.36110 0.00460	$ \begin{array}{c} (0,y,z \mid 0,m_{y},m_{z}) \; (0,-y+1/2,1/2 \mid 0,-m_{y},m_{z}) \\ (0,1/2,-z+1/2 \mid 0,-m_{y},m_{z}) \; (0,-y,-z \mid 0,m_{y},m_{z}) \\ (1/2,1/2,0 \mid 0,-m_{y},-m_{z}) \; (1/2,-y,1/2 \mid 0,m_{y},-m_{z}) \\ (1/2,0,-z+1/2 \mid 0,m_{y},-m_{z}) \; (1/2,-y+1/2,-z \mid 0,-m_{y},-m_{z}) \end{array} $	8	-	-
3	O1 O 0.25000 -0.00510 0.25000	(1/4,y,1/4   0,m <sub>y</sub> ,0) (3/4,-y+1/2,3/4   0,-m <sub>y</sub> ,0) (3/4,-y,3/4   0,m <sub>y</sub> ,0) (1/4,1/2,1/4   0,-m <sub>y</sub> ,0) (3/4,1/2,1/4   0,-m <sub>y</sub> ,0) (1/4,-y,3/4   0,m <sub>y</sub> ,0) (1/4,-y+1/2,3/4   0,-m <sub>y</sub> ,0) (3/4,0,1/4   0,m <sub>y</sub> ,0)	8	-	-
4	O2 O 0.00000 0.18300 -0.02430	$ \begin{array}{c} (0,y,z \mid 0,m_{y},m_{z}) \; (0,-y+1/2,1/2 \mid 0,-m_{y},m_{z}) \\ (0,1/2,-z+1/2 \mid 0,-m_{y},m_{z}) \; (0,-y,-z \mid 0,m_{y},m_{z}) \\ (1/2,1/2,0 \mid 0,-m_{y},-m_{z}) \; (1/2,-y,1/2 \mid 0,m_{y},-m_{z}) \\ (1/2,0,-z+1/2 \mid 0,m_{y},-m_{z}) \; (1/2,-y+1/2,-z \mid 0,-m_{y},-m_{z}) \end{array} $	8	-	-

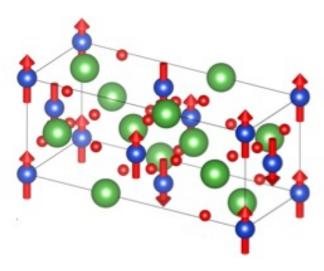
[Go to setting standard (c, a, b; 0, 0, 0)]

Export data to MCIF file Go to a subgroup

#### Maximal magnetic space groups for the space group 64 (Cmce) and the propagation vector k = (1, 0, 0)

Group (BNS)	Transformation matrix	General positions	Systematic absences	Magnetic structure
P <sub>C</sub> nma (#62.455)	0 1 0 1/4 -1 0 0 1/4 0 0 1 0 Alternatives (twin-related)	Show	Show	Show
Pobca (#61.439)	1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	Show	Show	Show
P <sub>A</sub> bcn (#60.429)	0 1 0 1/4 0 0 1 1/4 1 0 0 0 0	Show	Show	Show
P <sub>B</sub> bcm (#57.390)	0 0 1 1/4 1 0 0 1/4 0 1 0 0 0 Alternatives (twin-related)	Show	Show	Show
P <sub>A</sub> ccn (#56.374)	0 1 0 0 0 0 0 1 0 0 1 0 0 0 0 0 0 0 0 0	Show	Show	Show
P <sub>A</sub> bam (#55.362)	0 0 1 0 0 0 1 0 1 0 0 1 0 0 0 0 0 0 0 0	Show	Show	Show
Р <sub>А</sub> сса (#54.349)	0 1 0 1/4 0 0 1 1/4 1 0 0 0 0	Show	Show	Show
P <sub>C</sub> mna (#53.335)	1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0	Show	Show	Show

# La<sub>2</sub>CuO<sub>4</sub>



P<sub>A</sub>ccn (56.374)

Cu1 (0,0,0)

$$M_{Cu1} = (0, my, m_z)$$

Refinement result (Magndata #1.23):

$$M_{Cu1} = (0, 0, 0.17)$$

# Construction of possible models of a magnetic structure from the knowledge of its propagation vector(s):

#### **k-SUBGROUPSMAG & MAGMODELIZE**

M	agnetic Symmetry and Applications
MGENPOS	General Positions of Magnetic Space Groups
MWYCKPOS	Wyckoff Positions of Magnetic Space Groups
MKVEC A	The k-vector types and Brillouin zones of Magnetic Space Groups
IDENTIFY MAGNETIC GROUP	Identification of a Magnetic Space Group from a set of generators in an arbitrary setting
BNS2OG	Transformation of symmetry operations between BNS and OG settings
mCIF2PCR	Transformation from mCIF to PCR format (FullProf).
MPOINT	Magnetic Point Group Tables
MAGNEXT	Extinction Rules of Magnetic Space Groups
MAXMAGN	Maximal magnetic space groups for a given space group and a propagation vector
MAGMODELIZE	Magnetic structure models for any given magnetic symmetry
STRCONVERT	Convert & Edit Structure Data (supports the CIF, mCIF, VESTA, VASP formats with magnetic information where available)
k-SUBGROUPSMAG	Magnetic subgroups consistent with some given propagation vector(s) or a supercell
MAGNDATA	A collection of magnetic structures with portable cif-type files
MVISUALIZE	3D Visualization of magnetic structures with Jmol
MTENSOR 🗘	Symmetry-adapted form of crystal tensors in magnetic phases
MAGNETIC REP.	Decomposition of the magnetic representation into irreps
Get_mirreps	Irreps and order parameters in a paramagnetic space group- magnetic subgroup phase transition

For non-maximal symmetries and/or more than one propagation vector

#### **k-SUBGROUPSMAG & MAGMODELIZE**

**Magnetic Symmetry and Applications MGENPOS** General Positions of Magnetic Space Groups **MWYCKPOS** Wyckoff Positions of Magnetic Space Groups MKVEC A The k-vector types and Brillouin zones of Magnetic Space Groups Identification of a Magnetic Space Group from a set of generators in an **IDENTIFY MAGNETIC GROUP** arbitrary setting **BNS2OG** Transformation of symmetry operations between BNS and OG settings Tutorial\_magnetic\_sect Transformation from mCIF to PCR format (FullProf). mCIF2PCR ion BCS 3 **MPOINT** Magnetic Point Group Tables **MAGNEXT** Extinction Rules of Magnetic Space Groups Maximal magnetic space groups for a given space group and a propagation **MAXMAGN MAGMODELIZE** Magnetic structure models for any given magnetic symmetry Convert & Edit Structure Data **Tutorial magnetic sect STRCONVERT** (supports the CIF, mCIF, VESTA, VASP formats -- with magnetic information where available) ion\_BCS\_2 Magnetic subgroups consistent with some given propagation vector(s) or a -SUBGROUPSMAG supercell MAGNDATA A collection of magnetic structures with portable cif-type files **MVISUALIZE** 3D Visualization of magnetic structures with Jmol MTENSOR A Symmetry-adapted form of crystal tensors in magnetic phases **MAGNETIC REP.** Decomposition of the magnetic representation into irreps Tutorial-k-SUBGROUPSMAG Irreps and order parameters in a paramagnetic space group- magnetic Get mirreps (3 versions) subgroup phase transition

### **k-SUBGROUPSMAG & MAGMODELIZE**

k-Subgroupsmag: Magnetic subgroups compatible with some given propagation vector(s) or a supercell.

### Enter the serial number of the space group of the parent choose it paramagnetic phase: Choose an alternative magnetic group Introduce the magnetic wave vector(s) Alternatively give the basis vectors of the supercell (Give the components of the wave vectors in a fractional form, n/m) $k_{1y}$ $k_{1z}$ $k_{1x}$ Show the independent vectors of the star Choose the whole star of the propagation vector More wave-vectors needed Optionally give also non-magnetic modulation wave-vectors Include the subgroups compatible with intermediate cells. (It is not applied when only the maximal subgroups are calculated) Optional: refine further the subgroups of the output giving the Wyckoff positions of the atoms Give the Wyckoff positions Wyckoff Optional: Show only subgroups that can be the result of a Landau-type transition (single irrep order parameter).

#### k-SUBGROUPSMAG is

called by the refinement program **GSAS-II** through an internal link in order to obtain all possible alternative symmetries for a given set of propagation vectors.

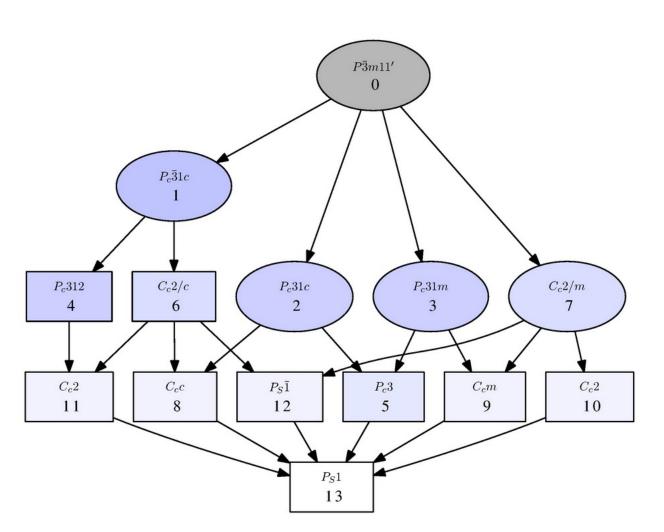
# Example: Ba3Nb2NiO9 MAGNDATA #1.13

Possible magnetic symmetries for a magnetic phase with parent space group P-3m1 (N. 164), propagation vector (1/3,1/3,1/2) and magnetic atom at 1b (0,0,1/2) allowing zon-zero momento on all sites

N	Group Symbol	Trans	forma	ation	matrix	Group-Subgroup index	Other members of the Conjugacy Class	irreps	Magnetic structure models (MAGMODELIZE)
1	$P_c \overline{3}1c$ (No. 163.84)	$\begin{pmatrix} & 1 \\ & -1 \\ & 0 \end{pmatrix}$	1 2 0	0 0 2	1/2	6=6x1	Conjugacy Class	Get irreps	
2	P <sub>c</sub> 31c (No. 159.64)	$\begin{pmatrix} & 1 \\ -1 \\ 0 \end{pmatrix}$	1 2 0	0 0 2	-2/3 -1/3 0	12=6x2	Conjugacy Class	Get irreps	
3	P <sub>c</sub> 31 <i>m</i> (No. 157.56)	$\begin{pmatrix} & 1 \\ -1 \\ 0 \end{pmatrix}$	1 2 0	0 0 2	-2/3 -1/3 0	12=6x2	Conjugacy Class	Get irreps	
4	P <sub>c</sub> 312 (No. 149.24)	$\begin{pmatrix} & 1 \\ & -1 \\ & 0 \end{pmatrix}$	1 2 0	0 0 2	0 0	12=6x2	Conjugacy Class	Get irreps	
5	P <sub>c</sub> 3 (No. 143.3)	$\begin{pmatrix} & 2\\ & 1\\ & 0 \end{pmatrix}$	-1 1 0	0 0 2	1/3 -1/3 0	24=6x4	Conjugacy Class	Get irreps	
6	C <sub>c</sub> 2/c (No. 15.90)	$\begin{pmatrix} & 2\\ & 1\\ & 0 \end{pmatrix}$	0 3 0	0 0 2	$\begin{pmatrix} 0 \\ -1/2 \\ 1/2 \end{pmatrix}$	18=6x3	Conjugacy Class	Get irreps	
7	C <sub>c</sub> 2/m (No. 12.63)	$\begin{pmatrix} & 2\\ & 1\\ & 0 \end{pmatrix}$	0 3 0	0 0 2	$\begin{pmatrix} 0 \\ -1/2 \\ 1/2 \end{pmatrix}$	18=6x3	Conjugacy Class	Get irreps	
8	C <sub>c</sub> c (No. 9.40)	$\begin{pmatrix} 2\\1\\0 \end{pmatrix}$	0 3 0	0 0 2	1/5 -2/5 n	36=6x6	Conjugacy Class	Get irreps	

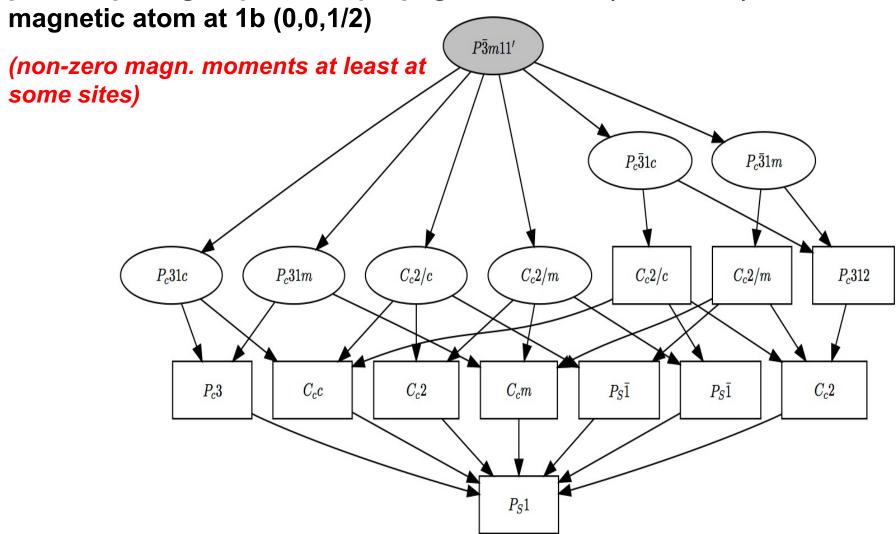
## **k-SUBGROUPSMAG** (Example Ba<sub>3</sub>Nb<sub>2</sub>NiO<sub>9</sub> Ni at WP 1b)

Possible magnetic symmetries for a magnetic phase with parent space group P-3m1, propagation vector (1/3,1/3,1/2) and magnetic atom at 1b (0,0,1/2) (non-zero magn. moments at all sites!)



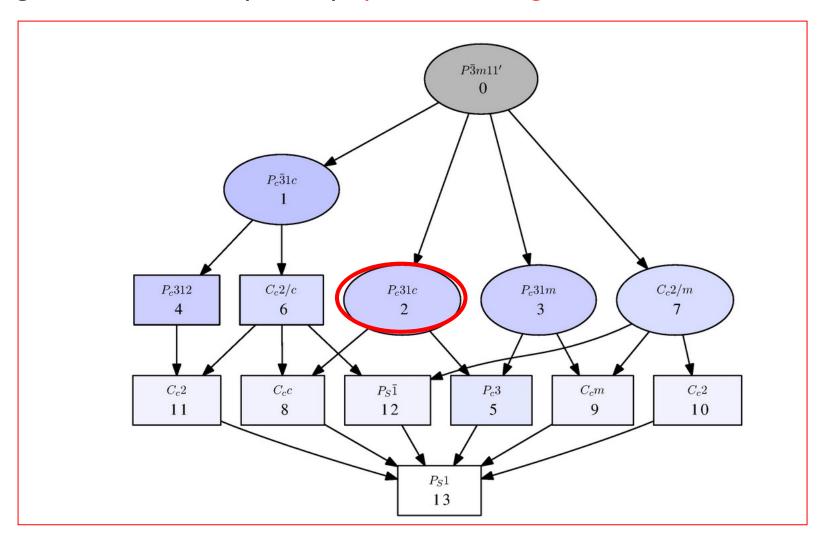
# **k-SUBGROUPSMAG** (Example Ba<sub>3</sub>Nb<sub>2</sub>NiO<sub>9</sub> Ni at WP 1b)

Possible magnetic symmetries for a magnetic phase with parent space group P-3m1, propagation vector (1/3,1/3,1/2) and



## **k-SUBGROUPSMAG** (Example Ba<sub>3</sub>Nb<sub>2</sub>NiO<sub>9</sub> Ni at WP 1b)

Possible magnetic symmetries for a magnetic phase with parent space group P-3m1, propagation vector (1/3,1/3,1/2) and magnetic atom at 1b (0,0,1/2) (non-zero magn. moments at all sites!)



# Example: Ba3Nb2NiO9 MAGNDATA #1.13

Possible MAXIMAL magnetic symmetries for a magnetic phase with parent space group P-3m1, propagation vector (1/3,1/3,1/2) and magnetic atom at 1b (0,0,1/2) allowing zon-zero moments on all 1b sites

N	Group (BNS)	Transformation matrix	General positions	Properties	Magnetic structure
1	P <sub>c</sub> -31c (#163.84) Go to a subgroup	$ \begin{pmatrix} 2 & -1 & 0 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 0 & 2 & 1/2 \end{pmatrix} $ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
2	P <sub>c</sub> 31c (#159.64) Go to a subgroup	2 -1 0 7/3 1 1 0 8/3 0 0 2 0 Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
3	P <sub>c</sub> 31m (#157.56) Go to a subgroup	2 -1 0 7/3 1 1 0 8/3 0 0 2 0 Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show
4	<i>C<sub>c</sub>2/m</i> (#12.63) Go to a subgroup	2 0 0 0 0 1 3 0 5/2 0 0 0 2 1/2 Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show

mCIFs of the transformed structure in the selected subgroups ('ksubgroupsmag\_mCIFs\_1473394.zip')

### k-SUBGROUPSMAG

### Example: Ba3Nb2NiO9 **MAGNDATA #1.13**

Selected magnetic space group: 2- P<sub>c</sub>31c (#159.64)

Setting parent-like (3a, 3b, 2c, 0, 0, 0)

Parent space group *P*-3*m*1 (No. 164)

Lattice parameters: a=17.26500, b=17.26500, c=14.13120, alpha=90.00, beta=90.00, gamma=120.00

[Go to setting standard (2a+b, -a+b, 2c; 7/3, 8/3, 0)] [Go to an alternative setting]

Export data to MCIF file/Visualize Go to a subgroup

#### **Atomic positions, Wyckoff positions and Magnetic Moments**

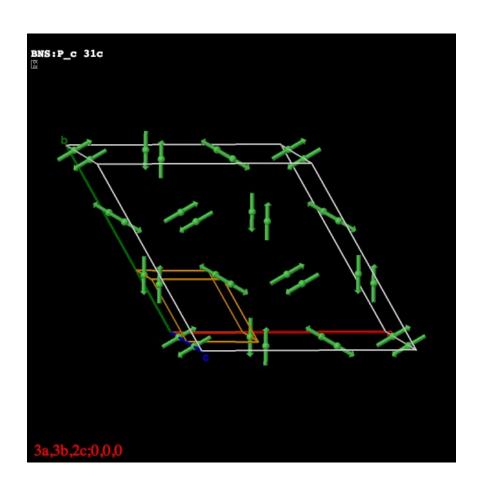
2	Ba2 Ba 0.00000 0.00000 0.00000	$ \begin{array}{c} (0,0,0 \mid 2m_{y},m_{y},m_{z}) \; (0,0,1/2 \mid -2m_{y},-m_{y},-m_{z}) \\ (0,1/3,0 \mid -m_{y},-2m_{y},m_{z}) \; (0,1/3,1/2 \mid m_{y},2m_{y},-m_{z}) \\ (0,2/3,0 \mid -m_{y},m_{z}) \; (0,2/3,1/2 \mid m_{y},-m_{y},-m_{z}) \\ (1/3,0,0 \mid -m_{y},-2m_{y},m_{z}) \; (1/3,0,1/2 \mid m_{y},2m_{y},-m_{z}) \\ (1/3,1/3,0 \mid -m_{y},m_{y},m_{z}) \; (1/3,1/3,1/2 \mid m_{y},-m_{y},-m_{z}) \\ (1/3,2/3,0 \mid 2m_{y},m_{y},m_{z}) \; (1/3,2/3,1/2 \mid -2m_{y},-m_{y},-m_{z}) \\ (2/3,0,0 \mid -m_{y},m_{y},m_{z}) \; (2/3,0,1/2 \mid m_{y},-m_{y},-m_{z}) \\ (2/3,1/3,0 \mid 2m_{y},m_{y},m_{z}) \; (2/3,1/3,1/2 \mid -2m_{y},-m_{y},-m_{z}) \end{array} $	18	-	-
3	Ni1 Ni 0.00000 0.00000 0.25000	(2/3,2/3,0   -m <sub>y</sub> ,-2m <sub>y</sub> ,m <sub>z</sub> ) (2/3,2/3,1/2   m <sub>y</sub> ,2m <sub>y</sub> ,-m <sub>z</sub> ) (0,0,1/4   2m <sub>y</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (0,0,3/4   -2m <sub>y</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (0,1/3,1/4   -m <sub>y</sub> ,-2m <sub>y</sub> ,m <sub>z</sub> ) (0,1/3,3/4   m <sub>y</sub> ,2m <sub>y</sub> ,-m <sub>z</sub> ) (0,2/3,1/4   -m <sub>y</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (0,2/3,3/4   m <sub>y</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (1/3,0,1/4   -m <sub>y</sub> ,-2m <sub>y</sub> ,m <sub>z</sub> ) (1/3,0,3/4   m <sub>y</sub> ,2m <sub>y</sub> ,-m <sub>z</sub> ) (1/3,1/3,1/4   -m <sub>y</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (1/3,1/3,3/4   m <sub>y</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (1/3,2/3,1/4   2m <sub>y</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (1/3,2/3,3/4   -2m <sub>y</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (2/3,0,1/4   -m <sub>y</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (2/3,0,3/4   m <sub>y</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (2/3,1/3,1/4   2m <sub>y</sub> ,m <sub>y</sub> ,m <sub>z</sub> ) (2/3,1/3,3/4   -2m <sub>y</sub> ,-m <sub>y</sub> ,-m <sub>z</sub> ) (2/3,2/3,1/4   -m <sub>y</sub> ,-2m <sub>y</sub> ,m <sub>z</sub> ) (2/3,2/3,3/4   m <sub>y</sub> ,2m <sub>y</sub> ,-m <sub>z</sub> )	18	(2M <sub>y</sub> ,M <sub>y</sub> ,M <sub>z</sub> )	M <sub>y</sub> = 0.00000 M <sub>z</sub> = 0.00000

### k-SUBGROUPSMAG

# Example: Ba3Nb2NiO9 Parent space group P-3m1

**MAGNDATA #1.13** 

k= (1/3,1/3,1/2) site:1b(001/2)



Generates an mCIF with all the information to be used in your refinement program:

it contains for instance:

```
loop
_space_group_symop_magn_operation.id
_space_group_symop_magn_operation.xyz
1 x, y, z, +1
2 -y+2/3, x-y, z, +1
3 - x + y + 2/3, -x + 2/3, z + 1
4 -y+2/3,-x+2/3,z+1/2,+1
5 x,x-y,z+1/2,+1
6 -x+y+2/3, y, z+1/2, +1
loop_
_space_group_symop_magn_centering.id
_space_group_symop_magn_centering.xyz
1 x, y, z, +1
2 x+1/3,y+2/3,z,+1
3 \times +2/3, y+1/3, z, +1
4 \times y,z+1/2,-1
5 x+1/3,y+2/3,z+1/2,-1
6 x+2/3, y+1/3, z+1/2, -1
```

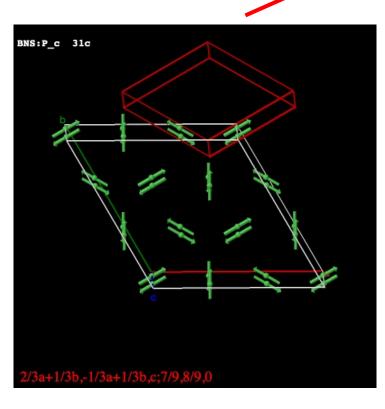
\_parent\_space\_group.child\_transform\_Pp\_abc '3a,3b,2c;0,0,0' \_space\_group\_magn.transform\_BNS\_Pp\_abc '2/3a+1/3b,-1/3a+1/3b,c;7/9,8/9,0'

### k-SUBGROUPSMAG

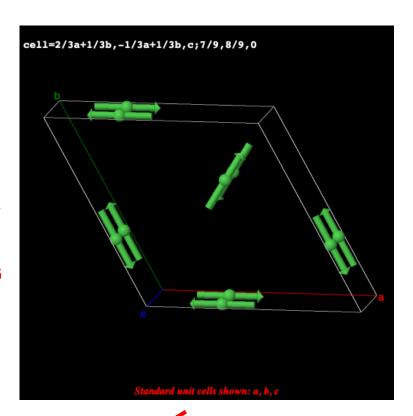
# Example: Ba3Nb2NiO9 MAGNDATA #1.13

 $MSG: P_c31c$ 

```
_parent_space_group.child_transform_Pp_abc '3a,3b,2c;0,0,0'
_space_group_magn.transform_BNS_Pp_abc '2/3a+1/3b,-1/3a+1/3b,c;7/9,8/9,0'
```



transformation to standard setting of MSG



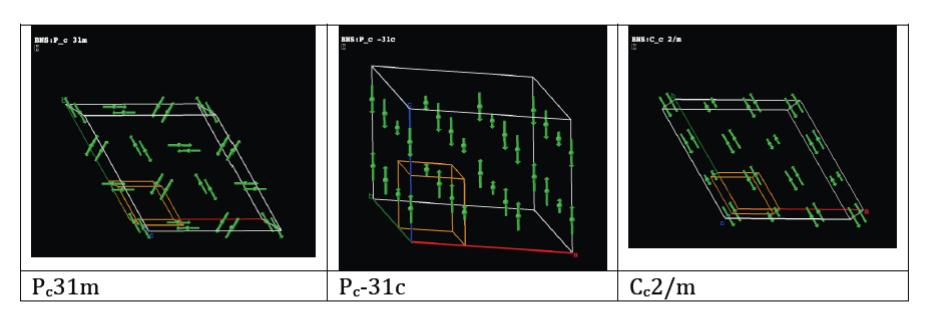
in the new mCIF file with the MSG in standard setting:

\_parent\_space\_group.child\_transform\_Pp\_abc '2a+b,-a+b,2c;7/3,8/3,0' \_space\_group\_magn.transform\_BNS\_Pp\_abc 'a,b,c;0,0,0'

### **k-SUBGROUPSMAG & MAGMODELIZE**

Models for each possible MSG can be constructed and magCIF files can be downloaded to use in other programs (refinement, visualization, etc.)

Some of the possible magnetic structures for parent space group P-3m1 propagation vector (1/3,1/3,1/2) and magnetic atom at 1b (0,0,1/2):



(obtained with MVISUALIZE (Jmol)

# Example: Ba3Nb2NiO9 MAGNDATA #1.13

Possible MAXIMAL magnetic symmetries for a magnetic phase with parent space group P-3m1, propagation vector (1/3,1/3,1/2) and magnetic atom at 1b (0,0,1/2) allowing zon-zero momento on all 1b sites

N	Group (BNS)	Transformation matrix	General positions	Properties	Magnetic structure	
1	<i>P<sub>c</sub>-31c</i> (#163.84)  Go to a subgroup	$ \begin{pmatrix} 2 & -1 & 0 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 0 & 2 & 1/2 \end{pmatrix} $ Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show	
2	<i>P<sub>c</sub>31c</i> (#159.64)  Go to a subgroup	2 -1 0 7/3 1 1 0 8/3 0 0 2 0 Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show	
3	<i>P<sub>c</sub>31m</i> (#157.56)  Go to a subgroup	2 -1 0 7/3 1 1 0 8/3 0 0 2 0 Alternatives (domain-related)	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show	
4	<i>C<sub>c</sub>2/m</i> (#12.63)  Go to a subgroup	\( \begin{pmatrix} 2 & 0 & 0 & 0 \\ 1 & 3 & 0 & 5/2 \\ 0 & 0 & 2 & 1/2 \end{pmatrix} \) \( \text{Alternatives (domain-related)} \end{pmatrix}	Show	Systematic absences  MAGNEXT  Tensor properties  MTENSOR	Show	

mCIFs of the transformed structure in the selected subgroups ('ksubgroupsmag\_mCIFs\_1473394.zip')

### **MAGNEXT:** Magnetic diffraction systematic absences

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	lugilotio o		y dilu A	193	IIIOutilo	110

MGENPOS General Positions of Magnetic Space Groups

MWYCKPOS Wyckoff Positions of Magnetic Space Groups

MKVEC 
The k-vector types and Brillouin zones of Magnetic Space Groups

IDENTIFY MAGNETIC GROUP Identification of a Magnetic Space Group from a set of generators in an

arbitrary setting

BNS2OG Transformation of symmetry operations between BNS and OG settings

mCIF2PCR Transformation from mCIF to PCR format (FullProf).

MPOINT Magnetic Point Group Tables

MAGNEXT Extinction Rules of Magnetic Space Groups

MAXMAGN Maximal magnetic space groups for a given space group and a propagation

vector

MAGMODELIZE Magnetic structure models for any given magnetic symmetry

STRCONVERT Convert & Edit Structure Data

(supports the CIF, mCIF, VESTA, VASP formats -- with magnetic information where available)

k-SUBGROUPSMAG

Magnetic subgroups consistent with some given propagation vector(s) or a

supercell

MAGNDATA A collection of magnetic structures with portable cif-type files

MVISUALIZE 3D Visualization of magnetic structures with Jmol

MTENSOR 

Symmetry-adapted form of crystal tensors in magnetic phases

MAGNETIC REP. Decomposition of the magnetic representation into irreps

Get mirreps Irreps and order parameters in a paramagnetic space group- magnetic

subgroup phase transition

### **MAGNEXT:** Systematic absences of msgs

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Received 26 June 2012 Accepted 8 October 2012 Magnetic symmetry in the Bilbao Crystallographic Server: a computer program to provide systematic absences of magnetic neutron diffraction

Samuel V. Gallego, Emre S. Tasci, Gemma de la Flor, J. Manuel Perez-Mato\* and Mois I. Aroyo

Departamento de Fisica de la Materia Condensada, Universidad del País Vasco (UPV/EHU), Apartado 644, 48080 Bilbao, Spain. Correspondence e-mail: jm.perez-mato@ehu.es

MAGNEXT is a new computer program available from the Bilbao Crystal-lographic Server (http://www.cryst.ehu.es) that provides symmetry-forced systematic absences or extinction rules of magnetic nonpolarized neutron diffraction. For any chosen Shubnikov magnetic space group, the program lists all systematic absences, and it can also be used to obtain the list of the magnetic space groups compatible with a particular set of observed systematic absences.

### **MAGNEXT: Magnetic Systematic Absences**

tinction rules for any Shubnikov magnetic

be obtained introducing the I for this purpose at the pted form of the structure

a set of generators in any patible with a set of or a superspace group

Option A: Systematic absences for a magnetic space group in standard settings

Magnetic Space Group number: Please, enter the label of group or choose it

Standard/Default Setting

Other interfaces for alternative uses MAGNEXT are:

- Option B: For systematic absences for a magnetic space group in any setting, click here
  - . Option C: For a list of magnetic space groups compatible with a given set of systematic absences, click here
  - For systematic absences for magnetic superspace groups click here

also for incommensurate magnetic structures from the input of its superspace group operations

## Systematic Absences of the magnetic space group $P_c31c$ (#159.64) in the setting (3a, 3b, 2c; 0, 0, 0) parent space group P-3m1 (No. 164)

Values of h, k, l: h integer, k integer, I integer

Warning: h, k, l are referred to the parent-like setting

This systematic extinction does not necessarily means that atomic moments are along c !!!!

#### Systematic absences for general reflections (produced by centrings):

Diffraction vector type: (h k l) -> Systematic absence: I = 2n or h + 2k /= 3n

#### Systematic absences for special reflections:

Diffraction vector type: (0 0 I) -> Systematic absence: I any

For 1 = 1: I = 0 F = (0,0,Fz)

[Show form of structure factor for every type of reflection]

## **Symmetry-adapted form of the Structure Factors**

Values of h, k, l: h integer, k integer, l integer

Warning: h, k, I are referred to the parent-like setting

#### Structure factors for general reflections (produced by centrings):

Diffraction vector type: h,k,l

For 
$$1 = 2n$$
 or  $h + 2k \neq 3n$ :  $I = 0$   $F = (0,0,0)$   
Elsewhere:  $I \neq 0$   $F = (Fx,Fy,Fz)$ 

#### **Structure factors for special reflections:**

Those diffraction vector types which are fully absent due to the general rule are not listed

Diffraction vector type: 0,0,1

For 
$$1 = 1$$
:  $I = 0$   $F = (0,0,Fz)$ 

Diffraction vector type: **0,k,l** 

For 
$$k = 3$$
,  $l = 1$ : I /= 0  $F = (Fx, 2*Fx, Fz)$ 

Diffraction vector type: h,-h,l

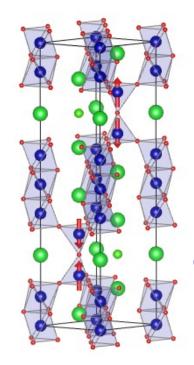
For 
$$h = 3$$
,  $l = 1$ :  $I /= 0$   $F = (Fx, -Fx, Fz)$ 

Diffraction vector type: h,0,I

For 
$$h = 3$$
,  $l = 1$ : I /= 0  $F = (2*Fy,Fy,Fz)$ 

## MAGNEXT can be used to discriminate between possible models:

## Ba<sub>5</sub>Co<sub>5</sub>ClO<sub>13</sub>



nuclear/positional reflection condition:

(2h,-h,I) I=2n

(magnetic sites: 2a, 4e, 4f. all  $(0,0,m_z)$ 

Magnetic diffraction:

Reflection (2, -1, 3) pure magnetic

(2h,-h,l)

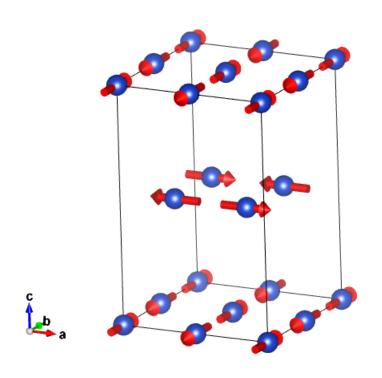
P6<sub>3</sub>' /m' m' c (194.268): absent I even

P6<sub>3</sub>/m' m' c (194.270): absent I odd

( spins are symmetry restricted to be along c in both groups)



## Modelling multi-k structures with KSUBGROUPSMAG & MAGMODELIZE



Nd<sub>2</sub>CuO<sub>4</sub>

Parent SG: 14/mmm

k1 = (1/2, 1/2, 0)

k2=(-1/2,1/2,0)

Cu Site: 2a (0,0,0)

(MAGNDATA 2.6)

Tutorial\_magnetic\_section\_BCS\_3

Parent SG: I4/mmm

$$\mathbf{k}1=(1/2,1/2,0)$$
  
 $\mathbf{k}2=(-1/2,1/2,0)$ 

not necessarily all moments non-zero

Cu Site: 2a (0,0,0)

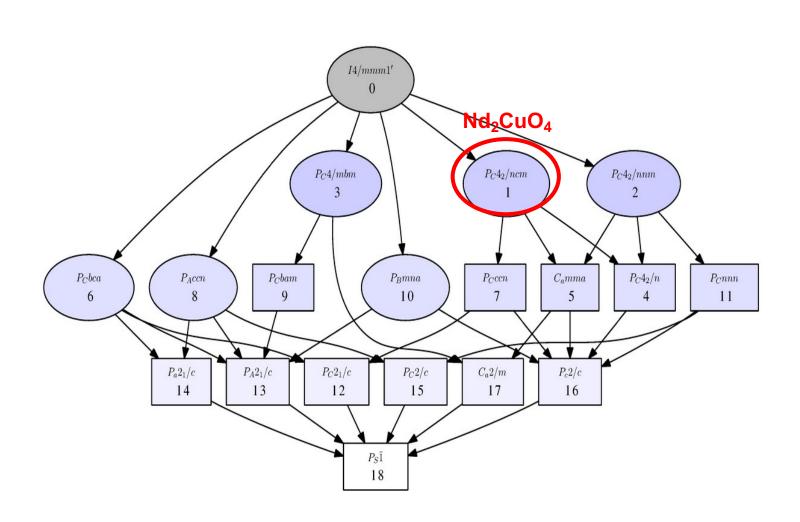
Subgroups of the paramagnetic space group : I4/mmm1 (N. 139) Lowest magnetic space group to consider: P1 (N. 1.1) Wyckoff positions occupied by the magnetic atoms 2a:(0,0,0)

#### List of subgroups which allow a non zero magnetic moment in some sites

Get the subgroup-graph More options

N	Group Symbol	Trans	form	ation	matrix	Group-Subgroup index	Other members of the Conjugacy Class	irreps	Magnetic structure models (MAGMODELIZE)
1	P <sub>C</sub> 4 <sub>2</sub> /ncm (No. 138.529)	$\begin{pmatrix} & 1\\ & 1\\ & 0 \end{pmatrix}$	-1 1 0	0 0 1	$\begin{pmatrix} 1/2 \\ 1/2 \\ 0 \end{pmatrix}$	4=4x1	Conjugacy Class	Get irreps	
2	P <sub>C</sub> 4 <sub>2</sub> /nnm (No. 134.481)	$\begin{pmatrix} & 1\\ & 1\\ & 0 \end{pmatrix}$	-1 1 0	0 0 1	0 0	4=4x1	Conjugacy Class	Get irreps	
3	P <sub>C</sub> 4/mbm (No. 127.397)	$\begin{pmatrix} & 1\\ & 1\\ & 0 \end{pmatrix}$	-1 1 0	0 0 1	0 0	4=4x1	Conjugacy Class	Get irreps	
4	P <sub>C</sub> 4 <sub>2</sub> /n (No. 86.73)	$\begin{pmatrix} & 1\\ & 1\\ & 0 \end{pmatrix}$	-1 1 0	0 0 1	0 0	8=4x2	Conjugacy Class	Get irreps	
5	C <sub>a</sub> mma (No. 67.509)	$\begin{pmatrix} & 2 \\ & 0 \\ & 0 \end{pmatrix}$	0 2 0	0 0 1	$\begin{pmatrix} 1/2\\1/2\\0\end{pmatrix}$	8=4x2	Conjugacy Class	Get irreps	
6	P <sub>C</sub> bca (No. 61.439)	$\begin{pmatrix} & 1 \\ & -1 \\ & 0 \end{pmatrix}$	1 1 0	0 0 1	0 0	8=4x2	Conjugacy Class	Get irreps	
7	P <sub>C</sub> ccn (No. 56.375)	$\begin{pmatrix} & 1\\ & 1\\ & 0 \end{pmatrix}$	-1 1 0	0 0 1	0 0	8=4x2	Conjugacy Class	Get irreps	
8	Pacen (No. 56.374)	0	1	-1 1	0	8=4x2	Conjugacy Class	Get irreps	

Possible magnetic symmetries for a magnetic phase with two propagation vectors (1/2,1/2,0) and (-1/2,1/2,0), parent space group I4/mmm and magnetic atom at site 2a.



Parent SG: 14/mmm

$$\mathbf{k}1 = (1/2, 1/2, 0)$$
  
 $\mathbf{k}2 = (-1/2, 1/2, 0)$ 

not necessarily all moments non-zero

Cu Site: 2a (0,0,0)

Subgroups of the paramagnetic space group:

Lowest magnetic space group to consider:

P1 (N. 139)

Wyckoff positions occupied by the magnetic atoms

2a:(0,0,0)

#### List of subgroups which allow a non zero magnetic moment in some sites

More options

Get the subgroup-graph

Group-Subgroup Other members of Magnetic structure models **Group Symbol Transformation matrix** index the Conjugacy Class (MAGMODELIZE) Conjugacy Class Get irreps 1/2 1 Pc42/ncm (No. 138.529)  $4 = 4 \times 1$ Conjugacy Class Get irreps 2 Pc42/nnm (No. 134.481)  $4 = 4 \times 1$ Conjugacy Class Get irreps 3 P<sub>C</sub>4/mbm (No. 127.397) 4=4x1 0 Conjugacy Class Get irreps P<sub>C</sub>4<sub>2</sub>/n (No. 86.73) 8 = 4x21/2 2 0 0 1 Conjugacy Class Get irreps C<sub>a</sub>mma (No. 67.509) 8 = 4x2Conjugacy Class 0 Get irreps P<sub>C</sub>bca (No. 61.439) 8=4x2 Conjugacy Class Get irreps P<sub>C</sub>ccn (No. 56.375) 8 = 4x20) Conjugacy Class Get irreps Paccn (No. 56,374) 8=4x2

# The MSG symmetry is the result of a magnetic ordering according to a single irrep of the gray parent group Landau condition fulfilled.

List of physically irreducible representations and order parameters between a parent group and a given subgroup.

#### Input data

Group→subgroup	Transform	tion matrix
I4/mmm1' (N. 139.532)→P <sub>C</sub> 4 <sub>2</sub> /ncm (N. 138.529)	$\begin{pmatrix} & 1 & -1 \\ & 1 & & b \\ & & 0 & & b \end{pmatrix}$	$     \begin{bmatrix}       0 & 1/2 \\       0 & 1/2 \\       1 & 0     \end{bmatrix} $

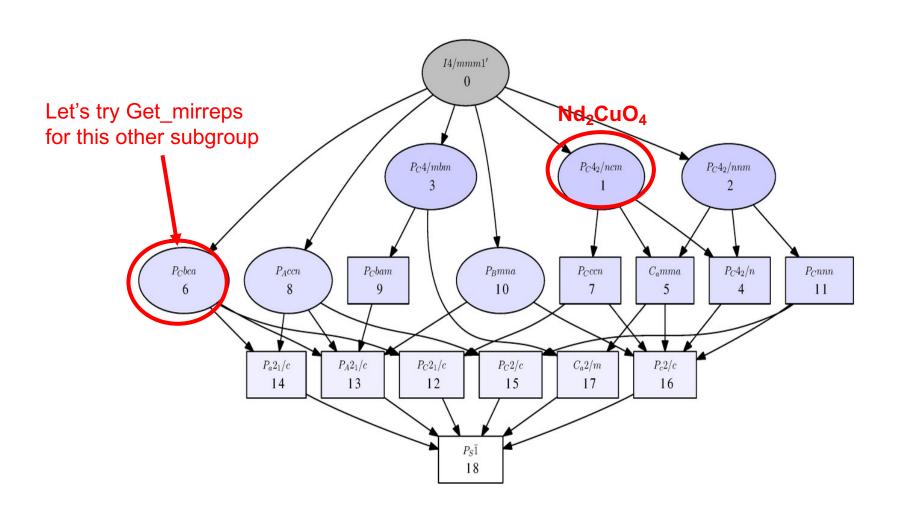
## Output of Get\_mirrreps for this subgroup

#### Representations and order parameters

Show the graph of isotropy subgroups

k-vectors	irreps and order parameters	isotropy subgrou transfermation ma	
GM: (0,0,0)	GM <sub>1</sub> <sup>+</sup> : (a)	/4/mm/n1' (No. 139.5 a,b,c;0,0,0	matrices of the irreps
X: (1/2,1/2,0)(1/2,1/2,1)	mX <sub>3</sub> <sup>+</sup> : (a,-a)	P <sub>C</sub> 4 <sub>2</sub> /ncm (No. 138.5 a+b,-a+b,c;1/2,1/2	matrices of the irrens
M: (1,1,1)	M <sub>2</sub> <sup>+</sup> : (a)	P4 <sub>2</sub> /mmc1' (No. 131. a,b,c;0,1/2,0	matrices of the irreps

Possible magnetic symmetries for a magnetic phase with two propagation vectors (1/2,1/2,0) and (-1/2,1/2,0), parent space group I4/mmm and magnetic atom at site 2a.



# The MSG symmetry is NOT the result of a magnetic ordering according to a single irrep of the gray parent group Landau condition NOT fulfilled.

List of physically irreducible representations and order parameters between a parent group and a given subgroup.

#### Input data

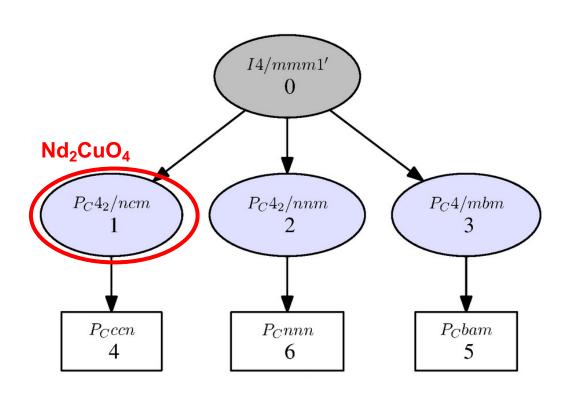
Group→subgroup	Т	ransf	orma	tior	matrix
/4/mmm1' (N. 139.532)→P <sub>C</sub> bca (N. 61.439)	(	-1 -1 0	1 1 0		0 0 0

#### Representations and order parameters

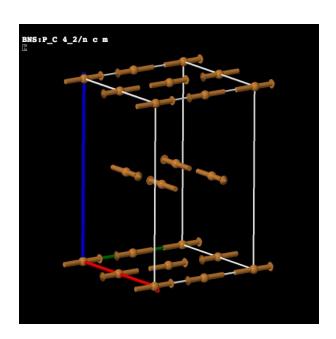
Show the graph of isotropy subgroups

k-vectors	irreps and order parameters	isotropy subgroup transformation matrix	link to the irreps	
CM: (0.0.0)	GM <sub>1</sub> <sup>+</sup> : (a)	/4/mmm1 (No. 139.532 a p,c;0,0,0		
GM: (0,0,0)	GM <sub>4</sub> <sup>+</sup> : (a)	Fmmn 1' (No. 69.522) a+**,-a+b,c;0,0,0	matrices of the irreps	
	mX <sub>2</sub> <sup>+</sup> : (a,0)	C <sub>A</sub> mca (No. 64.480) c,-a+b,-a-b;0,0,0		
X: (1/2,1/2,0)(1/2,1/2,1)	mX <sub>3</sub> <sup>+</sup> : (0,a)	C <sub>A</sub> mca (No. 64.480) a+b,-c,-a+b;0,0,0	matrices of the irreps	
M: <b>(1,1,1)</b>		Cmca1' (No. 64.470) a-b,a+b,c;0,0,0	matrices of the irreps	

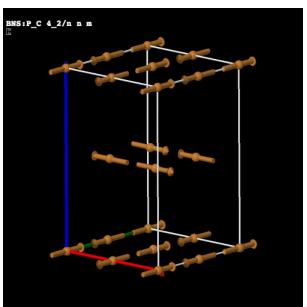
Possible magnetic symmetries for a magnetic phase with two propagation vectors (1/2,1/2,0) and (-1/2,1/2,0), parent space group I4/mmm and magnetic atom at site 2<sup>a</sup>, and a single primary irrep active (Landau condition)



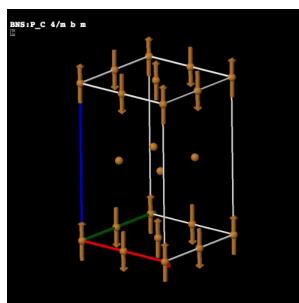
Scheme of the three possible 2k magnetic structures of maximal symmetry with propagation vectors (1/2,1/2,0) and (-1/2,1/2,0), parent space Igroup I4/mmm, magnetic atom at site 2a, and a single primary irrep active.



P<sub>c</sub>4<sub>2</sub>/ncm (a+b,-a+b,c; ½, ½, 0)



P<sub>c</sub>4<sub>2</sub>/nnm (a+b,-a+b,c; 0, 0, 0)



P<sub>C</sub>4<sub>2</sub>/mbm (a+b,-a+b,c; 0, 0, 0)

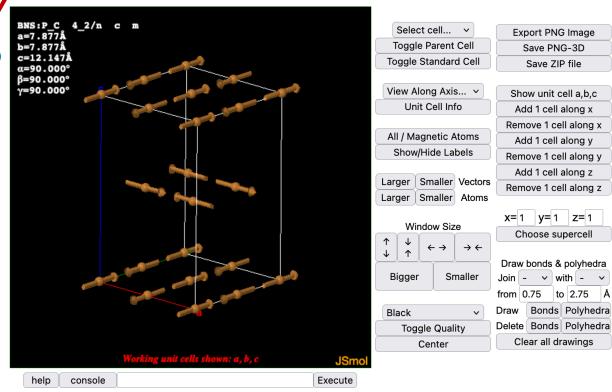
## MVISUALIZE: 3D Visualization of magnetic structures with Jmol

#### **MVISUALIZE Main Page**

Download complete mcif file (including all tags needed for submission to MAGNI ATA)

Domain-related equivalent descriptions

Show/Hide File



**Export PNG Image** 

Save PNG-3D

Save ZIP file

Show unit cell a,b,c

Add 1 cell along x Remove 1 cell along x

Add 1 cell along y

Remove 1 cell along y Add 1 cell along z

Remove 1 cell along z

x = 1 y = 1 z = 1

Choose supercell

Draw bonds & polyhedra

Join - v with - v from 0.75 to 2.75 Å

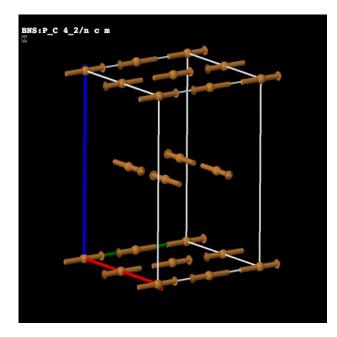
Clear all drawings

Symmetry-adapted form of material tensors via MTENSOR Symmetry-adapted form of material tensors for domain-related equivalent structures via MTENSOR

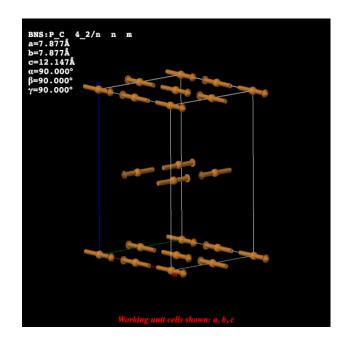
## **Domain-related equivalent structures**

N	Coset repres	entatives	Transformation matrix					Magnetic
IN .	(x,y,z) form	Seitz notation						Structure
1	x,y,z,+1	{1 0}	(	1 1 0	-1 1 0	0 0 1	0 0	Show
2	x+3/2,y+1/2,z+1/2,+1	{ 1   3/2 1/2 1/2 }	(	1 1 0	-1 1 0	0 0 1	3/2 1/2 1/2	Show

{1 | ½ ½ ½ }

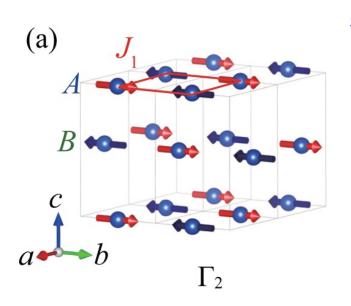


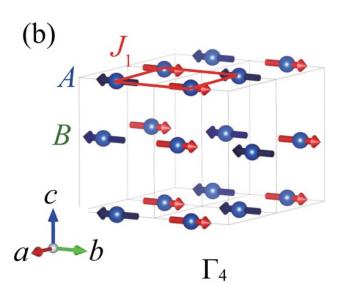
 $P_C4_2/ncm$  (a+b,-a+b,c;  $\frac{1}{2}$ ,  $\frac{1}{2}$ , 0)



P<sub>C</sub>4<sub>2</sub>/ncm (a+b,-a+b,c; ½, ½, ½)

## The confusion between EQUIVALENT (domain-related) magnetic structures and DIFFERENT models fitting equally the diffraction data





SrLaCuSbO<sub>6</sub> (MAGNDATA #1.674)

Phys. Rev. B (2022)  $\mathbf{k} = (\frac{1}{2} \frac{1}{2} 0)$ 

These two arrangements are reported to fit equally well the data....They are claimed to correspond to two different irreps and represent two different alternative models...

BUT in fact: ... they are the **SAME** magnetic structure!

They are related by some of the lost symmetry operations. They represent the two forms that the same magnetic ordering can be realized in the parent structure, forming twin domains

The two irreps are complex conjugate: they cannot yield different REAL magnetic arrangements! They form a SINGLE PHYSICALLY irreducible representation

## **Consequences of symmetry**

## From Neumann's principle:

- all variables/parameters/degrees of freedom compatible with the symmetry will be present (their magnitude may be small or large, but they are not forced to be zero).
- Tensor crystal properties are constrained by the (magnetic) point group symmetry of the crystal.
- Reversely: any tensor property allowed by the (magnetic) point group symmetry can exist (large or small, but it is not forced to be zero)

Magnetic point group symmetry assumes a non-zero SOC, and therefore it necessarily includes all possible SOC effects, independently of their magnitude.

MPGs do NOT introduce constraints that can be broken by spin-orbit (SOC) effects

## MTENSOR: Symmetry-adapted form of crystal tensors properties of magnetic crystals

Madhatic St	ymmetry and	1 Ann	licatione
			IIGALIUIIS

MGENPOS General Positions of Magnetic Space Groups

MWYCKPOS Wyckoff Positions of Magnetic Space Groups

MKVEC 
The k-vector types and Brillouin zones of Magnetic Space Groups

IDENTIFY MAGNETIC GROUP Identification of a Magnetic Space Group from a set of generators in an

arbitrary setting

BNS2OG Transformation of symmetry operations between BNS and OG settings

mCIF2PCR Transformation from mCIF to PCR format (FullProf).

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vector

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(supports the CIF, mCIF, VESTA, VASP formats -- with magnetic information where available)

k-SUBGROUPSMAG Magnetic subgroups consistent with some given propagation vector(s) or a

supercell

MAGNDATA A collection of magnetic structures with portable cif-type files

MVISUALIZE 3D Visualization of magnetic structures with Jmol

MAGNETIC REP. Decomposition of the magnetic representation into irreps

Get mirreps Irreps and order parameters in a paramagnetic space group- magnetic

subgroup phase transition



#### **MTENSOR: Tensor calculation for Magnetic Point Groups**

For the symmetry-adapted form of non-magnetic crystal tensors see TENSOR

#### **Tensor calculation for Magnetic Point Groups**

MTENSOR provides the symmetry-adapted form of tensor properties for any magnetic point (or space) group. On the one hand, a point or space group must be selected. On the other hand, a tensor must be defined by the user or selected from the lists of known equilibrium, optical, nonlinear optical susceptibility and transport tensors, gathered from scientific literature. If a magnetic point or space group is defined and a known tensor is selected from the lists the program will obtain the required tensor from an internal database; otherwise, the tensor is calculated live. Live calculation of tensors may take too much time and even exceed the time limit, giving an empty result, if high-rank tensors, and/or a lot of symmetry elements are introduced.

Tutorial of MTENSOR: download

Further information can be found here

If you are using this program in the preparation of an article, please cite this reference:

Gallego et al. "Automatic calculation of symmetry-adapted tensors in magnetic and non-magnetic materials: a new tool of the Bilbao Crystallographic Server" Acta Cryst. A (2019) **75**, 438-447.

Please, enter a magnetic point group or a magnetic space group: Magnetic Point or Space Group number: choose it Please, choose a tensor by one of these ways: Choose a tensor from the lists Show symmetry-adapted tensors for all the magnetic point groups in standard setting (this overrides previous choices) **EQUILIBRIUM TENSORS OPTICAL TENSORS NONLINEAR OPTICAL SUSCEPTIBILITY TENSORS** TRANSPORT TENSORS Build your own tensor - Introduce Jahn's symbol without superscripts. Examples: (1) [[V2][V2]], (2) a{V2}\*, (3) (V2[V2])\*

Detailed information in. Gallego et al., Acta Cryst. A (2019) 75, 438-447. and tutorial: Tutorial\_magnetic\_section\_BCS\_1.pdf

## MTENSOR: Symmetry-adapted form of crystal tensors properties of magnetic crystals

M	lagnetic Symmetry and Applications
MGENPOS	General Positions of Magnetic Space Groups
MWYCKPOS	Wyckoff Positions of Magnetic Space Groups
MKVEC A	The k-vector types and Brillouin zones of Magnetic Space Groups
IDENTIFY MAGNETIC GROUP	Identification of a Magnetic Space Group from a set of generators in an arbitrary setting
BNS2OG	Transformation of symmetry operations between BNS and OG settings
mCIF2PCR	Transformation from mCIF to PCR format (FullProf).
MPOINT	Magnetic Point Group Tables
MAGNEXT	Extinction Rules of Magnetic Space Groups
MAXMAGN	Maximal magnetic space groups for a given space group and a propagation vector
MAGMODELIZE	Magnetic structure models for any given magnetic symmetry
STRCONVERT	Convert & Edit Structure Data (supports the CIF, mCIF, VESTA, VASP formats with magnetic information where available)
k-SUBGROUPSMAG	Magnetic subgroups consistent with some given propagation vector(s) or a supercell
MAGNDATA	A collection of magnetic structures with portable cif-type files
MVISUALIZE	3D Visualization of magnetic structures with Jmol
MTENSOR A	Symmetry-adapted form of crystal tensors in magnetic phases
MAGNETIC REP.	Decomposition of the magnetic representation into irreps

subgroup phase transition

**Get\_mirreps** 

Irreps and order parameters in a paramagnetic space group- magnetic

## **122 Magnetic Point Groups**

## from **MPOINT**

### **Magnetic Point Group Tables**

(Labels are presented in UNI notation - to see them in the Hermann-Mauguin notation click here)

Choose a magnetic point group from the next table

1.1.1	1.1	1.2.2	1.1'	2.1.3	-1.1	2.2.4	-1.1'	2.3.5	-1'	3.1.6	2.1	3.2.7	2.1'	3.3.8	2'
4.1.9	m.1	4.2.10	m.1'	4.3.11	m'	5.1.12	2/m.1	5.2.13	2/m.1'	5.3.14	2'/m	5.4.15	2/m'	5.5.16	2'/m'
6.1.17	222.1	6.2.18	222.1'	6.3.19	2'2'2	7.1.20	mm2.1	7.2.21	mm2.1'	7.3.22	m'm2'	7.4.23	m'm'2	8.1.24	mmm.1
8.2.25	mmm.1'	8.3.26	m'mm	8.4.27	m'm'm	8.5.28	m'm'm'	9.1.29	4.1	9.2.30	4.1'	9.3.31	4'	10.1.32	-4.1
10.2.33	-4.1'	10.3.34	-4'	11.1.35	4/m.1	11.2.36	4/m.1'	11.3.37	4'/m	11.4.38	4/m'	11.5.39	4'/m'	12.1.40	422.1
12.2.41	422.1'	12.3.42	4'22'	12.4.43	42'2'	13.1.44	4mm.1	13.2.45	4mm.1'	13.3.46	4'm'm	13.4.47	4m'm'	14.1.48	-42m.1
14.2.49	-42m.1'	14.3.50	-4'2'm	14.4.51	-4'2m'	14.5.52	-42'm'	15.1.53	4/mmm.1	15.2.54	4/mmm.1'	15.3.55	4/m'mm	15.4.56	4'/mm'm
15.5.57	4'/m'm'm	15.6.58	4/mm'm'	15.7.59	4/m'm'm'	16.1.60	3.1	16.2.61	3.1'	17.1.62	-3.1	17.2.63	-3.1'	17.3.64	-3'
18.1.65	32.1	18.2.66	32.1'	18.3.67	32'	19.1.68	3m.1	19.2.69	3m.1'	19.3.70	3m'	20.1.71	-3m.1	20.2.72	-3m.1'
20.3.73	-3'm	20.4.74	-3'm'	20.5.75	-3m'	21.1.76	6.1	21.2.77	6.1'	21.3.78	6'	22.1.79	-6.1	22.2.80	-6.1'
22.3.81	-6'	23.1.82	6/m.1	23.2.83	6/m.1'	23.3.84	6'/m	23.4.85	6/m'	23.5.86	6'/m'	24.1.87	622.1	24.2.88	622.1'
24.3.89	6'22'	24.4.90	62'2'	25.1.91	6mm.1	25.2.92	6mm.1'	25.3.93	6'mm'	25.4.94	6m'm'	26.1.95	-6m2.1	26.2.96	-6m2.1'
26.3.97	-6'm'2	26.4.98	-6'm2'	26.5.99	-6m'2'	27.1.100	6/mmm.1	27.2.101	6/mmm.1'	27.3.102	6/m'mm	27.4.103	6'/mmm'	27.5.104	6'/m'mm'
27.6.105	6/mm'm'	27.7.106	6/m'm'm'	28.1.107	23.1	28.2.108	23.1'	29.1.109	m-3.1	29.2.110	m-3.1'	29.3.111	m'-3'	30.1.112	432.1
30.2.113	432.1'	30.3.114	4'32'	31.1.115	-43m.1	31.2.116	-43m.1'	31.3.117	-4'3m'	32.1.118	m-3m.1	32.2.119	m-3m.1'	32.3.120	m'-3'm
32 4 12	m-3m'	32 5 122	m'-3'm'												

II et al.

## **Magnetic Point Group Tables of 42'2' (#12.4.43)**

## from **MPOINT**

N	(x,y,z) form	matrix form	Seitz symbol
1	x,y,z, +1 m <sub>x</sub> ,m <sub>y</sub> ,m <sub>z</sub>	$\left(\begin{array}{cccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array}\right)$	{1 0}
2	-x,-y,z, +1 -m <sub>x</sub> ,-m <sub>y</sub> ,m <sub>z</sub>	$\left(\begin{array}{cccc} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{array}\right)$	{ 2 <sub>001</sub>   0 }
3	-y,x,z, +1 -m <sub>y</sub> ,m <sub>x</sub> ,m <sub>z</sub>	$ \left(\begin{array}{cccc} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{array}\right) $	{ 4 <sup>+</sup> 001   0 }
4	y,-x,z, +1 m <sub>y</sub> ,-m <sub>x</sub> ,m <sub>z</sub>	$\left(\begin{array}{cccc} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{array}\right)$	{ 4 <sup>-</sup> 001   0 }
5	x,-y,-z, -1 -m <sub>x</sub> , m <sub>y</sub> , m <sub>z</sub>	$\left(\begin{array}{cccc} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{array}\right)'$	{ 2'100   0 }
6	-x,y,-z, -1 m <sub>x</sub> , -m <sub>y</sub> , m <sub>z</sub>	$\left(\begin{array}{cccc} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{array}\right)'$	{ 2'010   0 }
7	-y,-x,-z, -1 m <sub>y</sub> , m <sub>x</sub> , m <sub>z</sub>	$\left(\begin{array}{cccc} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{array}\right)'$	{ 2'1-10   0 }
8	y,x,-z, -1 -m <sub>y</sub> , -m <sub>x</sub> , m <sub>z</sub>	\[ \begin{pmatrix} 0 & 1 & 0 & \\ 1 & 0 & 0 & \\ 0 & 0 & -1 & \end{pmatrix} \end{pmatrix},	{ 2'110   0 }

Subgroups Table

#### **MTENSOR: Tensor calculation for Magnetic Point Groups**

For the symmetry-adapted form of non-magnetic crystal tensors see TENSOR

#### **Tensor calculation for Magnetic Point Groups**

MTENSOR provides the symmetry-adapted form of tensor properties for any magnetic point (or space) group. On the one hand, a point or space group must be selected. On the other hand, a tensor must be defined by the user or selected from the lists of known equilibrium, optical, nonlinear optical susceptibility and transport tensors, gathered from scientific literature. If a magnetic point or space group is defined and a known tensor is selected from the lists the program will obtain the required tensor from an internal database; otherwise, the tensor is calculated live. Live calculation of tensors may take too much time and even exceed the time limit, giving an empty result, if high-rank tensors, and/or a lot of symmetry elements are introduced.

Tutorial of MTENSOR: download

Further information can be found here

If you are using this program in the preparation of an article, please cite this reference:

Gallego et al. "Automatic calculation of symmetry-adapted tensors in magnetic and non-magnetic materials: a new tool of the Bilbao Crystallographic Server" Acta Cryst. A (2019) **75**, 438-447.

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Detailed information in. Gallego et al., Acta Cryst. A (2019) 75, 438-447. and tutorial: Tutorial\_magnetic\_section\_BCS\_1.pdf

	/ NJ		
aeV <sup>2</sup>	Isothermal magnetoelectric effect tensor (inverse effect) A <sup>T</sup> <sub>ij</sub>	$M_i=A^T_{ij}D_j$	0
	Magnetoelectric tensor (direct effect) α <sub>ij</sub>	P <sub>i</sub> =α <sub>ij</sub> H <sub>j</sub>	0
	Magnetoelectric tensor (inverse effect) $\alpha^{T}_{ij}$	$M_i = \alpha^T_{ij} E_j$	0
	Acoustoelectricity tensor ρ <sub>ijk</sub>	$\sigma_{ij} = \rho_{ijk} J_k$	0
$[V^2]V$	Isothermal piezoelectric tensor (inverse effect) e <sup>T</sup> <sub>ijk</sub>	σ <sub>ij</sub> =-e <sup>T</sup> ijkE <sub>k</sub>	0
	Piezoelectric tensor (inverse effect) d <sup>T</sup> ijk	$\epsilon_{ij}$ =d $^{T}_{ijk}$ E $_{k}$	0
	Isothermal piezoelectric tensor (direct effect) e <sub>ijk</sub>	$D_i=e_{ijk}\epsilon_{jk}$	0
$V[V^2]$	Piezoelectric tensor (direct effect) d <sub>ijk</sub>	$P_i=d_{ijk}\sigma_{jk}$	0
	Second order magnetoelectric tensor (direct effect) $\alpha_{ijk}$	$P_i = \alpha_{ijk}H_jH_k$	0
a[V <sup>2</sup> ]V	Piezotoroidic tensor (inverse effect) $\gamma^{T}_{ijk}$	$\epsilon_{ij} = \gamma^{T}_{ijk} S_k$	0
aV[V <sup>2</sup> ]	Piezotoroidic tensor (direct effect) γ <sub>ijk</sub>	$T_i = \gamma_{ijk}\sigma_{jk}$	0
n /2n /	Isothermal piezomagnetic tensor (inverse effect) e <sup>mT</sup> ijk	σ <sub>ij</sub> =-e <sup>mT</sup> ijkH <sub>k</sub>	0
ae[V <sup>2</sup> ]V	Piezomagnetic tensor (inverse effect) $\Lambda^{T}_{ijk}$	$\epsilon_{ij} = \Lambda^{T}_{ijk} H_k$	0
	Isothermal piezomagnetic tensor (direct effect) e <sup>m</sup> ijk	$M_i=e^m_{ijk}\epsilon_{jk}$	0
aeV[V <sup>2</sup> ]	Piezomagnetic tensor (direct effect) $\Lambda_{ijk}$	$M_i = \Lambda_{ijk} \sigma_{jk}$	0
40 v[v ]	Second order magnetoelectric tensor (inverse effect) $\alpha^{T}_{ijk}$	$M_i = \alpha^T_{ijk} E_j E_k$	0
	Elastic compliance tensor S <sub>ijkl</sub>	$\epsilon_{ij}$ =S $_{ijkl}\sigma_{kl}$	0
$[[V^2][V^2]]$	Elastic stiffness tensor C <sub>ijkl</sub>	$\sigma_{ij}$ = $C_{ijkl}\epsilon_{kl}$	0
	Viscosity tansor n	σ::=n::λε/λŧ	

## Jahn Symbols: rank 1 tensors

	V	eV	aV	aeV
R	<b>R</b> .T	det(R)R.T	<b>R</b> .T	det(R)R.T
R'	<b>R</b> .T	det( <b>R</b> ) <b>R</b> .T	-R.T	-det( <b>R</b> ) <b>R</b> .T

Intrinsic symmetry	Tensor description	Defining equation
	Electric polarization vector P <sub>i</sub>	-
	Electrocaloric effect tensor p <sup>T</sup> <sub>i</sub>	$\Delta S=p^{T}_{i}E_{i}$
V	Electrothermal effect tensor t <sub>i</sub>	E <sub>i</sub> =-t <sub>i</sub> ΔT
<b>v</b>	Heat of polarization tensor t <sup>T</sup> i	ΔS=t <sup>T</sup> iΔPi
	Piezoelectric polarization tensor under hydrostatic pressure d <sub>ijj</sub>	P <sub>i</sub> =-d <sub>ijj</sub> p
	Pyroelectric tensor p <sub>i</sub>	$\Delta P_i = p_i \Delta T$
eV	Axial toroidal moment A <sub>i</sub>	-
	Polar Toroidal moment T <sub>i</sub>	-
aV	Pyrotoroidic tensor r <sub>i</sub>	T <sub>i</sub> =r <sub>i</sub> ΔT
	Toroidalcaloric tensor r <sup>T</sup> i	ΔS=r <sup>T</sup> <sub>i</sub> S <sub>i</sub>
	Heat of Magnetization tensor t <sup>T</sup> i	$\Delta S=t^{T}_{i}M_{i}$
	Magnetization vector M <sub>i</sub>	-
aeV	Magnetocaloric tensor q <sup>T</sup> i	$\Delta S = q^{T}_{i}H_{i}$
	Magnetothermal effect tensor ti	H <sub>i</sub> =-t <sub>i</sub> ∆T
	Pyromagnetic tensor (direct effect) qi	M <sub>i</sub> =q <sub>i</sub> ∆T

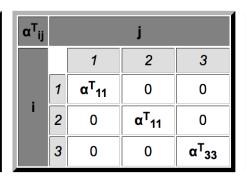
## **MTENSOR**

## Magnetoelectric tensor:

Group 6/m' (#23.4.85)

$\alpha^{T}_{ij}$		j				
		1	2	3		
	1	α <sup>T</sup> 11	α <sup>T</sup> 12	0		
'	2	-α <sup>T</sup> <sub>12</sub>	α <sup>T</sup> 11	0		
	3	0	0	α <sup>T</sup> 33		

Group 622 (#24.1.87)



Group 62'2' (#24.4.90)

$\alpha^{\text{T}}_{ij}$		j			
		1	2	3	
	1	0	α <sup>T</sup> 12	0	
•	2	-α <sup>T</sup> <sub>12</sub>	0	0	
	3	0	0	0	

Group 6mm (#25.1.91)

$\alpha^{T}_{ij}$	j			
		1	2	3
١.	1	0	α <sup>T</sup> 12	0
	2	-α <sup>T</sup> <sub>12</sub>	0	0
	3	0	0	0

Number of independent coefficients: 3

Number of independent coefficients: 2

Number of independent coefficients: 1

Number of independent coefficients: 1

Group 6m'm' (#25.4.94)

$\alpha^{\text{T}}_{ij}$			j	
		1	2	3
	1	α <sup>T</sup> 11	0	0
i	2	0	α <sup>T</sup> <sub>11</sub>	0
	3	0	0	α <sup>T</sup> 33

Group -6'm'2 (#26.3.97)

$\alpha^{\text{T}}_{ij}$	j			
		1	2	3
١.	1	α <sup>T</sup> 11	0	0
l '	2	0	α <sup>T</sup> <sub>11</sub>	0
	3	0	0	α <sup>T</sup> 33

Group -6'm2' (#26.4.98)

$\alpha^{\text{T}}_{ij}$		j				
		1	2	3		
	1	0	α <sup>T</sup> <sub>12</sub>	0		
•	2	-α <sup>T</sup> 12	0	0		
	3	0	0	0		

Group 6/m'mm (#27.3.102)

$\alpha^{\text{T}}_{ij}$	j				
		1	2	3	
	1	0	α <sup>T</sup> 12	0	
	2	-α <sup>T</sup> <sub>12</sub>	0	0	
	3	0	0	0	

Number of independent coefficients: 2

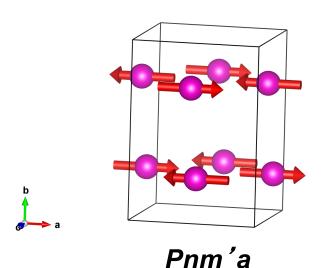
Number of independent coefficients: 2

Number of independent coefficients: 1

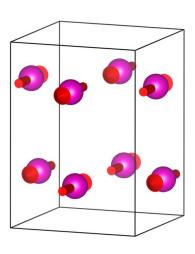
Number of independent coefficients: 1

## **Consequences of symmetry**

## EuZrO<sub>3</sub>: magndata #0.146 & 0.147







Pn'm'a'

#### **Table of tensor components**

$\alpha^{T}_{ij}$			j	
		1	2	3
١.	1	0	0	α <sup>T</sup> 13
'	2	0	0	0
	3	α <sup>T</sup> 31	0	0

Number of independent coefficients: 2

#### Information about the selected tensor

- 2  $^{nd}$  rank Magnetoelectric tensor  $\alpha^T_{ij}$  (inverse effect)
- Axial tensor which inverts under time-reversal symmetry operation
- Defining equation: P<sub>i</sub>=α<sup>T</sup><sub>ij</sub>H<sub>j</sub>
- Relates Magnetic field H with Polarization P
- Intrinsic symmetry symbol: aeV<sup>2</sup>

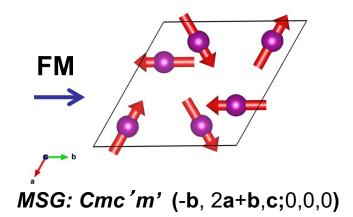
### **Output of MTENSOR**

#### **Table of tensor components**

ſij		j						
		1	2	3				
	1	α <sup>T</sup> 11	0	0				
	2	0	α <sup>T</sup> 22	0				
	3	0	0	α <sup>T</sup> 33				

lumber of independent coefficients: 3

## Mn<sub>3</sub>Sn



Magndata #0.199

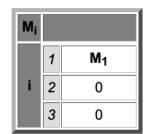
spins are all rotated 90 degrees

MSG: Cm'cm' (-b, 2a+b,c;0,0,0)

Magndata #0.200

## **Magnetization:**

#### **Table of tensor components**

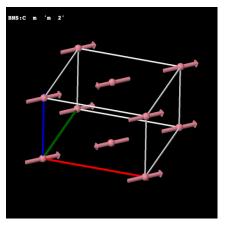


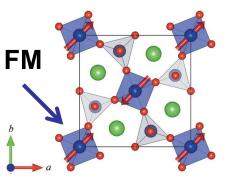
Number of independent coefficients: 1

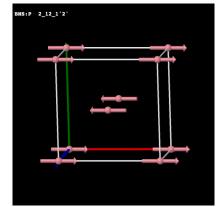
### Table of tensor components

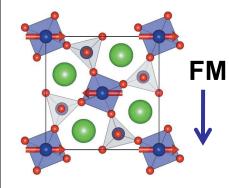
Mi		
	1	0
i	2	M <sub>2</sub>
	3	0

Number of independent coefficients: 1









Cm'm2' (a+b,-a+b,c;1/2,0,0)

 $P2_12_1'2'$  (-**b**,**a**,**c**;0,0,0)

#### **Table of tensor components**

Pi		
	1	0
i	2	0
	3	P <sub>3</sub>

#### Information about the selected tensor

- 1 st rank Electric polarization vector Pi
- Polar tensor invariant under time-reversal symmetry operation
- Intrinsic symmetry symbol: V

non-polar group

P=0

#### Number of independent coefficients:

## Murakawa et al. PRL (2010):

